

2HDMs *(Two Higgs doublet models)*

P R E S E N T A T I O N

Koji TSUMUTA (Nagoya U.)

**Higgs as a Probe of New Physics 2013
Toyama, Japan**

13-16/2/2013

2HDMs **Towards ILC** *(Two Higgs doublet models)*

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- ❖ **Extended Higgs sector**
 - ρ parameter and FCNC
- ❖ **2HDM (two-Higgs-doublet model)**
 - Model & experimental status
- ❖ **Leptophilic 2HDM**
- ❖ **$\tan\beta$ measurement**
- ❖ **Summary**

Introduction

Whether

“the” Higgs boson in the SM,
or “a” Higgs boson?

Introduction

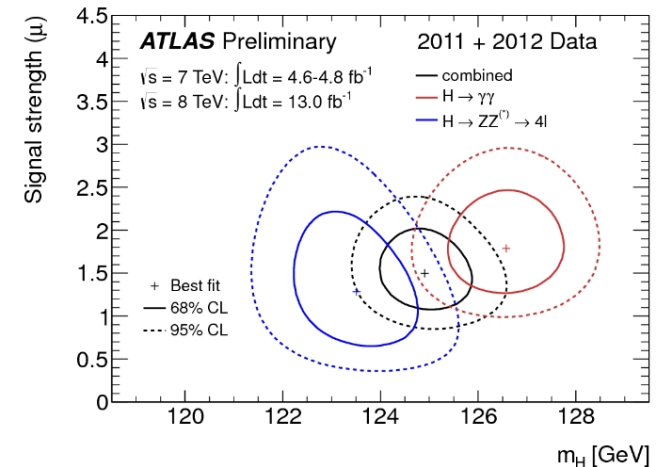
Whether

“the” Higgs boson in the SM,

or “a” Higgs boson,

or Higgs bosons,

or dilaton, etc...



Guideline for Ext. Higgs sector

❖ **Electroweak ρ parameter:**
$$\rho = \frac{\sum_{\alpha} (I_{\alpha}(I_{\alpha} + 1) - Y_{\alpha}^2) v_{\alpha}^2}{\sum_{\beta} 2Y_{\beta}^2 v_{\beta}^2}$$
 Veltman (1977)

- ❖ Precision data suggests [$\rho \sim 1$]
- ❖ SM predicts [$\rho = 1$] @ tree level

❖ **FCNC** (Flavor Changing Neutral Current)

- ❖ No FCNC @ tree level
- ❖ GIM suppression @ 1-loop

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❖ Singlet/**Doublet** w/ $Y=1/2$ VEV (or Inert multiplets) preserves $\rho=1$

- ❖ Minimal extension
- ❖ Mix w/ Higgs
- ❖ No contrib. to EWSB

- ❖ Not Higgs, but scalar
- ❖ DM candidate
- ❖ No contrib. to EWSB

Septet w/ $Y=2$
 26-plet w/ $Y=15/2$
 97-plet w/ $Y=-28$
 362-plet w/ $Y=-209/2$
 1351-plet w/ $Y=-390$
 ...

- ❖ (Main) contrib. to EWSB
- ❖ Yukawa int.
- ❖ (SUSY extension)

❖ higher rep. ($d \geq 3$) cannot give large contributions to EWSB

Triplet, Quadruplet, ...

See next presentation by Dr. Yagyu

- ❖ No direct interaction w/ SM fermions

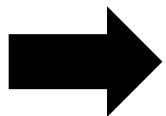
Guideline for Ext. Higgs sector

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- ❖ (SUSY extension)



**2HDM can give viable description
of the low energy effective theory**

2HDM (two-Higgs-doublet model)

- 2HDM is an effective theory

$$\Phi_1 = \begin{pmatrix} \omega_1^+ \\ \frac{v_1 + h_1 + i z_1}{\sqrt{2}} \end{pmatrix} \quad \Phi_2 = \begin{pmatrix} \omega_2^+ \\ \frac{v_2 + h_2 + i z_2}{\sqrt{2}} \end{pmatrix}$$

- Softly Z_2 broken 2HDM

$$V_{2\text{HDM}} = m_1^2 \Phi_1^\dagger \Phi_1 + m_2^2 \Phi_2^\dagger \Phi_2 - \left(m_3^2 \Phi_1^\dagger \Phi_2 + \text{H.c.} \right) + \frac{\lambda_1}{2} (\Phi_1^\dagger \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^\dagger \Phi_2)^2 \\ + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) + \left[\frac{\lambda_5}{2} (\Phi_1^\dagger \Phi_2)^2 + \text{H.c.} \right]$$

- 5 Physical Higgs bosons (assume CP inv.)

m_3^2, λ_5 real

$$\begin{pmatrix} h_1 \\ h_2 \end{pmatrix} = R(\alpha) \begin{pmatrix} H \\ h \end{pmatrix}, \quad \begin{pmatrix} z_1 \\ z_2 \end{pmatrix} = R(\beta) \begin{pmatrix} z \\ A \end{pmatrix}, \quad \begin{pmatrix} \omega_1^+ \\ \omega_2^+ \end{pmatrix} = R(\beta) \begin{pmatrix} \omega^+ \\ H^+ \end{pmatrix}, \quad R(\theta) = \begin{pmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{pmatrix}$$

2HDM

□ Mass spectrum (in the nearly SM-like limit)

$$m_h^2 \sim 2\lambda v^2 \sim 125 \text{ GeV}$$

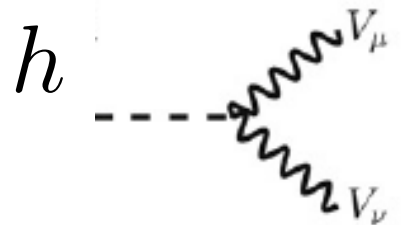
$$M^2 \equiv m_3^2 / (\sin \beta \cos \beta)$$

M^2 characterizes non-decoupling effects

(Only important for scalar interactions,
eg., hH^+H^- coupling in $h \rightarrow \gamma\gamma$)

$$m_{H,A,H^\pm}^2 \sim M^2 + \frac{\lambda v^2}{2} \sim \text{Not yet observed}$$

□ gauge-gauge-Higgs coupling: $\sin(\beta - \alpha)$

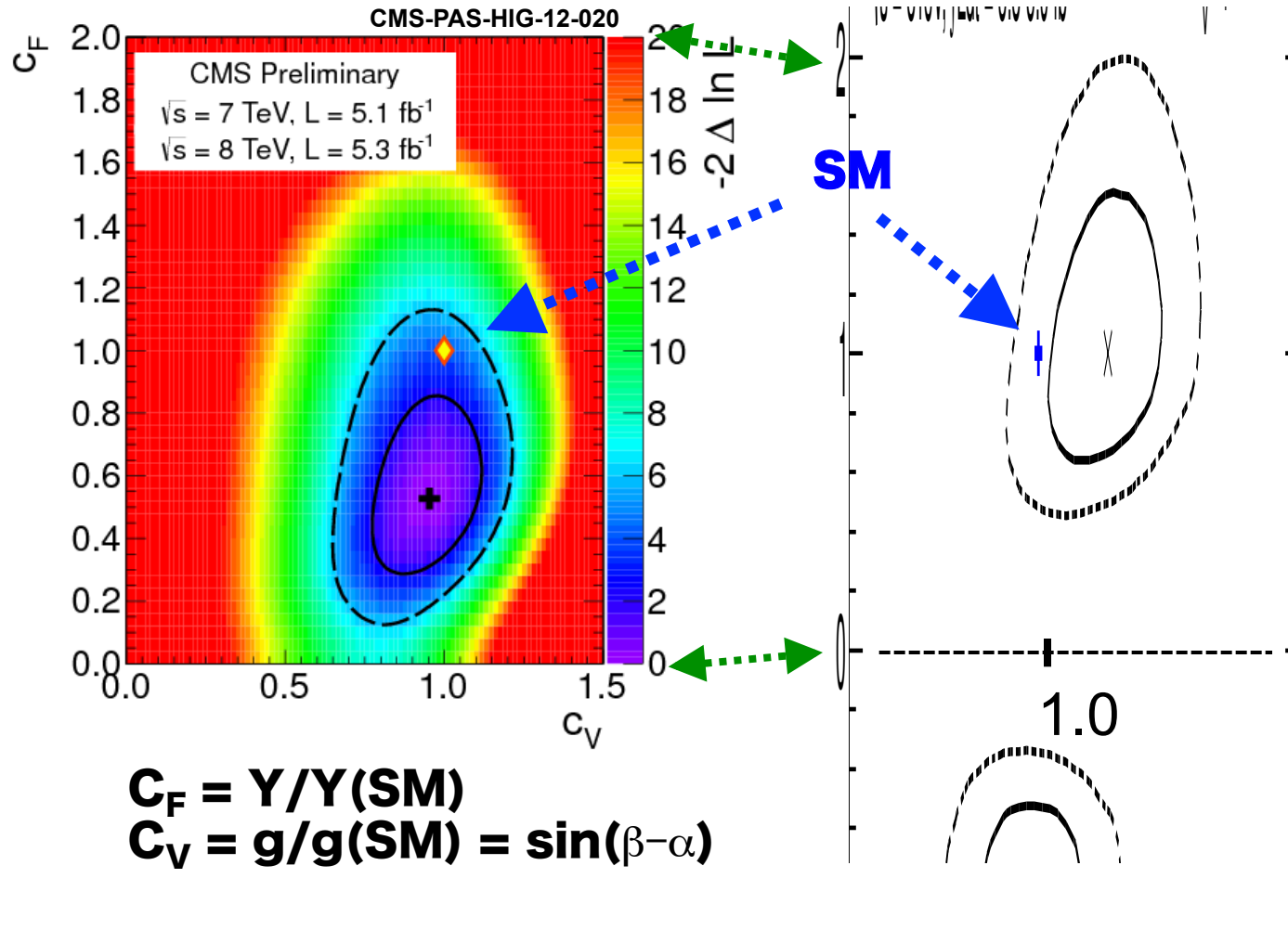


$$i g_V M_V \sin(\beta - \alpha) g_{\mu\nu}$$

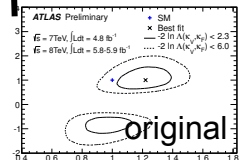
□ $\tan\beta$ ($=v_2/v_1$) is a free parameter

Is it SM-like?

□ 125 GeV boson

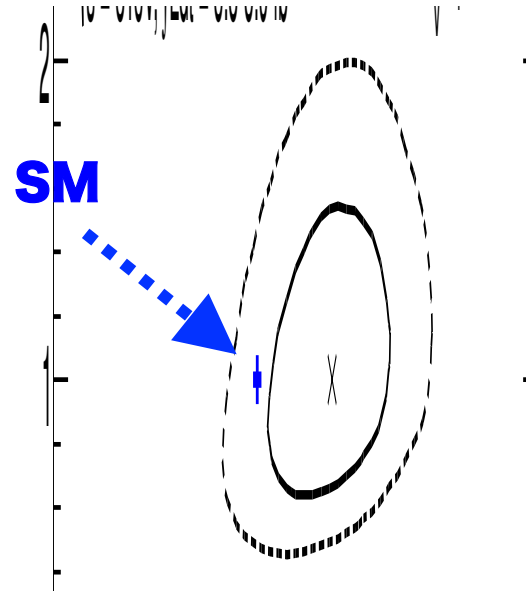
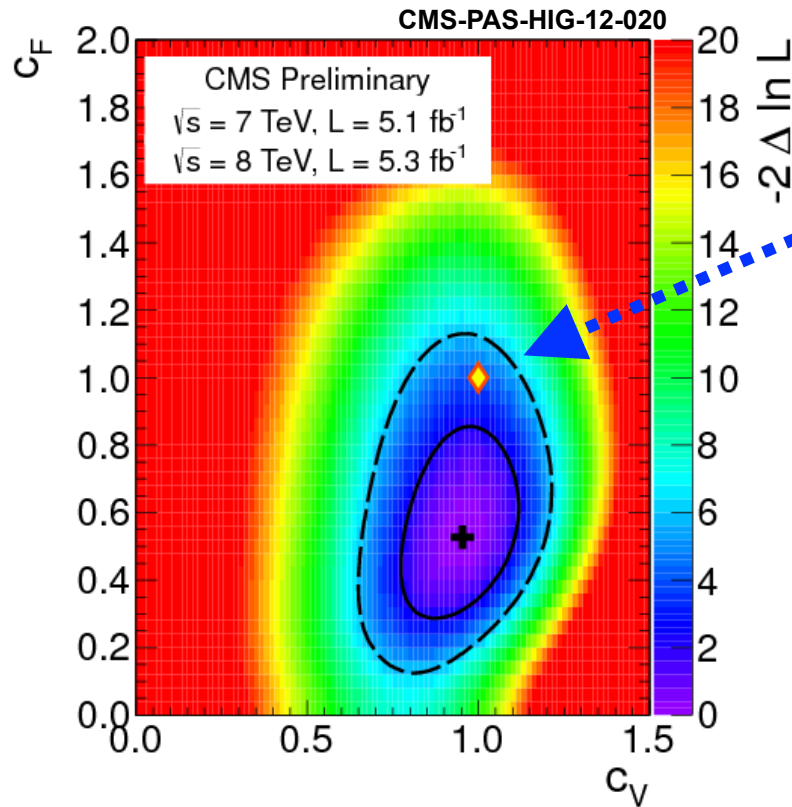


ATLAS-CONF-2012-127



Is it SM-like?

