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A brief review on radiative seesaw models and DM A two-loop model with two or three DM **By products:** * 135 gamma-ray line at the Fermi LAT * Enhancement of h-> two gammas **V** Conclusion

Radiative Seesaw and DM Radiative Neutrino Mass Generation (ZEE,80;86; WOLFENSTEIN,80; BABU,88, ETC)

Radiative Seesaw Mechanism (Kraus, Nasri + Trodden,02; Ma,06; Aoki, Kanemura+ Seto,08; etc)

Unbroken discrete symmetry to forbid the Dirac masses

NR, Inert Higgs, etc are DM candidates.

Three-loop Model Kraus, Nasri + Trodden, 02



Z2-ODD SM SINGLET

NR CAN BE DM.

$$\mathbf{m}_{\nu} = \begin{pmatrix} 0 & 0 \\ 0 & M \end{pmatrix} \rightarrow \begin{pmatrix} m^2/M & 0 \\ 0 & M \end{pmatrix}$$

Radiative Seesaw

One-loop Model Ma, 06



Z2-0DD

INERT SU(2) DOUBLET HIGGS

 $<\eta>=0$

NR and eta are DM candidates.

Eta DM studied by

BARBIERI, HALL + RYCHKOV, 06; LOPEZ, OLIVER + TYTGAT,06; DOLLE + SU,09 ETC

N_R **DM** studied by

Kubo, Ma + Suematsu, 06; Aristizabal Sierra, Kubo, Restrepo, Suematsu +Zapata, 08; Gelmini, Osoba+ Palomares-Ruiz, 09, etc

Three-loop Model

AOKI, KANEMURA+SETO, 08



Z₂ODD

INERT SU(2) DOUBLET HIGGS

 $<\eta>$

	Q^i	u_R^i	d_R^i	L^i	e_R^i	Φ_1	Φ_2	S^{\pm}	η	N_R^{α}
Z_2 (exact)	+	+	+	+	+	+	+	—	_	_
\tilde{Z}_2 (softly broken)	+	_	_	+	+	+	_	+	_	+

Non-susy Models of radiative generation of $\mathcal{m}_{\mathcal{V}}$

Model	L-violating dim.	No. of loops	$ u_R $	No. of stable DMs
[1]	3 (tri-linear scalar coupling)	1	No	0
[2, 3, 21]	3 (tri-linear scalar coupling)	2	No	0
[15]	3 (tri-linear scalar coupling)	1	No	1
[22]	3 (tri-linear scalar coupling))	2	Yes	2
[4, 5, 11]	3 (Majorana mass)	3	Yes	1
[6-9, 12, 14, 23, 24]	3 (Majorana mass)	1	Yes	1
[13]	3 (Majorana mass)	1	Yes $(SU(2)_L \text{ triplet})$	1
[17]	4 (quartic scalar coupling)	1	No	1
[19]	No L-violation	1	Yes	0
[18]	Spontaneous violation	2	No	1
[20]	Sponataneos violation	2	Yes	1
[16]	Spontaneous violation	1	Yes	1
[10]	2 (scalar mass)	1	Yes	0
Our model	2 (scalar mass)	2	Yes	2 or 3

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THE MODEL

Μ

ModelL-violating dim.No. of loops ν_R No. of stable DMsOur model2 (scalar mass)2Yes2 or 3

	field	statistics	$SU(2)_L$	$U(1)_Y$	L	Z_2	Z'_2	D_{2N}
	(u_L, l)	F	2	-1/2	1	+	+	1
	l^c	F	1	1	1	+	+	1
Α	N_R^c	F	1	1	0	_	+	1″
	$H = (H^+, H^0)$	В	2	1/2	0	+	+	1
	$\eta = (\eta^+, \eta^0)$	В	2	1/2	-1		+	1″
· · · · · · · · · · · · · · · · · · ·	χ	В	1	0	0	+		1'
	ϕ	В	1	0	1		_	1‴

MATTER CONTENT (MINIMAL EXTENSION)







TWO LOOP SEESAW

$$m_{\nu} \sim \left(\frac{\kappa}{16\pi^2}\right)^2 \frac{m_D^2}{M_R} \sim 10^{-7} \ \frac{m_D^2}{M_R} \ \text{for } \kappa = 0.1$$

$M_R \sim 1$ TEV IS A NATURAL SCALE.

THE Z2 X Z2 X LINVARIANT QUARTIC COUPLINGS

 $V_{\lambda} = \lambda_{1}(H^{\dagger}H)^{2} + \lambda_{2}(\eta^{\dagger}\eta)^{2} + \lambda_{3}(H^{\dagger}H)(\eta^{\dagger}\eta) + \lambda_{4}(H^{\dagger}\eta)(\eta^{\dagger}H)$ $+ \frac{1}{4}\gamma_{1}\chi^{4} + \gamma_{2}(H^{\dagger}H)\chi^{2} + \gamma_{3}(\eta^{\dagger}\eta)\chi^{2} + \gamma_{4}|\phi|^{4} + \gamma_{5}(H^{\dagger}H)|\phi|^{2}$ $+ \gamma_{6}(\eta^{\dagger}\eta)|\phi|^{2} + \gamma_{7}\chi^{2}|\phi|^{2} + \frac{\kappa}{2}[(H^{\dagger}\eta)\chi\phi + h.c.].$

THE Z2 X Z2 INVARIANT SCALAR MASS TERMS

$$V_m = m_1^2 H^{\dagger} H + m_2^2 \eta^{\dagger} \eta + \frac{1}{2} m_3^2 \chi^2 + m_4^2 |\phi|^2 + \frac{1}{2} m_5^2 [\phi^2 + (\phi^*)^2]$$



COLD DARK MATTER CANDIDATES

field	statistics	$SU(2)_L$	$U(1)_Y$	L	Z_2	Z'_2	D_{2N}
$(u_L, l_)$	F	2	-1/2	1	+	+	1
l^c	F	1	1	1	+	+	1
N_R^c	F	1	1	0	—	+	1″
$H = (H^+, H^0)$	В	2	1/2	0	+	+	1
$\eta = (\eta^+, \eta^0)$	В	2	1/2	-1	—	+	1″
χ	В	1	0	0	+	_	1'
ϕ	В	1	0	1	_	—	1‴

OF DMS=3: $(\eta, \chi, \phi) \operatorname{OR}(N_R^c, \chi, \phi)$ **# OF DMS=2:** $(\eta, \chi) \operatorname{OR}(\chi, \phi)$ ETC

Non-standard annihilations and relic abundance





$$\Omega_T h^2 (\simeq \Omega_\chi h^2) = 0.1157 \pm 0.0046 \ (2\sigma)$$
 with $m_\chi = 135 \ {
m GeV}$



 $\lambda_1 = 0.129 , \ \lambda_3 = -1.26 , \ \lambda_4 = -0.0205$

Bonus

* THE FIRST BONUS: FERMI-LAT 135 GEV GAMMA-RAY LINE



FERMI-LAT IS MEASURING GAMMA RAYS COMING FROM THE UNIVERSE SINCE 2008.

LAT COLLABORATION, ARXIV:1205.2739; ETC

IF THE DATA FROM THE WHOLE SKY IS INCLUDED:



HOWEVER, IF YOU LOOK AT THE CENTER OF THE GALAXY, SOMETHING MORE INTERESTING IS GOING ON.

WENIDER, ARXIV:1204.2797; BRINGMANN ET AL, ARXIV:1203.1312; ETC







WENIGER, JCAP 1208 (2012) 007

LOOKING AT THE CENTER MORE IN DETAIL. (INNER 3 DEGREE RADIUS AROUND THE CENTER)

COHEN ET AL, ARXIV:1207.0800



THE BEST FIT: NO ANNIHILATIONS INTO W^+W^- , ZZ , $Z\gamma$ ETC.