□ 125 GeV boson



CMS: $C_F < 1, C_V \sim 1$

ATLAS: $C_F \sim 1, C_V > 1$

$C_V = \sin(\beta - \alpha)$ in 2HDM

$\sin(\beta - \alpha)$ can be different from unity

SUSY Higgs search

- SUSY Higgs sector is the most popular 2HDM

- Type-II Yukawa interaction w/ SUSY relation $\sin(\beta - \alpha) \simeq 1 - \frac{2m_Z^4}{m_A^4 \tan^2 \beta}$

$$\begin{cases} \Phi_u : u, \\ \Phi_d : d, \ell \end{cases}$$

$$\frac{g_{htt}}{g_{htt}^{\text{SM}}} = \sin(\beta - \alpha) + \cot \beta \cos(\beta - \alpha) \simeq 1 - \frac{2m_Z^2}{m_A^2 \tan^2 \beta}$$

$$\frac{g_{hbb}}{g_{hbb}^{\text{SM}}} = \frac{g_{h\tau\tau}}{g_{h\tau\tau}^{\text{SM}}} = \sin(\beta - \alpha) - \tan \beta \cos(\beta - \alpha) \simeq 1 + \frac{2m_Z^2}{m_A^2}$$

$$\frac{g_{Htt}}{g_{htt}^{\text{SM}}} = \cos(\beta - \alpha) - \cot \beta \sin(\beta - \alpha) \simeq -\frac{1}{\tan \beta}$$

$$\frac{g_{Hbb}}{g_{hbb}^{\text{SM}}} = \frac{g_{H\tau\tau}}{g_{h\tau\tau}^{\text{SM}}} = \cos(\beta - \alpha) + \tan \beta \sin(\beta - \alpha) \simeq \tan \beta$$

$u \quad d, \ell$

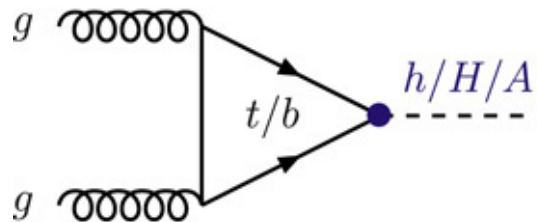
Yukawa int. for H, A, H^\pm is suppressed/enhanced for large $\tan \beta$

SUSY Higgs production @ LHC

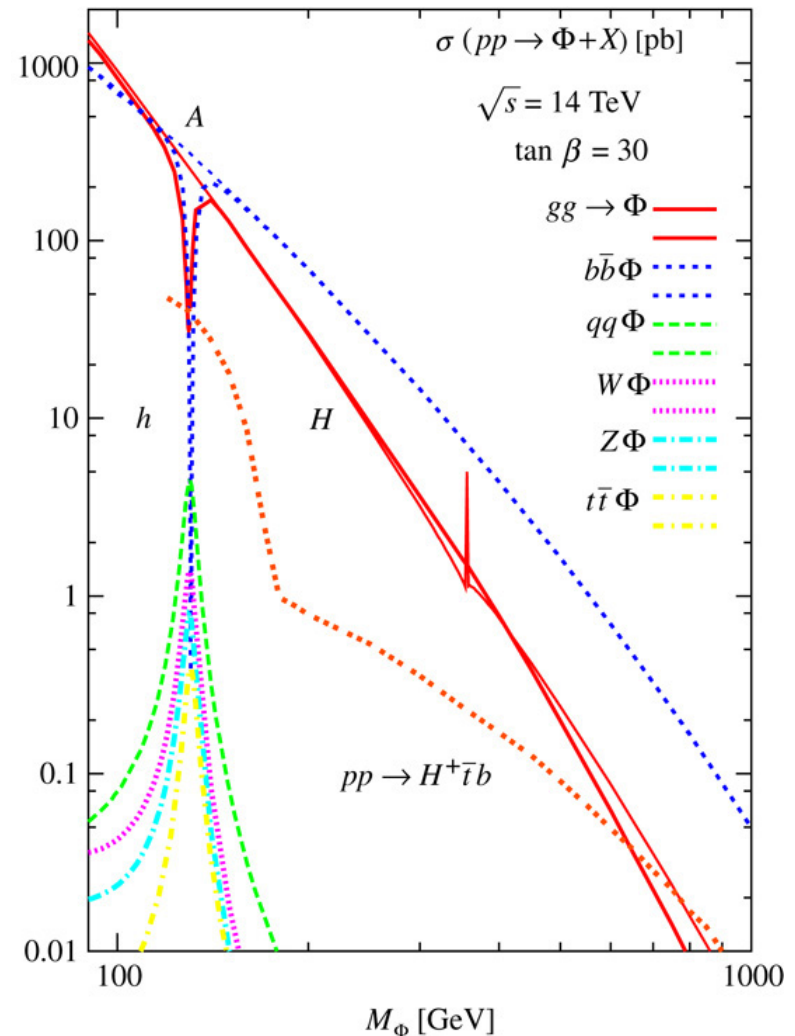
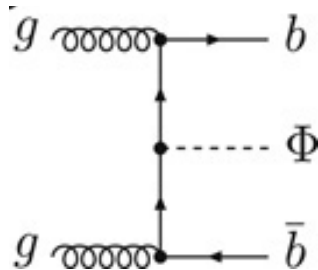
Djouadi (2008)

$$\frac{g_{Hbb}}{g_{hbb}^{\text{SM}}} = \frac{g_{H\tau\tau}}{g_{h\tau\tau}^{\text{SM}}} \simeq \tan \beta$$

❖ $gg \rightarrow h/H/A$ with $h/H/A \rightarrow \tau\tau$



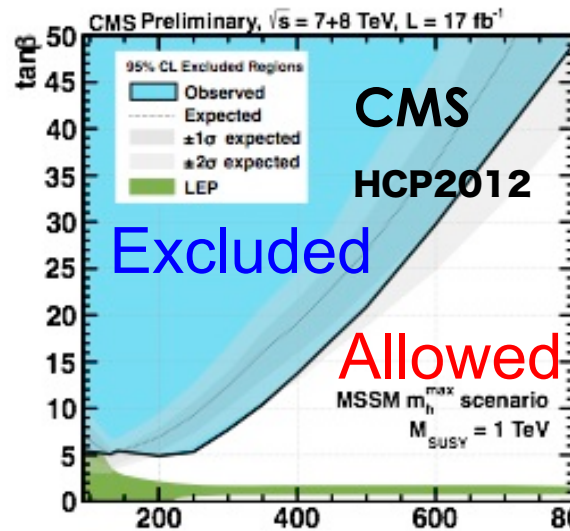
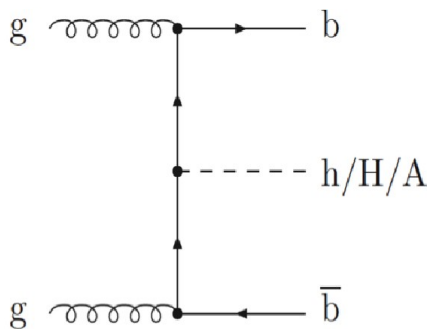
❖ $bbh/H/A$ with $h/H/A \rightarrow \tau\tau$



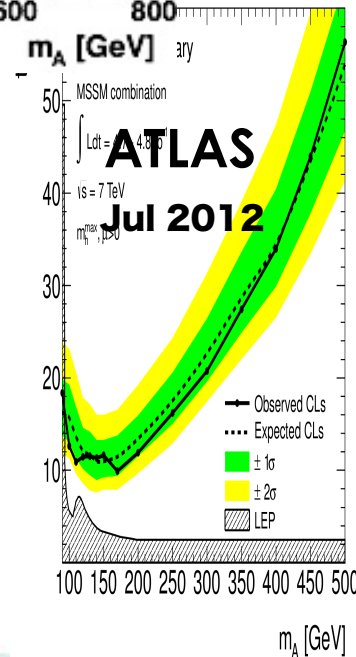
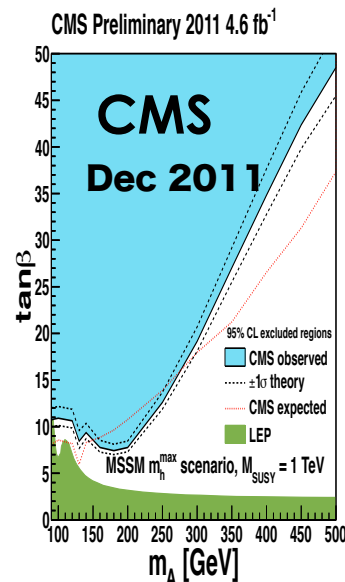
SUSY Higgs search @ LHC

□ LHC results

($H/A \rightarrow \tau\tau$)

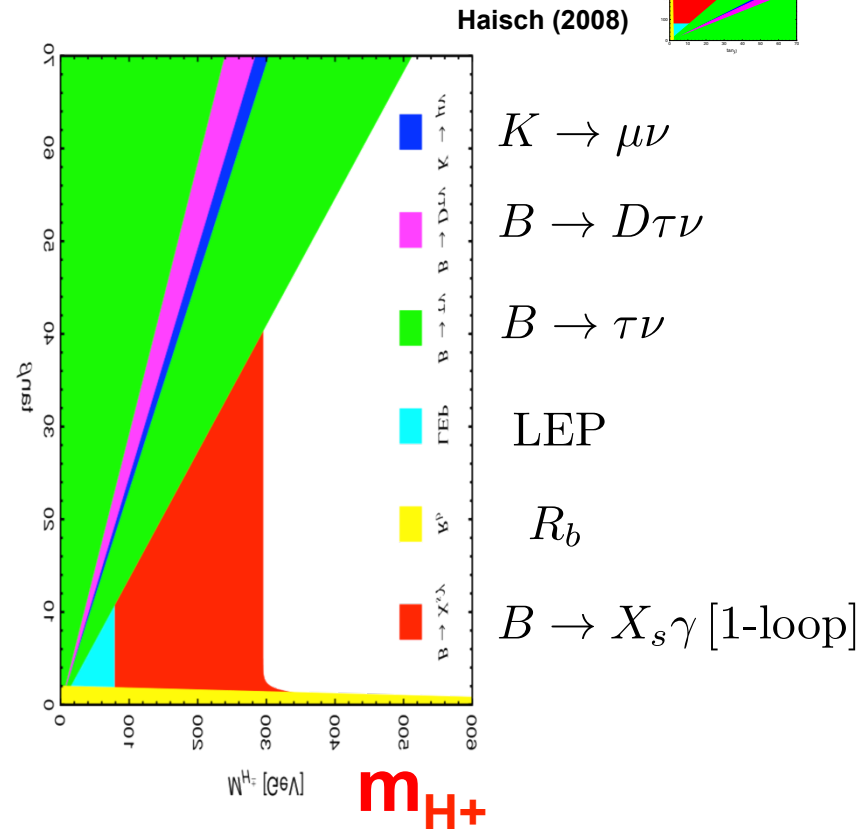
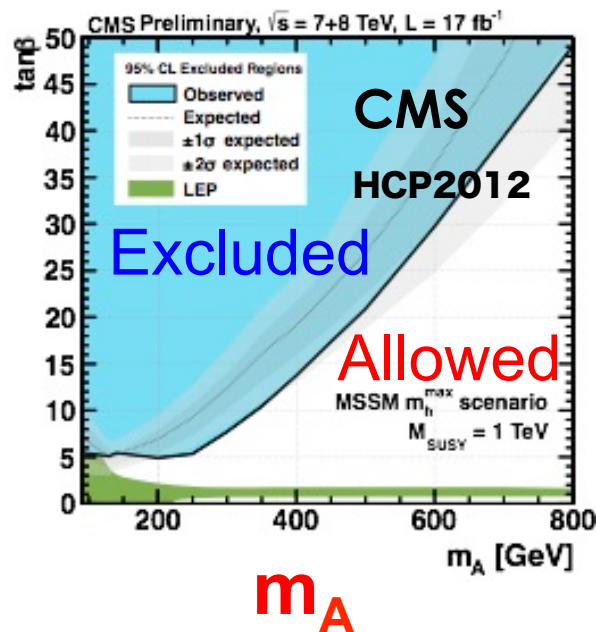


LHC is continuously excluding SUSY Higgs



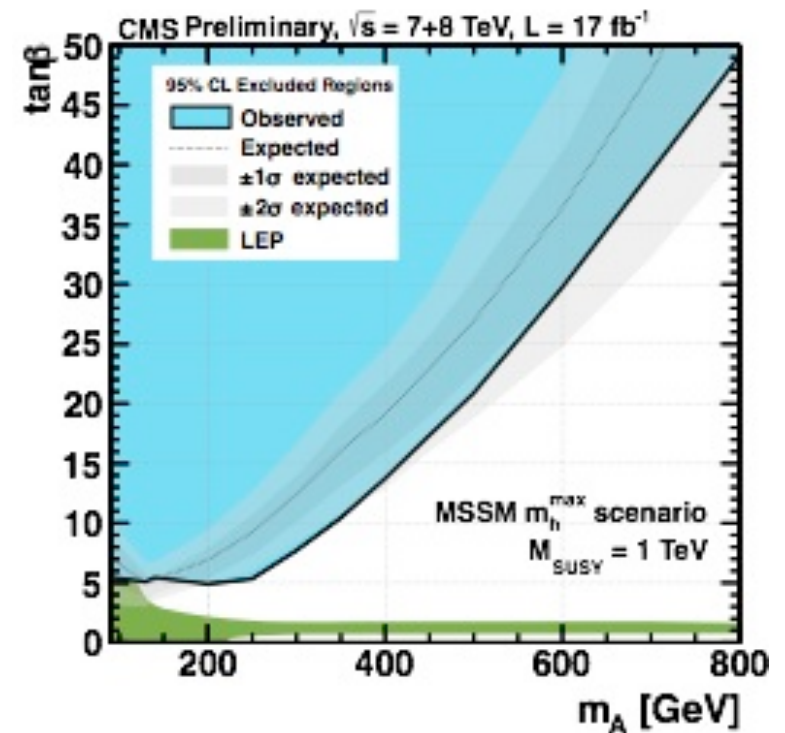
Other constraints on 2HDM-II

□ 2HDM confronts FLAVOR DATA



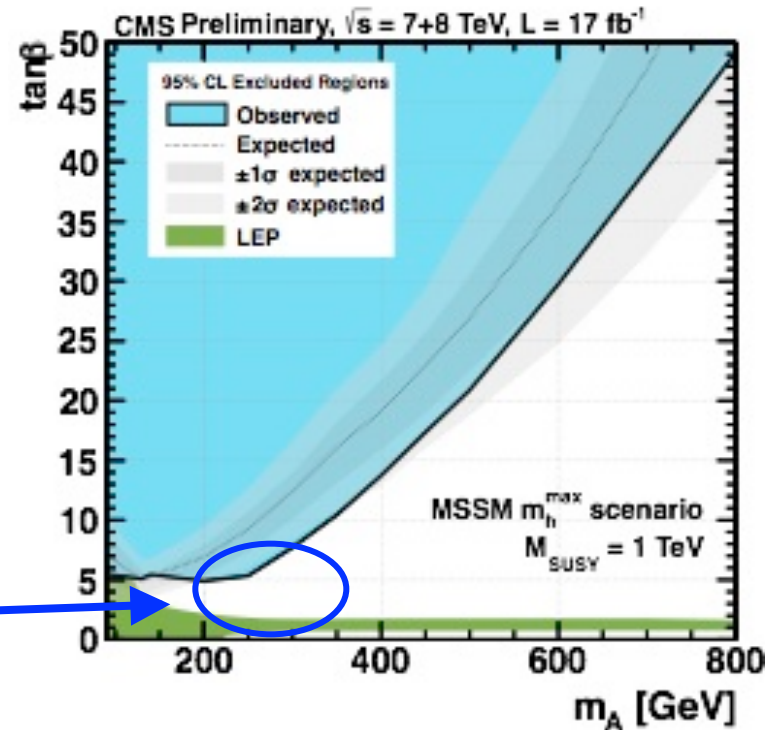
Direct search exceeds FLAVOR DATA

What's Next?