 $\sigma_{\gamma Z}/\sigma_{\gamma \gamma}$



COHEN ET AL, ARXIV:1207.0800

 $\sigma_{W^+W^-}/(2\sigma_{\gamma\gamma}+\sigma_{\gamma Z})$



DILEMMA

* MONOCHROMATIC GAMMA

 $v\sigma_{\gamma\gamma}\simeq 10^{-27}~{
m cm}^3{
m s}^{-1}$ (loop effect)

* CONTINUUM GAMMA

 $v\sigma(\mathbf{DMDM} \to \mathbf{SM}), i.e. v\sigma(\mathbf{DMDM} \to W^+W^-)$ etc $\lesssim 10 \times v\sigma(\mathbf{DMDM} \to \gamma\gamma) \sim 10^{-26} \text{ cm}^3 \text{s}^{-1}$ (TREE LEVEL)

* Observed relic density $\Omega_T h^2 = 0.116$

 $v\sigma(\mathbf{DMDM}) \simeq 10^{-26} \ \mathbf{cm}^3 \mathbf{s}^{-1}$



IN OUR MODEL:





How to realize a large O At the freeze out, while suppressing O in the galaxy, i.e. at low temperature.

IN OUR MODEL:





 $(2\gamma_2,\lambda_3)v_h$

To make the continuum gammas small: For chi DM: small γ_2 For eta DM: small Ω_n

TEMPERATURE DEPENDENT CROSS SECTION:





SEE ALSO: BAEK, KO+SENAHA, ARXIV:1209.1685







* YET ANOTHER BONUS:





VCONCLUSION

A TWO-LOOP SEESAW MODEL IS PROPOSED;

L IS SOFTLY VIOLATED BY A DIM. 2 OPERATOR,
Z_2 X Z_2 IS THE UNBROKEN SYMMETRY, AND
THE HIGGS SECTOR IS MINIMAL.

2 WITH η_R^0 and χ as DM the model has a potential to explain:

*135 GEV GAMMA-RAY LINE OBSERVED AT THE FERMI LAT AND

*ENHANCEMENT OF $h
ightarrow \gamma\gamma$

OBSERVED AT LHC.

TANK YOU VERY MUCH!

$$B(\mu \to e\gamma) = \frac{3\alpha}{64\pi (G_F m_{\eta^{\pm}}^2)^2} \left| \sum_k Y_{\mu k}^{\nu} Y_{ek}^{\nu} F_2\left(\frac{M_k^2}{m_{\eta^{\pm}}^2}\right) \right|^2 \lesssim 2.4 \times 10^{-12}$$
$$F_2(x) = \frac{1}{6(1-x)^4} (1 - 6x + 3x^2 + 2x^3 - 6x^2 \ln x) ,$$

$$\delta a_{\mu} = \frac{m_{\mu}^2}{16\pi^2 m_{\eta\pm}^2} \sum_k Y_{\mu k}^{\nu} Y_{\mu k}^{\nu} F_2 \left(\frac{M_k^2}{m_{\eta\pm}^2}\right)$$
$$|\delta a_{\mu}| \simeq 2.2 \times 10^{-5} B(\mu \to e\gamma) \lesssim 3.4 \times 10^{-11}$$

$$\Delta T \simeq 0.54 \left(\frac{m_{\eta^{\pm}} - m_{\eta_R^0}}{v} \right) \left(\frac{m_{\eta^{\pm}} - m_{\eta_I^0}}{v} \right) = 0.02^{+0.11}_{-0.12}$$

$$(\mathcal{M}_{\nu})_{ij} = \left(\frac{1}{16\pi^2}\right)^2 \frac{\kappa^2 v_h^2}{8} \sum_k Y_{ik}^{\nu} Y_{jk}^{\nu} \int_0^{\infty} dx \{ B_0(-x, m_{\chi}, m_{\phi_R}) - B_0(-x, m_{\chi}, m_{\phi_I}) \} \\ \times \frac{x}{(x+m_{\eta}^2)^2 (x+M_k^2)} \quad \text{for } m_{\eta} = m_{\eta_R^0} \simeq m_{\eta_I^0} \\ \sim -\lambda_5^{\text{eff}} v_h^2 \sum_k \frac{Y_{ik}^{\nu} Y_{jk}^{\nu}}{16\pi^2 M_k} \left(ln \left(\frac{m_{\eta_R^0}}{M_k}\right)^2 + 1 \right) \text{for } m_{\eta} << M_k ,$$

Coupled Boltzmann eqs.