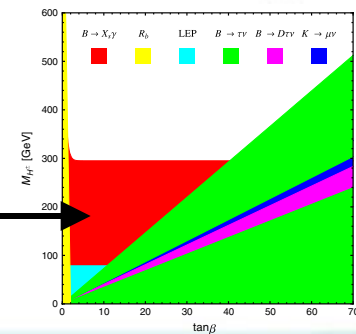


What's Next?

❖ Small m_A w/ small $\tan\beta$



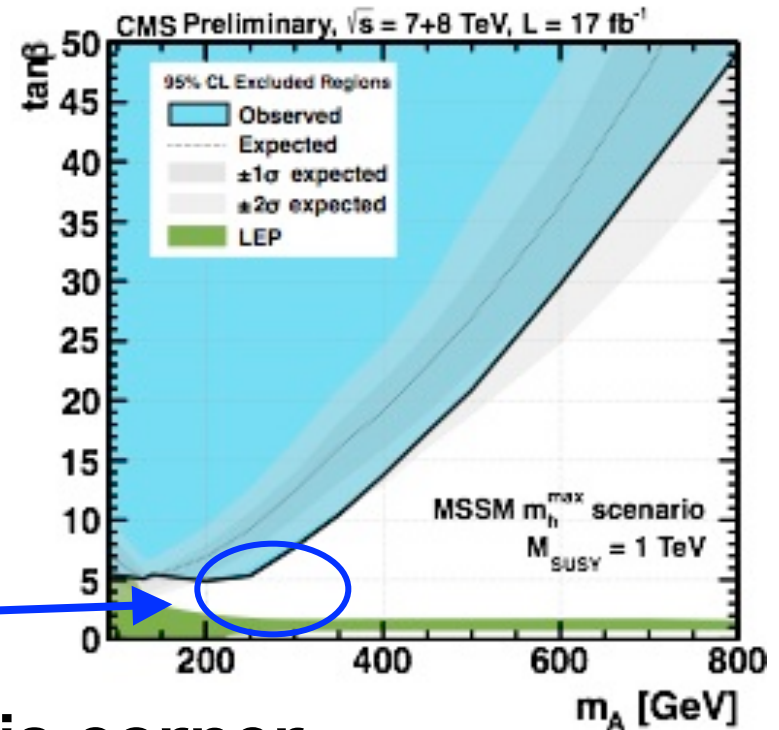
Cancellation mechanism is necessary for $B \rightarrow X_s \gamma$



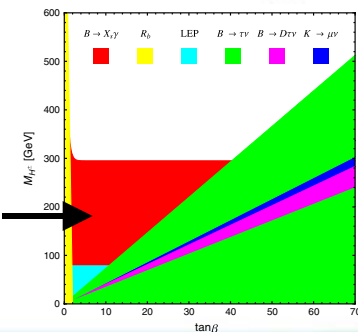
What's Next?

❖ Small m_A w/ small $\tan\beta$

LHC upgrade will answer this corner



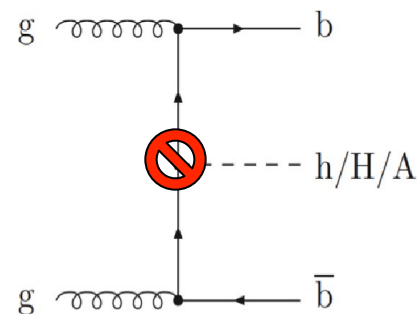
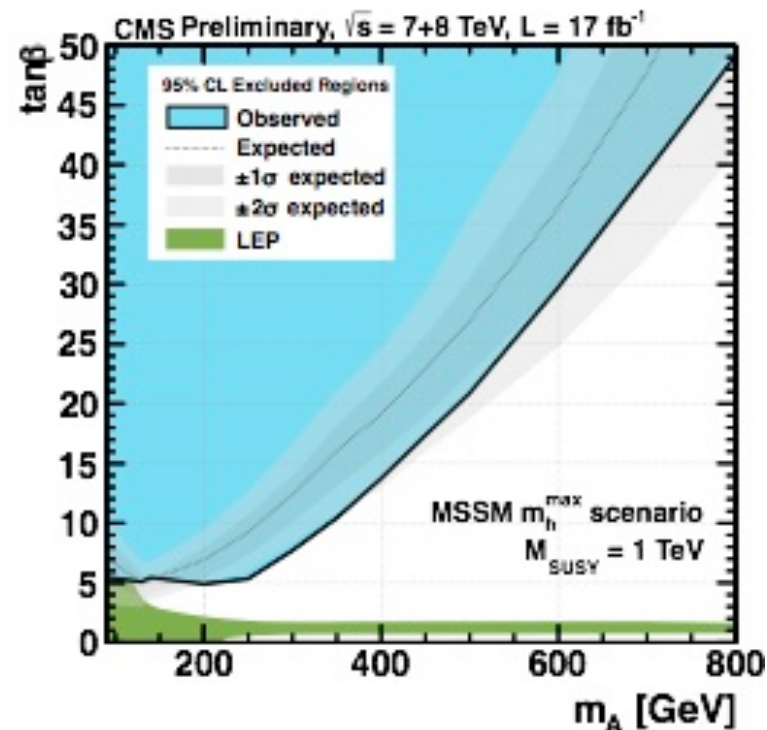
Cancellation mechanism is necessary for $B \rightarrow X_s \gamma$



What's Next?

❖ Leptophilic Higgs bosons

Beat quark interaction !!
(Less LHC & B phys. Constraints)



Leptophilic 2HDM

Recall

❖ Electroweak ρ parameter:

$$\rho = \frac{\sum_{\alpha} (I_{\alpha}(I_{\alpha} + 1) - Y_{\alpha}^2) v_{\alpha}^2}{\sum_{\beta} 2Y_{\beta}^2 v_{\beta}^2}$$

Veltman (1977)

- ❖ Precision data suggests [$\rho \sim 1$]
- ❖ SM predicts [$\rho = 1$] @ tree level

❖ FCNC (Flavor Changing Neutral Current)

- ❖ No FCNC @ tree level
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FCNC problem of 2HDM

- Flavor changing neutral current (FCNC)

$$\mathcal{L} = \bar{L} (Y_{\ell 1} \Phi_1 + Y_{\ell 2} \Phi_2) \ell_R + \text{H.c.}$$

Yukawa int. is not **simultaneously** diagonalized with mass matrix.

→ Generate tree level FCNC(, highly constrained by data)

- Adding extra Z2 sym. **to avoid FCNC**

$$\begin{array}{ll} \Phi_1 \rightarrow +\Phi_1, & L \rightarrow +L \\ \Phi_2 \rightarrow -\Phi_2, & \ell_R \rightarrow -\ell_R \end{array}$$

$$\mathcal{L} = \bar{L} (\text{X} + Y_{\ell 2} \Phi_2) \ell_R + \text{H.c.}$$

4 types of Yukawa int.

- 4 independent combinations of Z2 charges

	Φ_1	Φ_2	u_R	d_R	ℓ_R	Q, L
Type-I	+	-	-	-	-	+
Type-II	+	-	-	+	+	+
Type-X	+	-	-	-	+	+
Type-Y	+	-	-	+	-	+

- Type-II: 2HDM structure in SUSY

$$\mathcal{L} = +\bar{Q}Y_u u_R H_u + \bar{Q}Y_d d_R H_d + \bar{L}Y_\ell \ell_R H_d + \text{H.c.}$$

4 types of Yukawa int.

- 4 independent combinations of Z_2 charges

	Φ_1	Φ_2	u_R	d_R	ℓ_R	Q, L
Type-I	+	-	-	-	-	+
Type-II	+	-	-	+	+	+
Type-X	+	-	-	-	+	+
Type-Y	+	-	-	+	-	+

- Type-X: Leptophilic 2HDM for $\tan\beta > 1$

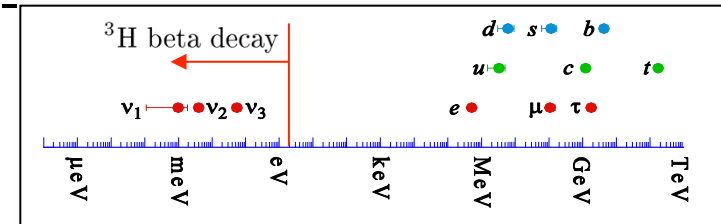
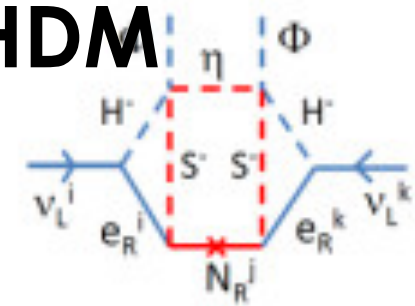
$$\mathcal{L} = +\bar{Q}Y_u u_R H_q + \bar{Q}Y_d d_R H_q + \bar{L}Y_\ell \ell_R H_\ell + \text{H.c.}$$

Higgs doublets distinguish quarks and leptons!!

Leptophilic Higgs in 2HDM

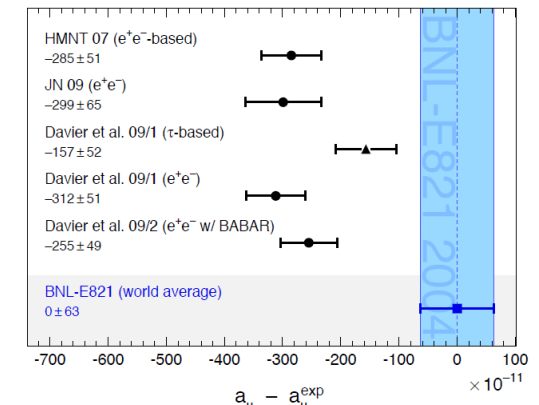
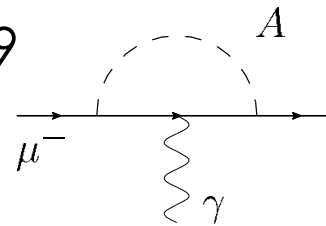
□ Tiny neutrino mass

ex. 3-loop radiative seesaw w/ light H^\pm /
by Aoki et al. PRL102:051805,2009



□ μ magnetic moment

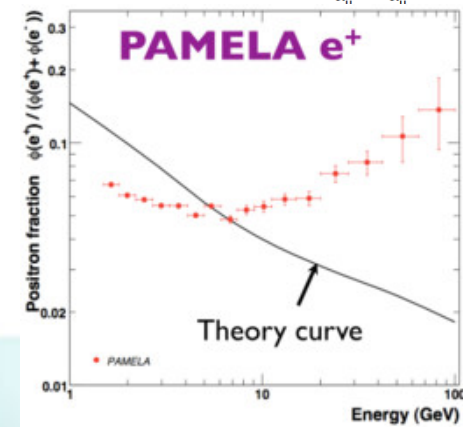
light A (CP odd) w/ large $\tan\beta$
by Cao et al. PRD80:071701,2009



□ e^+ excess @ PAMELA, FERMI

scalars as a messenger to DM
by Goh et al. JHEP 0905:097,2009

$$DM \ DM \rightarrow \Phi' \ \Phi' \rightarrow \tau\tau\tau$$

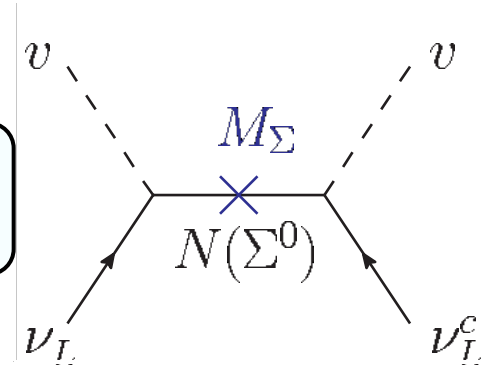


A model for tiny neutrino masses

□ Gauged Type-III seesaw

$$\mathcal{L} = +\bar{Q}Y_u u_R \tilde{H}_q + \bar{Q}Y_d d_R H_q + \bar{L}Y_\ell \ell_R H_\ell + \text{H.c.}$$

[B-L like] U(1) extension [in Type-I seesaw]



□ Anomaly cancellation requires 2HDM-X

Charge assignment:

$$(u, d)_L \sim (3, 2, 1/6; n_1), \quad u_R \sim (3, 1, 2/3; n_2), \quad d_R \sim (3, 1, -1/3; n_3),$$

$$(\nu, e)_L \sim (1, 2, -1/2; n_4), \quad e_R \sim (1, 1, -1; n_5), \quad \Sigma_R \sim (1, 3, 0; n_6).$$

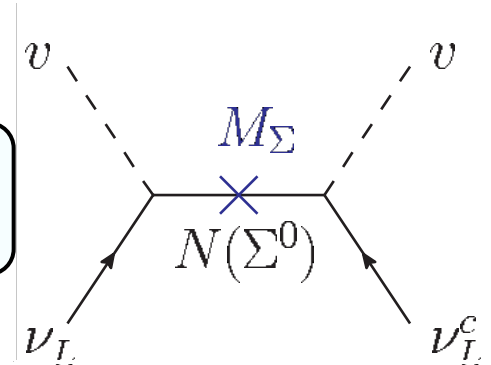
$$\text{U(1)x scalar: } \chi^0 \sim (1, 1, 0; -2n_6)$$

A model for tiny neutrino masses

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$$\mathcal{L} = +\bar{Q}Y_u u_R \tilde{H}_q + \bar{Q}Y_d d_R H_q + \bar{L}Y_\ell \ell_R H_\ell + \text{H.c.}$$

[B-L like] U(1) extension [in Type-I seesaw]



□ Anomaly cancellation requires 2HDM-X

Axial-vector anomaly:

$$[SU(3)]^2 U(1)_X : +2n_1 - n_2 - n_3 = 0$$

$$[SU(2)]^2 U(1)_X : +3\left(\frac{1}{2}\right)n_1 + \left(\frac{1}{2}\right)n_4 - (2)n_6 = 0$$

$$[U(1)_Y]^2 U(1)_X : +6\left(\frac{1}{6}\right)^2 n_1 - 3\left(\frac{2}{3}\right)^2 n_2 - 3\left(-\frac{1}{3}\right)^2 n_3 + 2\left(-\frac{1}{2}\right)^2 n_4 - (-1)^2 n_5 = 0$$

$$U(1)_Y [U(1)_X]^2 : +6\left(\frac{1}{6}\right)n_1^2 - 3\left(\frac{2}{3}\right)n_2^2 - 3\left(-\frac{1}{3}\right)n_3^2 + 2\left(-\frac{1}{2}\right)n_4^2 - (-1)n_5^2 = 0$$

$$[U(1)_X]^3 : +6n_1^3 - 3n_2^3 - 3n_3^3 + 2n_4^3 - n_5^3 - 3n_6^3 = 0$$

gravitational anomaly:

$$+6n_1 - 3n_2 - 3n_3 + 2n_4 - n_5 - 3n_6 = 0$$

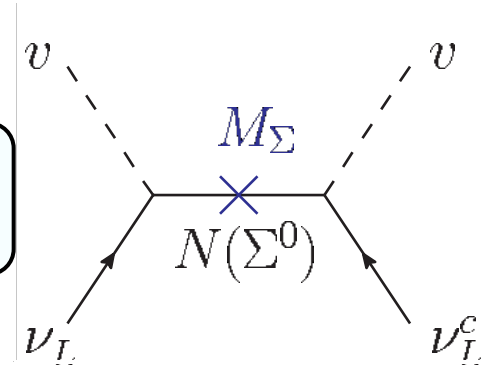
Unique solution exists!!

A model for tiny neutrino masses

□ Gauged Type-III seesaw

$$\mathcal{L} = +\bar{Q}Y_u u_R \tilde{H}_q + \bar{Q}Y_d d_R H_q + \bar{L}Y_\ell \ell_R H_\ell + \text{H.c.}$$

[B-L like] U(1) extension [in Type-I seesaw]



□ Anomaly cancellation requires 2HDM-X

possible Yukawa int:

$$n_1 - n_3 = n_2 - n_1 = n_6 - n_4 = \frac{3}{4}(n_1 - n_4), \quad n_4 - n_5 = \frac{1}{4}(9n_1 - n_4),$$

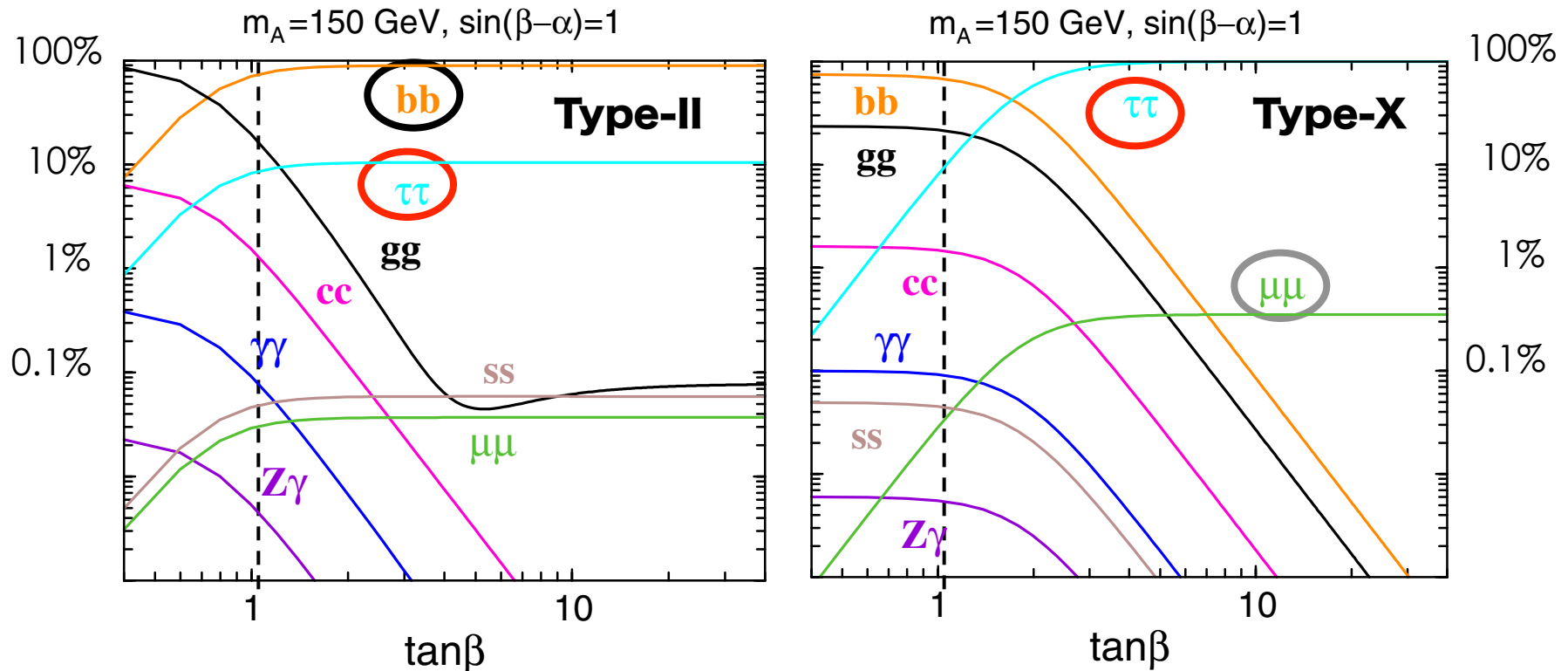
H_q

H_ℓ

2HDM-X can also be a low energy effective theory

Higgs decays in 2HDMs

Aoki, Kanemura, KT, Yagyu (2009)



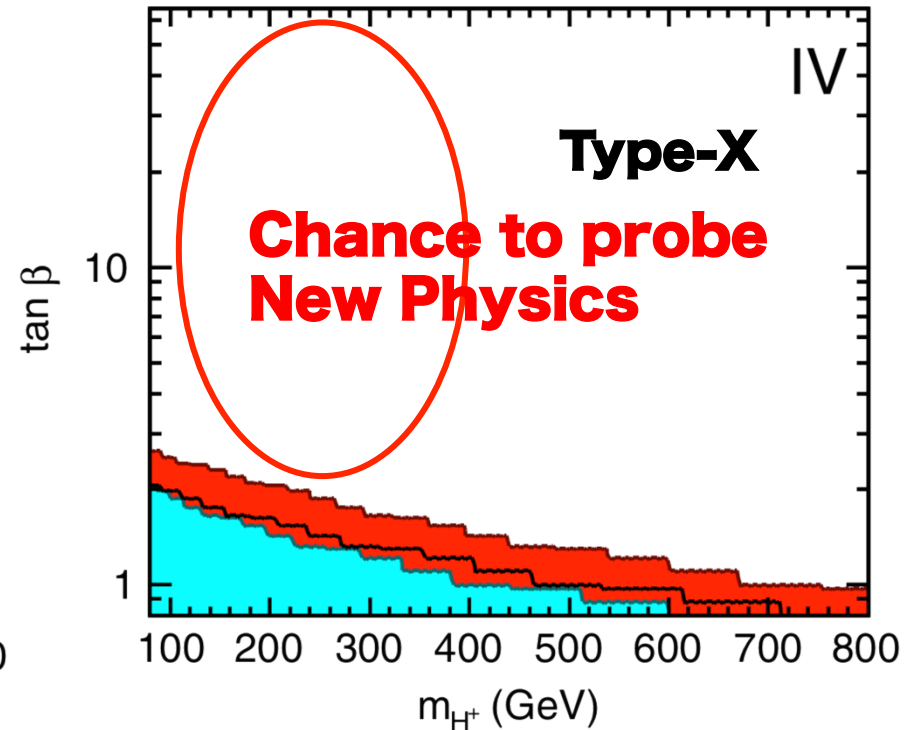
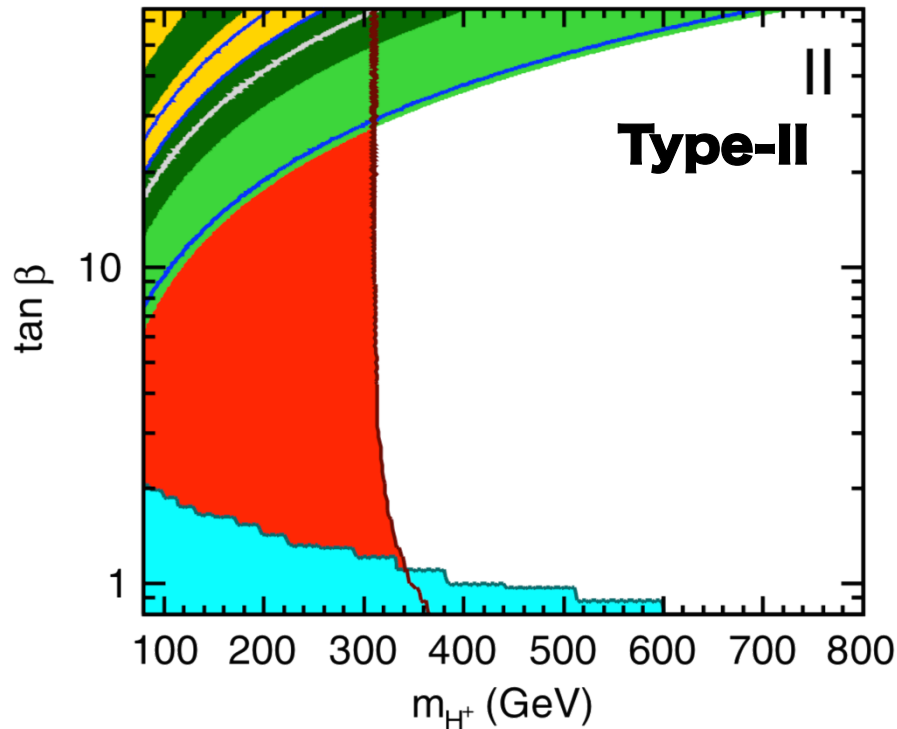
2HDM-X : Enhance leptonic Yukawa int. by $\tan\beta$

- ❖ More than 99% of H/A decay into $\tau\tau$
- ❖ Sizable $\mu\mu$ [$(m_\mu/m_\tau)^2 = 1/300$] mode

Flavor constraint on 2HDM-X

- No LHC results, and weaker flavor constraints

Mahmoudi, Stal (2009)

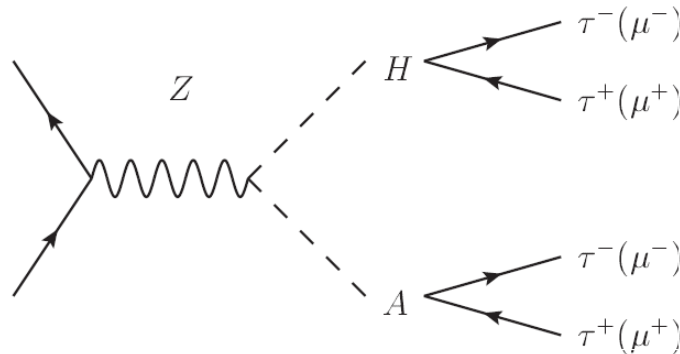


small m_{H^+} and
very large $\tan \beta$ are allowed

2HDM-X @ colliders

Kanemura, KT, Yokoya (2012)

- DY production with leptonic decay modes

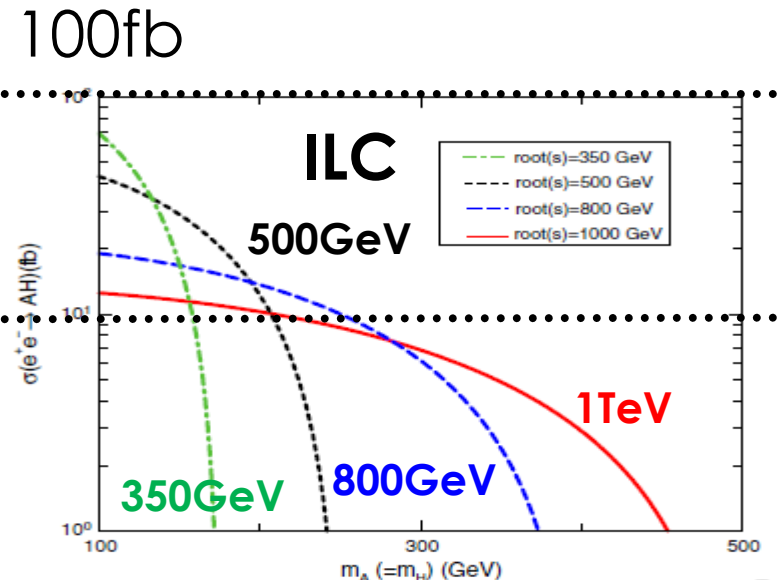
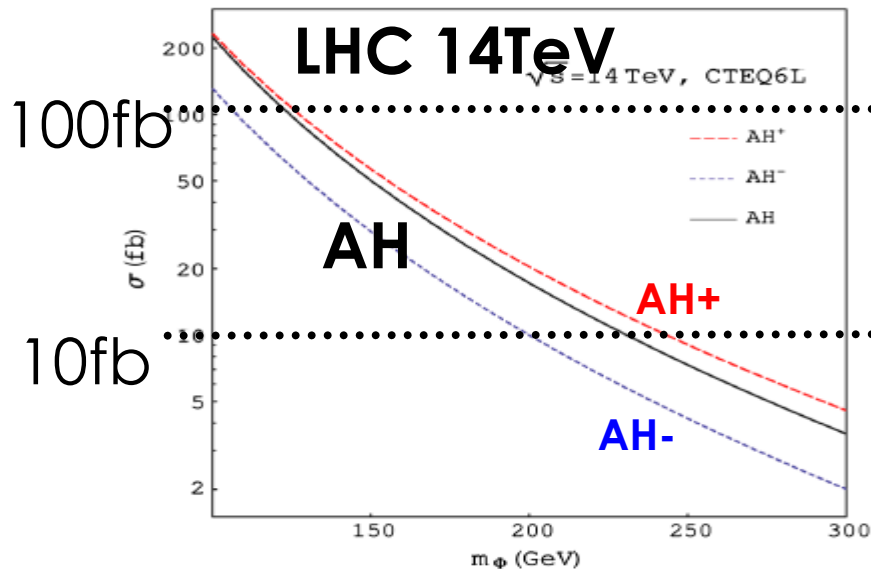


Multi-tau signature

4 τ : more than 99%

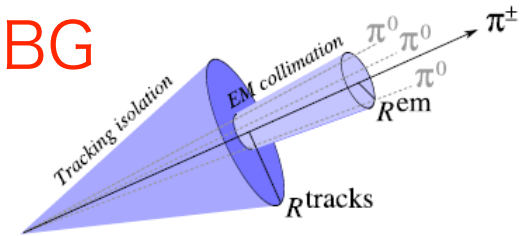
2 μ 2 τ : $\sigma(4\tau) \times 1/300 \times 2!$

Cross sections are O(10-100)fb



High multiplicity of tau jet reduces BG

τ ID is important (1 or 3 prong, narrow cone, less QCD activity)



$4\tau_h$ event analysis	HA	$\phi^0 H^\pm$	VV	$t\bar{t}$	$V+\text{jets}$	s/b	S (100 fb $^{-1}$)
Pre-selection	324.	52.8	147.	797.	5105.	0.1	4.7
$p_T^{\tau h} > 40$ GeV	67.2	4.9	2.0	14.7	21.7	1.9	9.4
$E_T^{\tau h} > 30$ GeV	48.6	4.4	1.1	7.6	10.4	2.8	9.3
$H_T^{\text{jet}} < 50$ GeV	34.2	3.4	0.5	0.8	8.2	3.9	8.7
$H_T^{\text{lep}} > 350$ GeV	27.6	2.7	0.4	0.5	3.1	7.5	9.3

Simulation results:

An example for $4\tau \rightarrow 4\tau_h$
 $m_A=130\text{GeV}$, $m_H=170\text{GeV}$

→ The excess can be seen!!