D'ERAMO+THALER, 11, BELANGER, KANNIKE, PUKOV+RAIDAL, 12; AOKI, DUERR, KUBO+TAKANO, 12.

 $\bullet \bullet \rightarrow xx$

standard

 $\begin{aligned} \frac{dY_i}{dx} &= -0.264 \ g_*^{1/2} \left[\frac{\mu M_{\rm PL}}{x^2} \right] \left\{ \begin{array}{l} < \sigma(ii; X_i X'_i) v > \left(Y_i Y_i - \bar{Y}_i \bar{Y}_i \right) \\ + \sum_{i>j} < \sigma(ii; jj) v > \left(Y_i Y_i - \frac{Y_j Y_j}{\bar{Y}_j \bar{Y}_j} \bar{Y}_i \bar{Y}_i \right) - \sum_{j>i} < \sigma(jj; ii) v > \left(Y_j Y_j - \frac{Y_i Y_i}{\bar{Y}_i \bar{Y}_i} \bar{Y}_j \bar{Y}_j \right) \\ \\ \end{array} \\ \begin{array}{l} \\ \end{array} \\ + \sum_{j,k} < \sigma(ij; kX_{ijk}) v > \left(Y_i Y_j - \frac{Y_k}{\bar{Y}_k} \bar{Y}_i \bar{Y}_j \right) - \sum_{j,k} < \sigma(jk; iX_{jki}) v > \left(Y_j Y_k - \frac{Y_i}{\bar{Y}_i} \bar{Y}_j \bar{Y}_k \right) \right\} \end{aligned}$

$$Y_i = n_i / s$$
 $\mu = (\sum_i m_i^{-1})^{-1}$

 $m_1 = 200 \text{ GeV}, m_2 = 160 \text{ GeV}, m_3 = 140 \text{ GeV}$

STANDARD: $\sigma_{0,1} = 0.1$, $\sigma_{0,2} = 2$, $\sigma_{0,3} = 6$

Temperature evolution



 $\sigma_{0,123} = \sigma_{0,312} = \sigma_{0,231} = 5.1$



LOPEZ, OLIVER AND TYTGAT,'06

Only low mass and higher mass regimes are allowed.

m_{χ} [GeV]

SUSY

Higgsino:

 $\begin{aligned} \sigma_{\gamma\gamma}v &\simeq 1.1 \times 10^{-28} \text{ cm}^3/\text{s} \\ \sigma_{\gamma_Z}v &\simeq 3.7 \times 10^{-28} \text{ cm}^3/\text{s} \\ \sigma_{\text{ann}}v &\simeq \sigma_{WW}v + \sigma_{ZZ}v &\simeq 4.2 \times 10^{-25} \text{ cm}^3/\text{s} \end{aligned}$

Wino:

$$\begin{aligned} \sigma_{\gamma\gamma}v &\simeq 2.5 \times 10^{-27} \text{ cm}^3/\text{s} \\ \sigma_{\gamma_Z}v &\simeq 1.4 \times 10^{-26} \text{ cm}^3/\text{s} \\ \sigma_{\text{ann}}v &\simeq \sigma_{WW}v &\simeq 4.0 \times 10^{-24} \text{ cm}^3/\text{s} \end{aligned}$$

Bino:

$$\sigma_{\gamma\gamma} v \simeq \text{few} \times 10^{-30} \text{ cm}^3/\text{s};$$

$$\sigma_{\gamma_Z} v \simeq \text{few} \times 10^{-31} \text{ cm}^3/\text{s};$$

$$\sigma_{\text{ann}} v \simeq \sigma_{\ell\bar{\ell}} v \simeq \text{few} \times 10^{-27} \text{ cm}^3/\text{s}.$$

NEUTRALINO DM CAN NOT EXPLAIN THE 130 GAMMA RAY LINE.

BUCHMÜLLER+GARNY, JCAP 1208 (2012)035; COHEN ET AL, ARXIV:1207.0800 DM mass $m_{\rm DM}$ [GeV]



BELANGER ET AL, ARXIV:1208.5009