But, mass reconstruction is difficult due to missing ν 's

→ " $HA \rightarrow 2\mu 2\tau$ " is reconstructable (w/ collinear approx.)

Huge lumi. is necessary due to $\mathcal{B}^{\mu\mu} / \mathcal{B}^{\tau\tau} \times 2! \simeq 0.7\%$

- 4 τ momentum are fully reconstructable from taujets & missing ν 's [We know initial 4 momenta @ LC (only p_T @ LHC)]

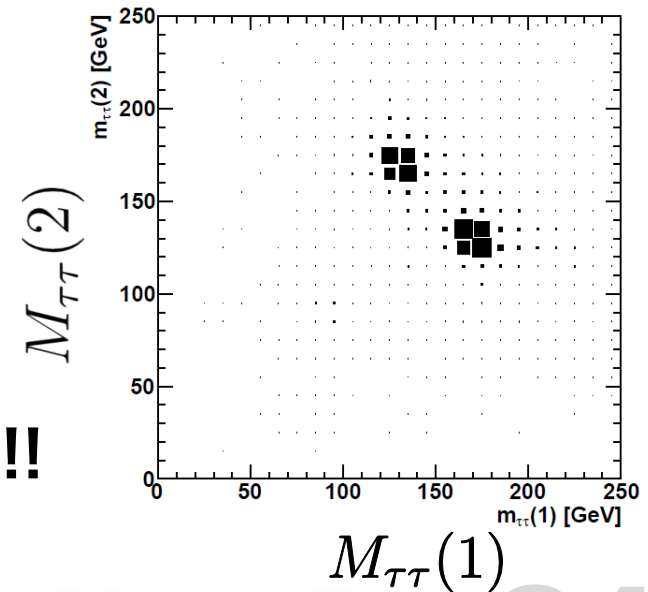
4 τ_h event analysis	HA	VV	$t\bar{t}$	S (100 fb $^{-1}$)
Pre-selection	300.	10.6	1.2	38.
$0 \leq z_{1-4} \leq 1$	251.	6.2	0.1	38.
$(m_Z)_{\tau\tau} \pm 20$ GeV	238.	1.8	0.	43.

Simulation result:

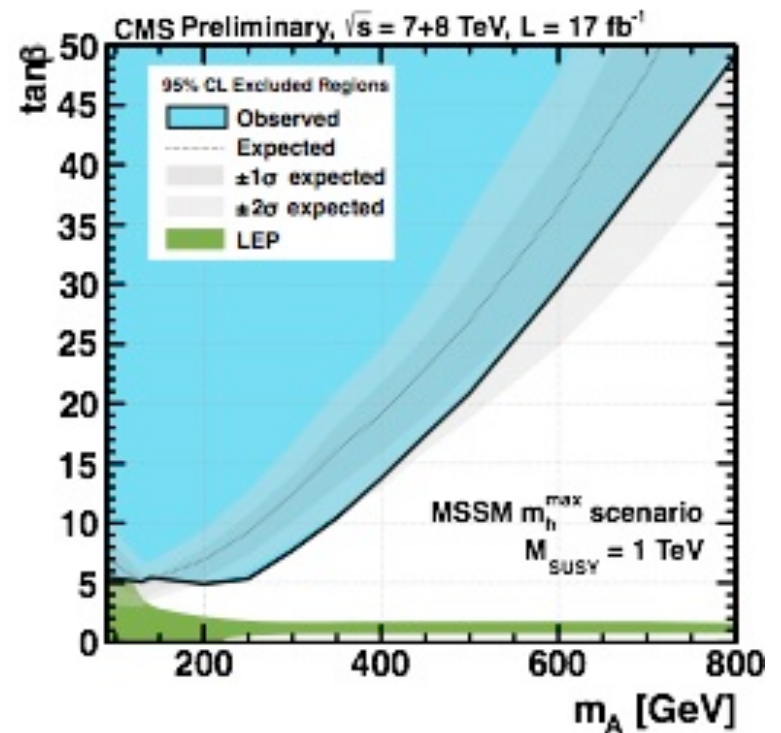
An example for $4\tau \rightarrow 4\tau_h$
 $m_A=130\text{GeV}$, $m_H=170\text{GeV}$

for $5\sigma \sim 2/\text{fb}$ @ LC

Not only mass reconstruction, but also
direct probe of pair production!!



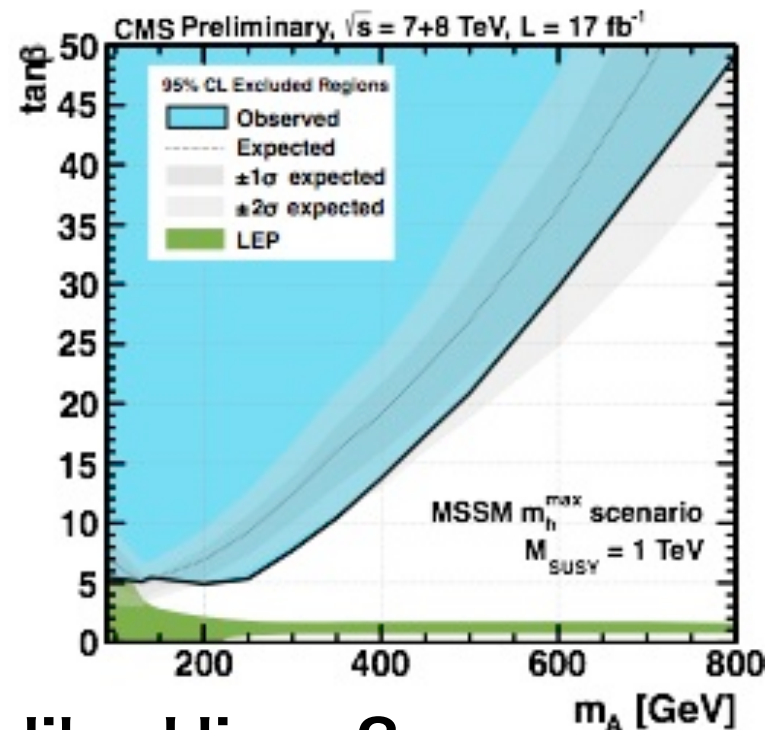
What Else?



What Else?

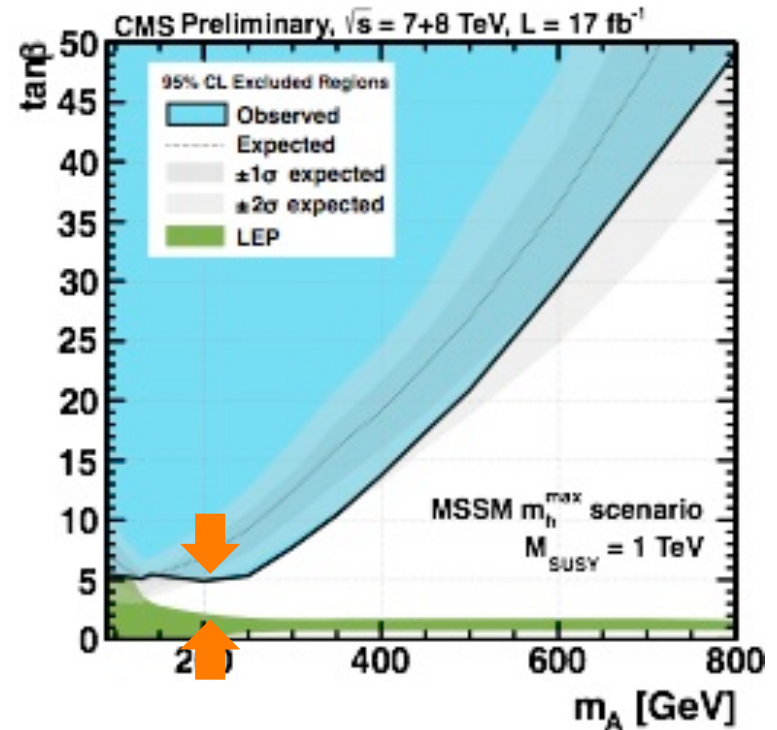
❖ Precision SM-like Higgs study

Can we probe 2HDM via SM-like Higgs?



$\tan\beta$ @ LHC

Once Extra Higgs
is discovered, then...



For example,

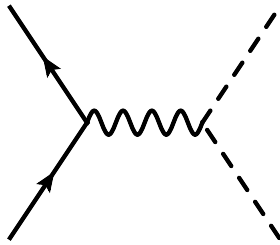
$m_A = 200 \text{ GeV} \rightarrow 3 < \tan\beta < 5$

by assuming **MSSM(2HDM-II)**

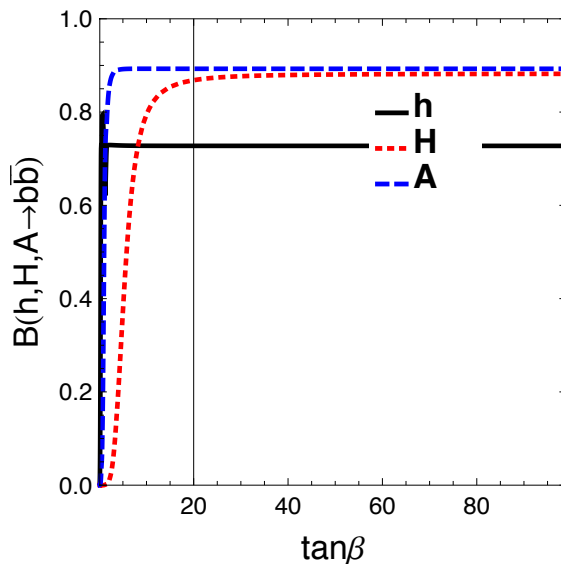
$\tan\beta$ measurement

tan β in **MSSM @ LC**

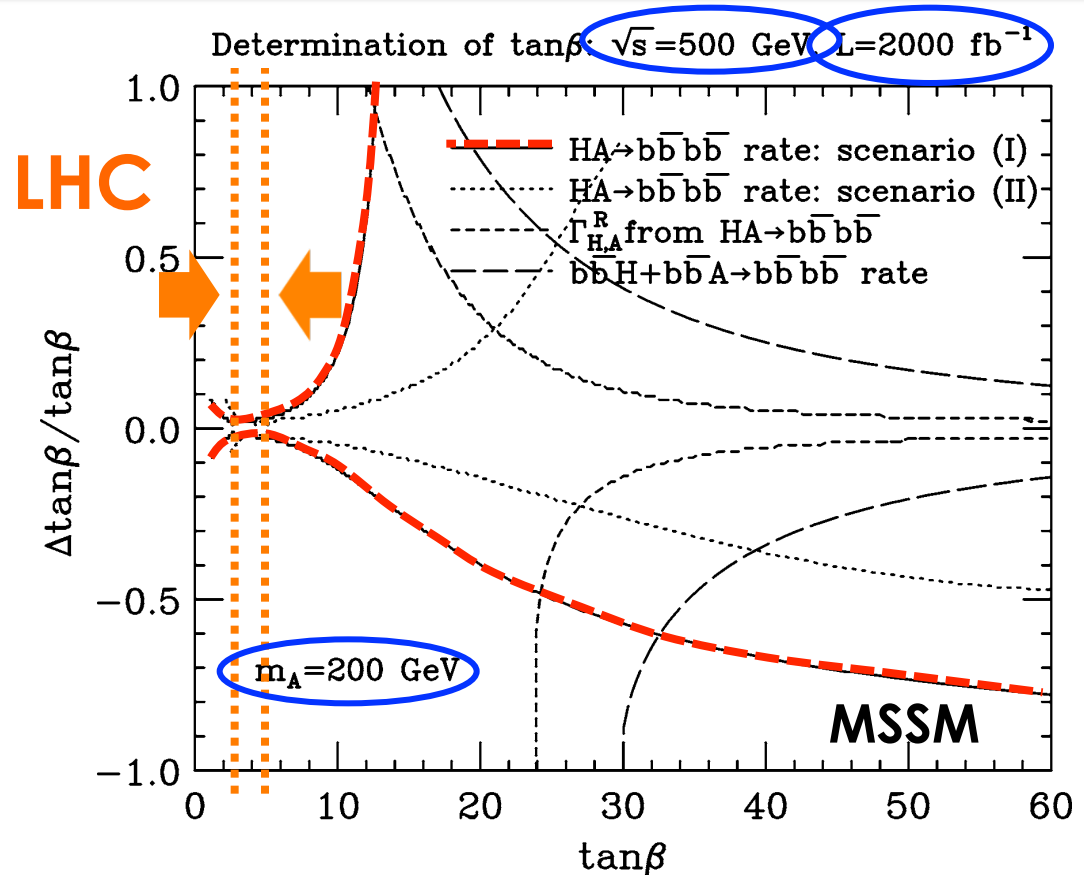
Gunion et.al. (2003)



HA production @ LC



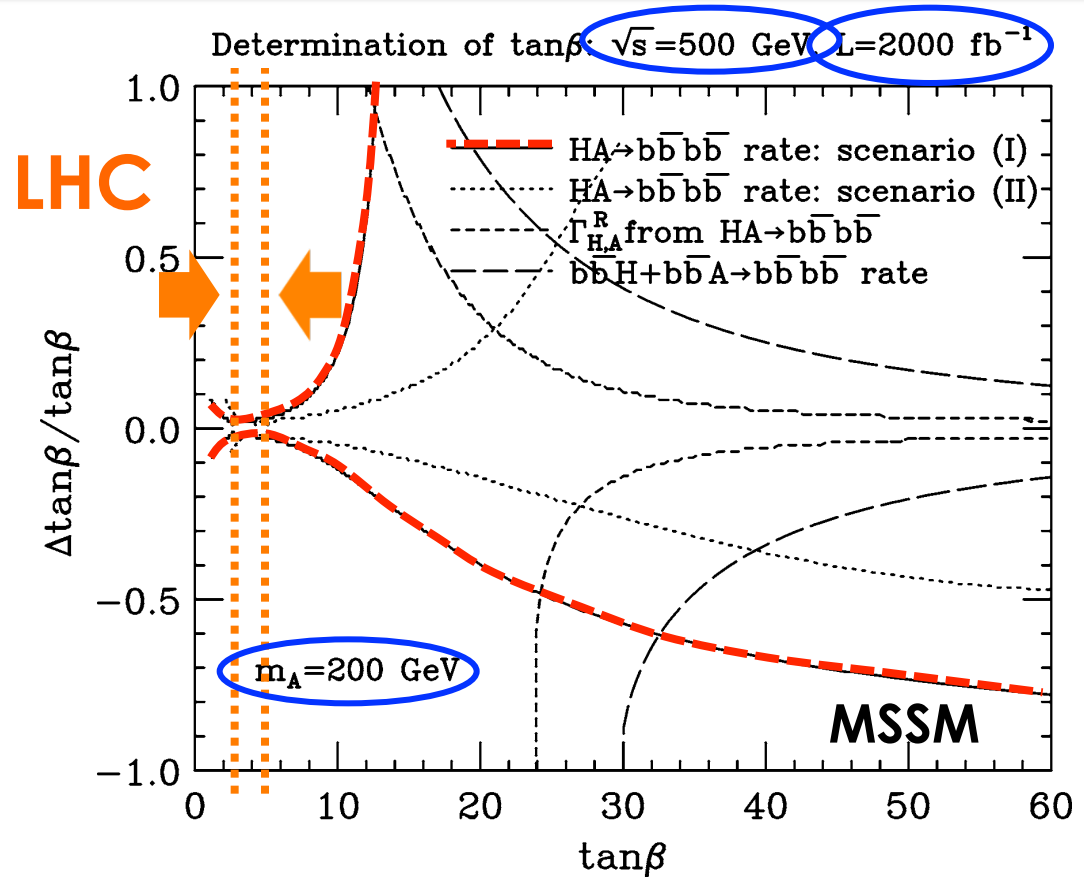
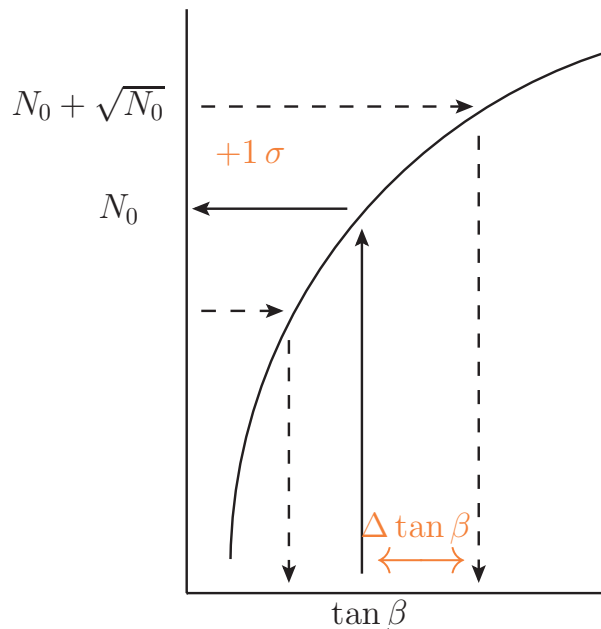
$B_{H^{bb}}$ rapidly depends on $\tan\beta$
 \rightarrow BR measurement can probe $\tan\beta$ **very precisely**



tan β in MSSM @ LC

Gunion et.al. (2003)

Definition of 1σ sensitivity



B_H^{bb} rapidly depends on tan β
 \rightarrow BR measurement can probe tan β very precisely

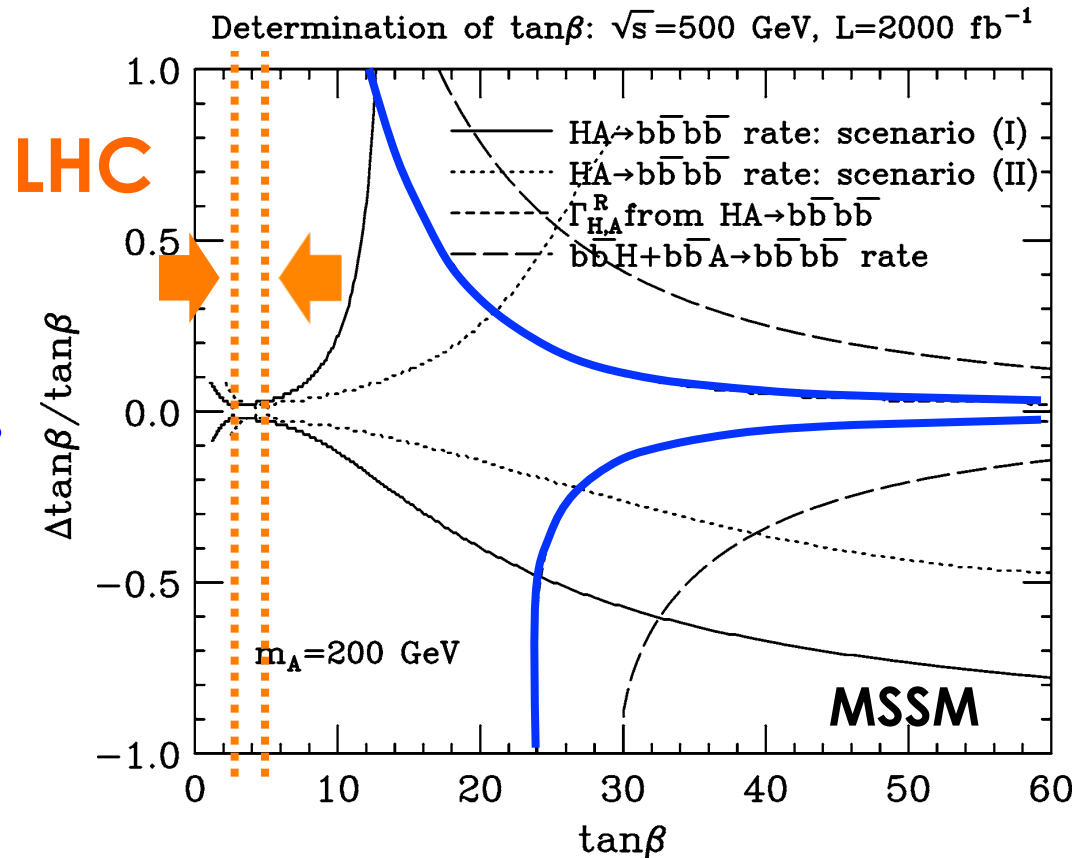
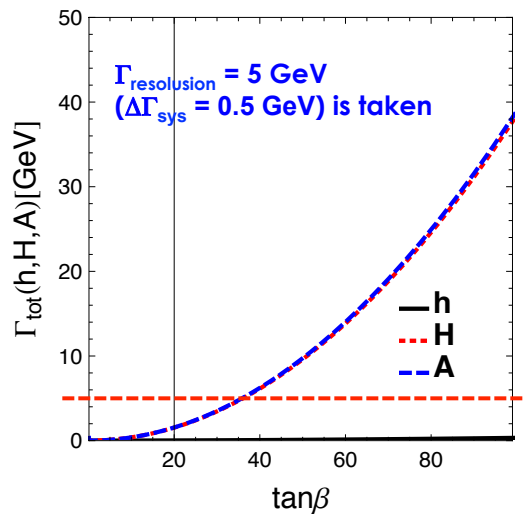
tan β @ LC

Gunion et.al. (2003)

Although, LHC already excluded

Width measurement

$$\Gamma_{\text{tot}}^{H,A} \simeq N_C \frac{G_F m_{H,A} m_b^2}{4\sqrt{2}\pi} \tan^2 \beta$$



Width measurement is sensitive for high tan β

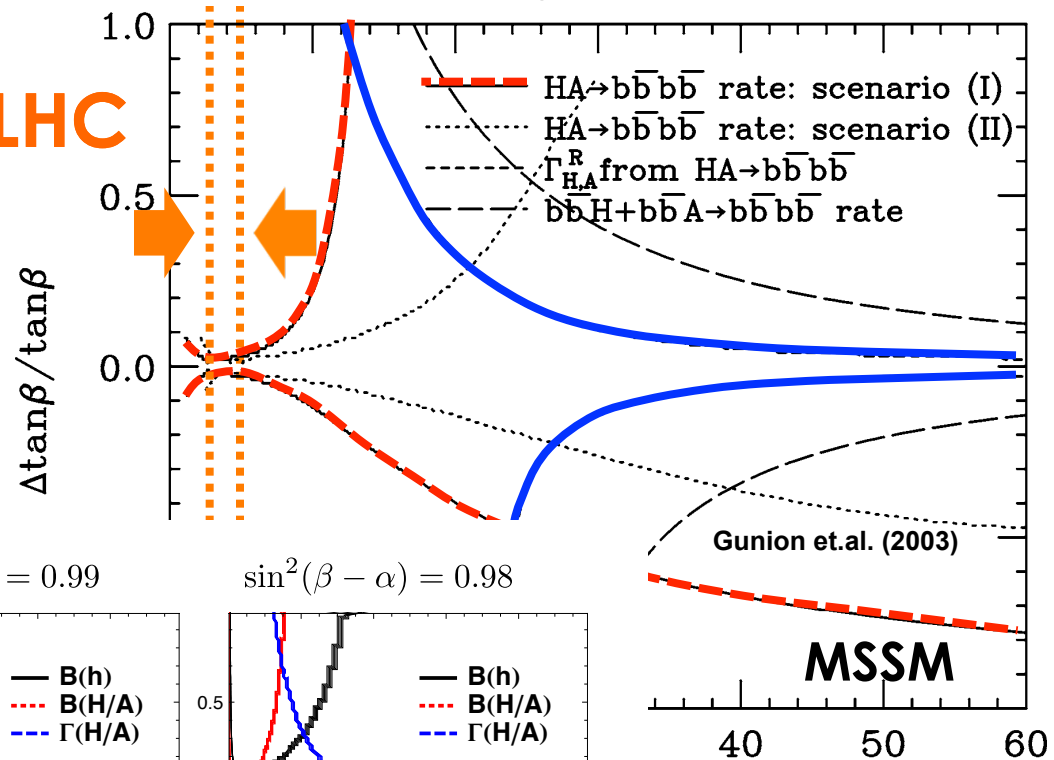
$\tan\beta$ in 2HDM-II @ LC

❖ Without SUSY relation

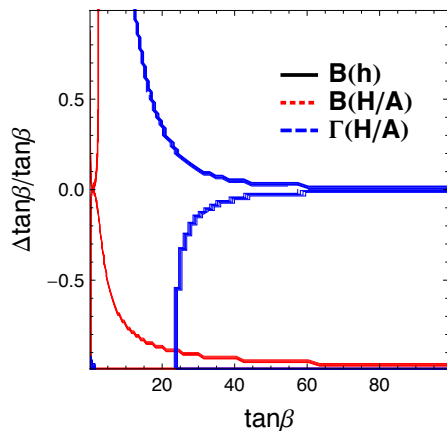
$$\sin(\beta - \alpha) \not\approx 1 - \frac{2m_Z^4}{m_A^4 \tan^2 \beta}$$

LHC

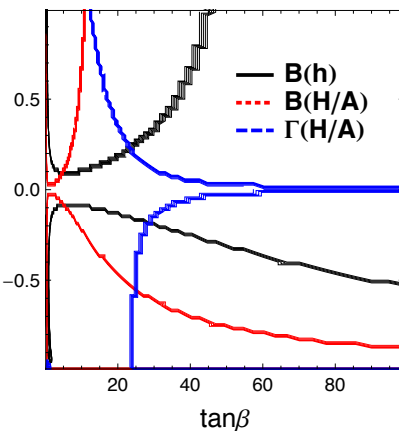
Determination of $\tan\beta$: $\sqrt{s}=500$ GeV, $L=2000$ fb $^{-1}$



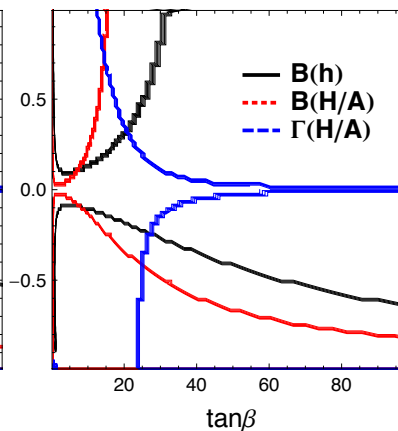
$\sin^2(\beta - \alpha) = 1$



$\sin^2(\beta - \alpha) = 0.99$



$\sin^2(\beta - \alpha) = 0.98$



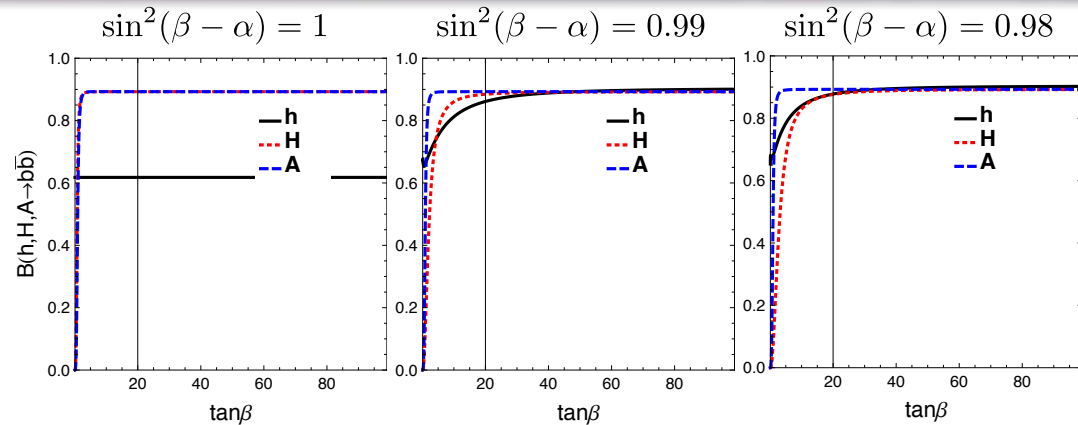
2HDM-II

Kanemura, KT, Yokoya, Yagyu

$\tan\beta$ in 2HDM-II @ LC

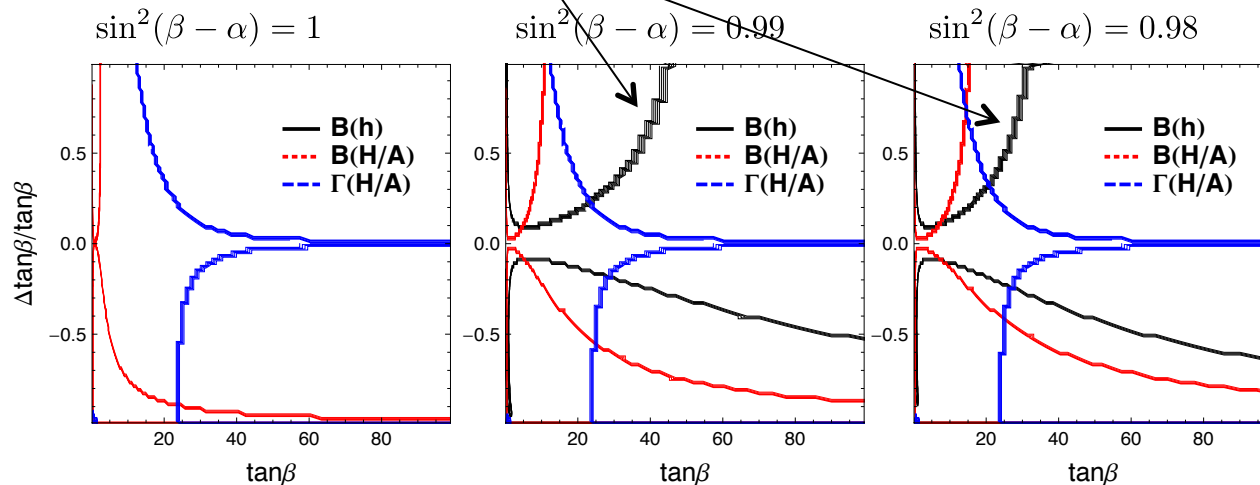
❖ Without SUSY relation

$$\sin(\beta - \alpha) \not\approx 1 - \frac{2m_Z^4}{m_A^4 \tan^2 \beta}$$



SM-like Higgs decay BRs strongly depend on $\tan\beta$

You may notice new BLACK curves



Assume $\Delta(\sigma \times \text{BR})/(\sigma \times \text{BR}) = 1\%$
[Ref: DBD, 250GeV, 250/fb]

For HA [500GeV, 2000/fb]

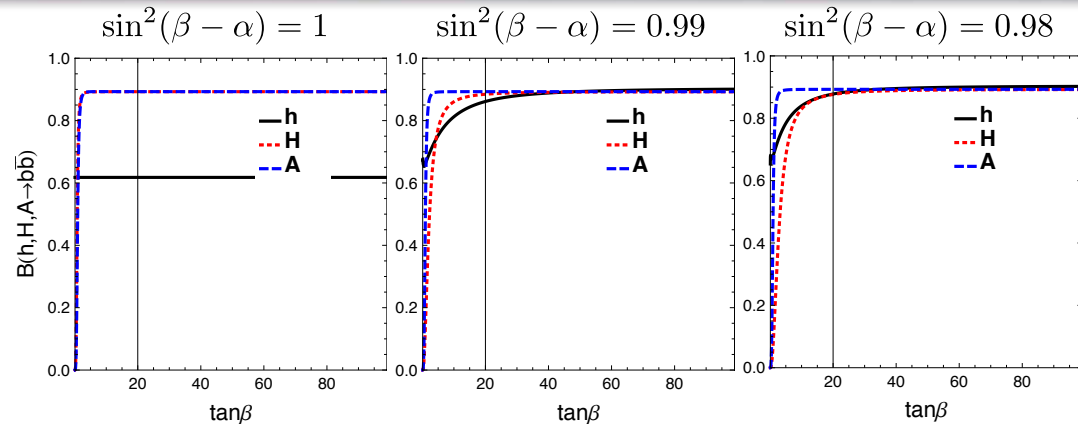
2HDM-II

Kanemura, KT, Yokoya, Yagyu

$\tan\beta$ in 2HDM-II @ LC

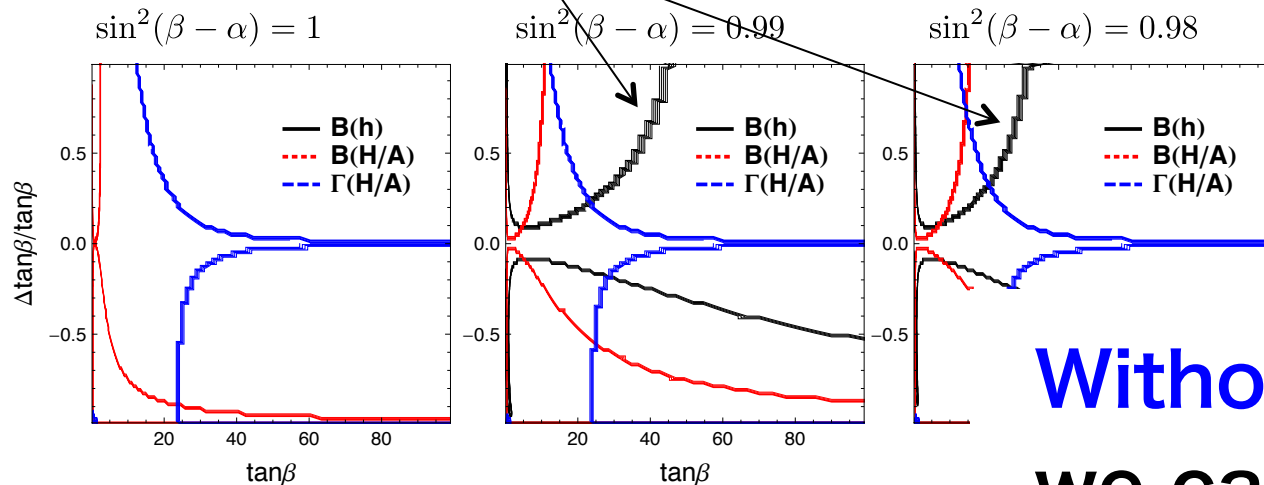
❖ Without SUSY relation

$$\sin(\beta - \alpha) \not\approx 1 - \frac{2m_Z^4}{m_A^4 \tan^2 \beta}$$



SM-like Higgs decay BRs strongly depend on $\tan\beta$

You may notice new BLACK curves



Initial stage of LC

Assume $\Delta(\sigma \times \text{BR})/(\sigma \times \text{BR}) = 1\%$
[Ref: DBD, 250GeV, 250/fb]

For HA [500GeV, 2000/fb]

Without H/A,
we can probe $\tan\beta$

2HDM-II

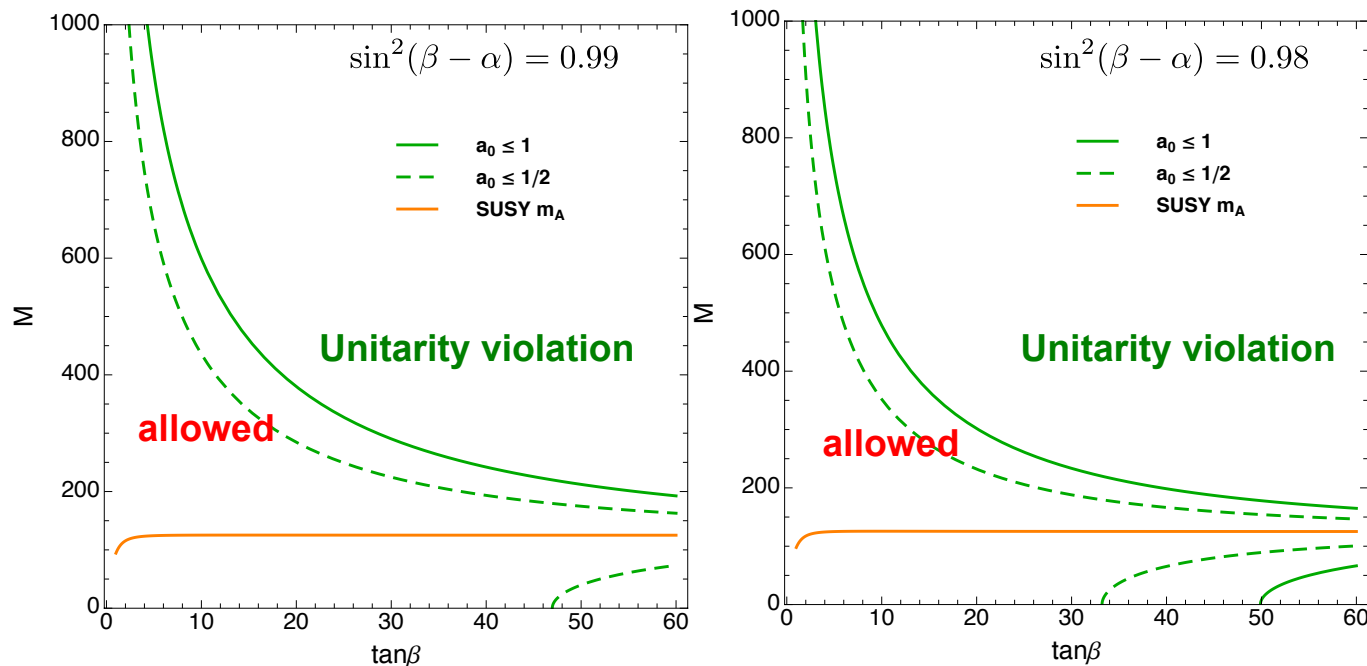
Kanemura, KT, Yokoya, Yagyu

Unitarity bound

- Potential largest eigenvalue:

Kanemura et,al, (1993)

$$a^{\pm} = -\frac{1}{32\pi} \left[3(\lambda_1 + \lambda_2) \pm \sqrt{9(\lambda_1 - \lambda_2)^2 + 4(2\lambda_3 + \lambda_4)^2} \right]$$



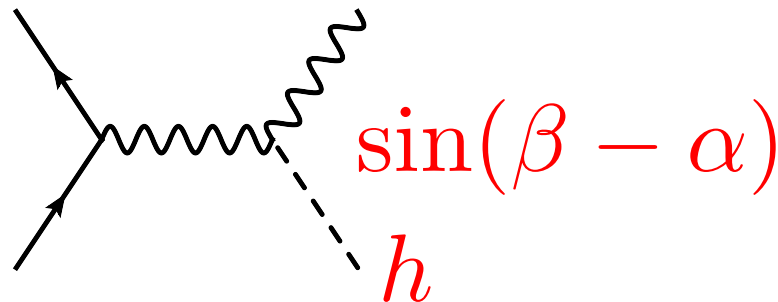
There are implicit upper mass bounds (new no lose theorem?)

[a deviation of $\sin(\beta - \alpha)$ requires large quartic coupling (non-decoupling)]

$\tan\beta$ @ LC

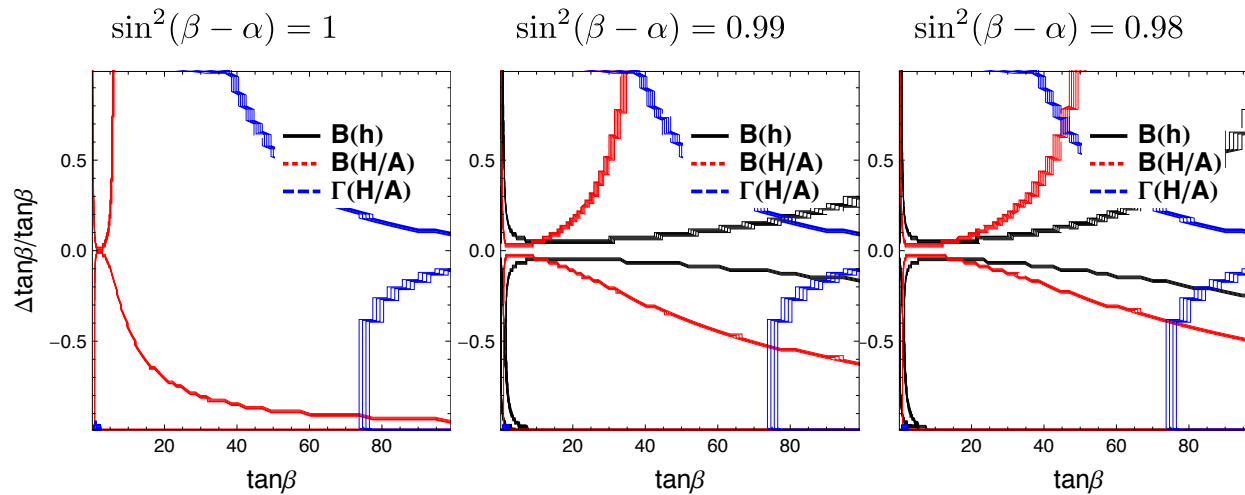
❖ Precise measurement of $\sin(\beta-\alpha)$
makes BR prediction better in 2HDMs

→ Key observable for determining $\tan\beta$

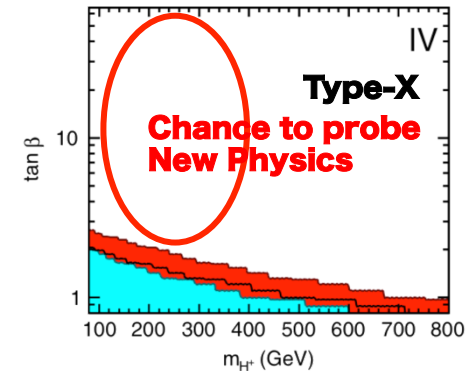


$\tan\beta$ in 2HDM-X

- SM-like Higgs decay into $\tau\tau$
- BR measurement w/ 4τ final states
- Width measurement of $H/A \rightarrow \tau\tau$



Wider parameter regions should be examined by LC



Summary

□ 2HDM can describe low energy effective theory

➤ Direct search:

❖ SUSY/2HDM-II Higgs has been searched

❖ **Leptophilic Higgs**

(4τ signature @ LHC)

(4τ signature & $\tan\beta$ @ LC)

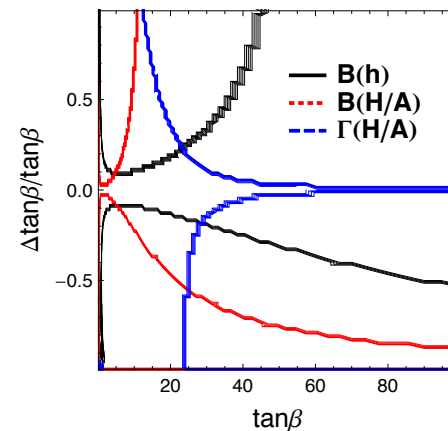
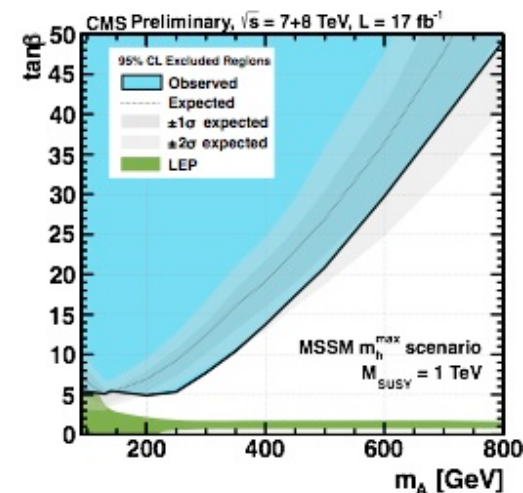
➤ $\tan\beta$ measurement:

❖ HA production, width measurement

❖ **Precision SM-like Higgs study**

($\tan\beta$ from $h \rightarrow b\bar{b}/\tau\tau$ @ LC)

(discriminate types of Yukawa in 2HDMs)



Conclusion

HPNP2013

Toyama International Workshop on
Higgs as a Probe of New Physics 2013

February 13-16, 2013, University of Toyama, Japan



Conclusion

HPNP2013

Toyama International Workshop on
Higgs as a Probe of New Physics 2013

February 13-16, 2013, **is** University of Toyama, Japan



Thank you for your attentions

Back up slides

SM-like Higgs in **SUSY**

□ SUSY Higgs sector is the most popular 2HDM

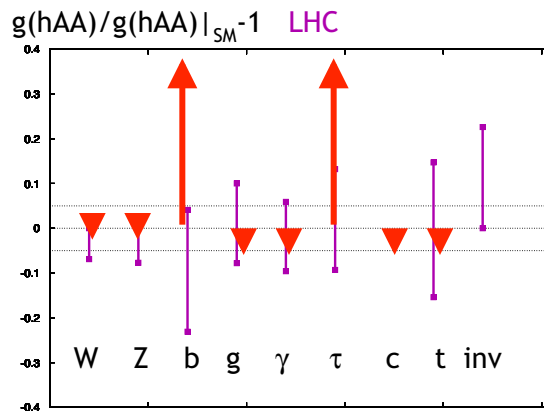
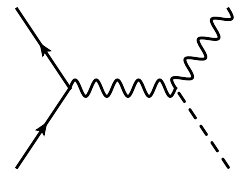
□ Type-II Yukawa interaction w/ **SUSY** relation

$$\begin{cases} \Phi_u : u, \\ \Phi_d : d, \ell \end{cases}$$

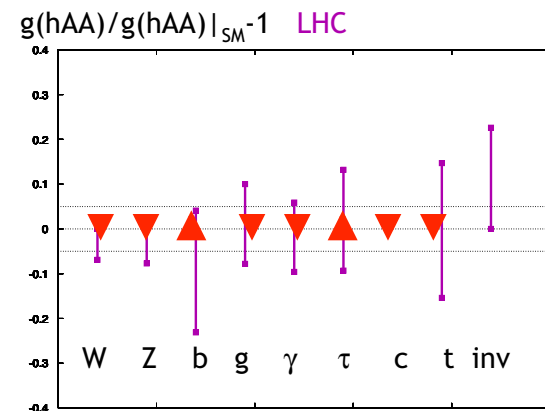
$$\sin(\beta - \alpha) \simeq 1 - \frac{2m_Z^4}{m_A^4 \tan^2 \beta} \approx 1$$

$$\frac{g_{hbb}}{g_{hbb}^{\text{SM}}} = \frac{g_{h\tau\tau}}{g_{h\tau\tau}^{\text{SM}}} = \sin(\beta - \alpha) - \tan \beta \cos(\beta - \alpha) \simeq 1 + \frac{2m_Z^2}{m_A^2}$$

$$\frac{g_{htt}}{g_{htt}^{\text{SM}}} = \sin(\beta - \alpha) + \cot \beta \cos(\beta - \alpha) \simeq 1 - \frac{2m_Z^2}{m_A^2 \tan^2 \beta}$$



$m_A = 200 \text{ GeV}$
w/ $\tan \beta = 5$



$m_A \gg m_Z$
w/ $\tan \beta = 5$

BG figure is taken from 1207.2516 by Peskin

SM-like Higgs in **SUSY**

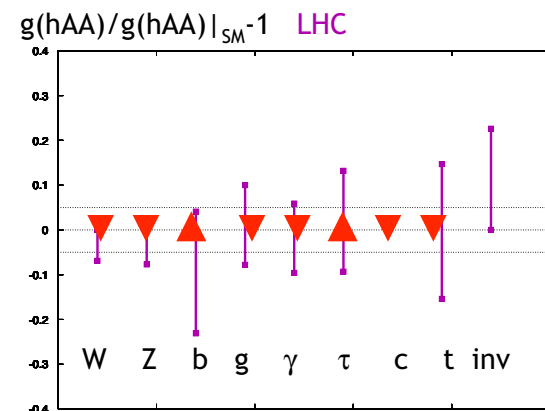
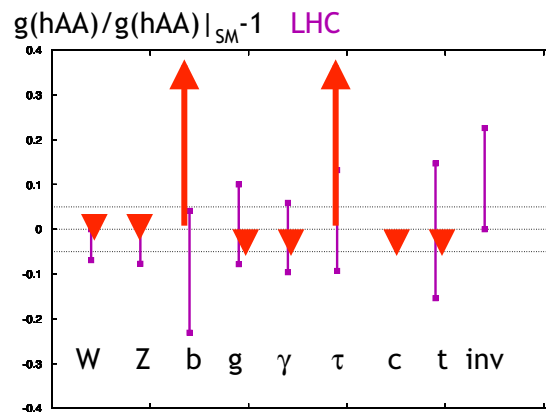
□ SUSY Higgs sector is the most popular 2HDM

□ Type-II Yukawa interaction w/ SUSY relation

$$\begin{cases} \Phi_u : u, \\ \Phi_d : d, \ell \end{cases}$$

$$\frac{g_{hbb}^{\text{SM}}}{g_{hbb}} = \frac{g_{h\tau\tau}^{\text{SM}}}{g_{h\tau\tau}} = \sin(\beta - \alpha) - \tan \beta \cos(\beta - \alpha) \simeq 1 + \frac{2m_Z^2}{m_A^2}$$

hbb deviation can probe m_A scale



SM-like Higgs in 2HDMs

□ 2HDM-II

$$\sin(\beta - \alpha) \not\approx 1 - \frac{2m_Z^4}{m_A^4 \tan^2 \beta}$$

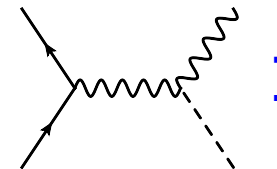
□ Type-II Yukawa interaction w/o SUSY relation

$$\begin{cases} \Phi_u : u, \\ \Phi_d : d, \ell \end{cases}$$

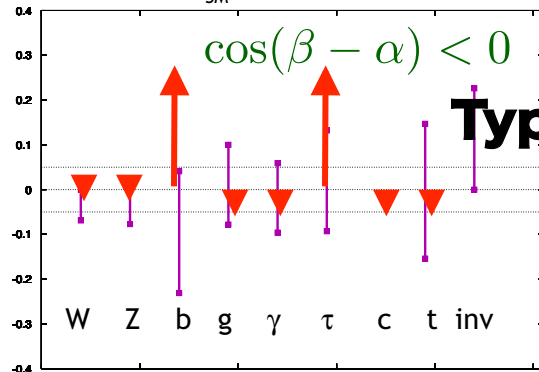
$$\begin{aligned} \frac{g_{hbb}^{\text{SM}}}{g_{hbb}^{\text{SM}}} &= \frac{g_{h\tau\tau}^{\text{SM}}}{g_{h\tau\tau}^{\text{SM}}} = \sin(\beta - \alpha) - \tan \beta \cos(\beta - \alpha) \\ \frac{g_{htt}^{\text{SM}}}{g_{htt}^{\text{SM}}} &= \sin(\beta - \alpha) + \cot \beta \cos(\beta - \alpha) \end{aligned}$$

❖ No m_A dependence [$\sin(\beta - \alpha)$ is determined by

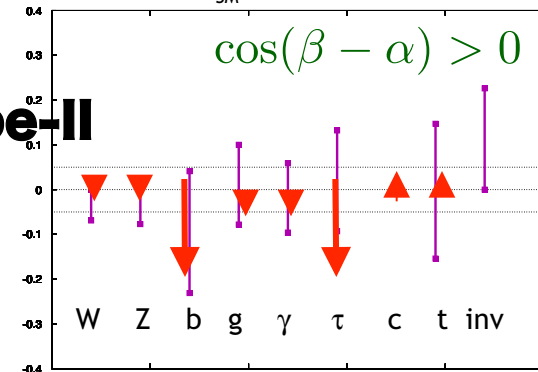
❖ $\cos(\beta - \alpha)$ can be sizable and positive



$g(hAA)/g(hAA)|_{\text{SM}}^{-1}$ LHC



$g(hAA)/g(hAA)|_{\text{SM}}^{-1}$ LHC



SM-like Higgs in 2HDMs

□ 2HDM-II

$$\sin(\beta - \alpha) \not\approx 1 - \frac{2m_Z^4}{m_A^4 \tan^2 \beta}$$

□ Type-II Yukawa interaction w/o SUSY relation

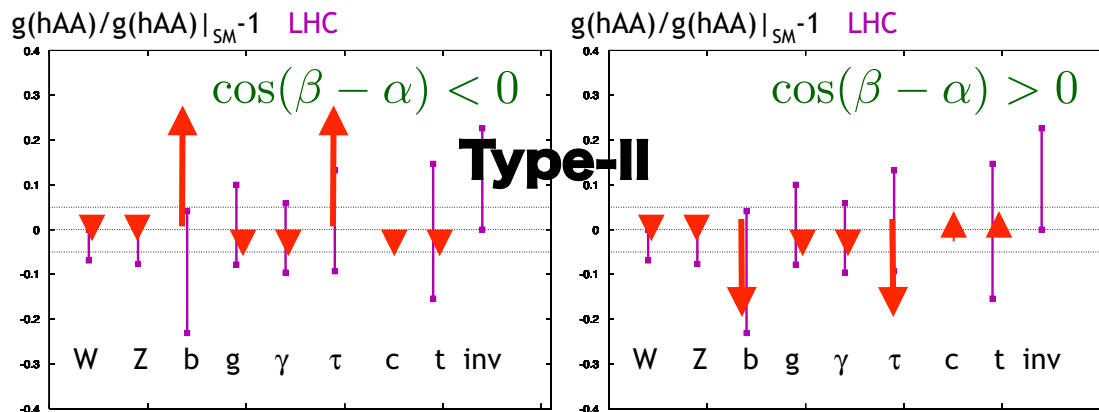
$$\begin{cases} \Phi_u : u, \\ \Phi_d : d, \ell \end{cases}$$

$$\frac{g_{hbb}^{\text{SM}}}{g_{hbb}^{\text{SM}}} = \frac{g_{h\tau\tau}^{\text{SM}}}{g_{h\tau\tau}^{\text{SM}}} = \sin(\beta - \alpha) - \tan \beta \cos(\beta - \alpha)$$

$$\frac{g_{htt}^{\text{SM}}}{g_{htt}^{\text{SM}}} = \sin(\beta - \alpha) + \cot \beta \cos(\beta - \alpha)$$

$\sin(\beta - \alpha)$ + hff deviations (w/o m_A)

→ determination of $\tan \beta$



SM-like Higgs in 2HDMs

□ 2HDM-II

$$\sin(\beta - \alpha) \not\approx 1 - \frac{2m_Z^4}{m_A^4 \tan^2 \beta}$$

□ Type-II Yukawa interaction w/o SUSY relation

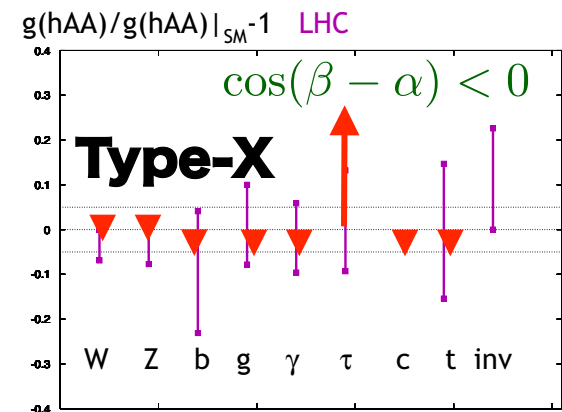
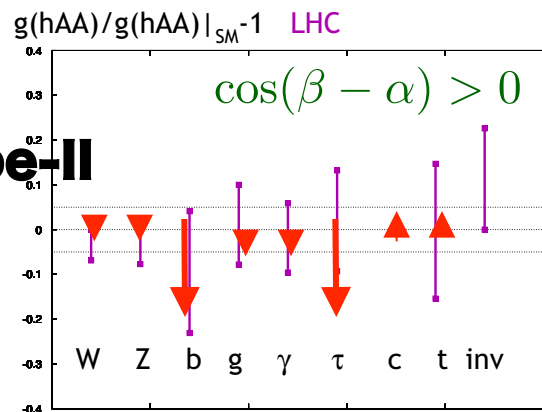
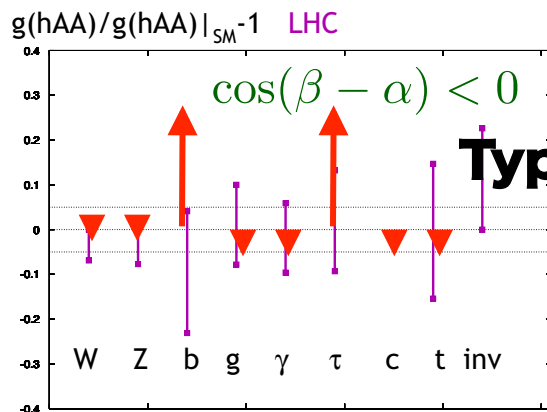
$$\begin{cases} \Phi_u : u, \\ \Phi_d : d, \ell \end{cases}$$

$$\frac{g_{hbb}^{\text{SM}}}{g_{hbb}} = \frac{g_{h\tau\tau}^{\text{SM}}}{g_{h\tau\tau}} = \sin(\beta - \alpha) - \tan \beta \cos(\beta - \alpha)$$

$$\frac{g_{htt}^{\text{SM}}}{g_{htt}} = \sin(\beta - \alpha) + \cot \beta \cos(\beta - \alpha)$$

$\sin(\beta - \alpha)$ + hff deviations (w/o m_A)

→ **discrimination of types of Yukawa**



Observable	Expected Error (experiment \oplus theory)
LHC at 14 TeV with 300 fb ⁻¹	
$\sigma(gg) \cdot BR(\gamma\gamma)$	0.06 \oplus 0.13
$\sigma(WW) \cdot BR(\gamma\gamma)$	0.15 \oplus 0.10
$\sigma(gg) \cdot BR(ZZ)$	0.08 \oplus 0.08
$\sigma(gg) \cdot BR(WW)$	0.09 \oplus 0.11
$\sigma(WW) \cdot BR(WW)$	0.27 \oplus 0.10
$\sigma(gg) \cdot BR(\tau^+\tau^-)$	0.11 \oplus 0.13
$\sigma(WW) \cdot BR(\tau^+\tau^-)$	0.15 \oplus 0.10
$\sigma(Wh) \cdot BR(b\bar{b})$	0.25 \oplus 0.20
$\sigma(Wh) \cdot BR(\gamma\gamma)$	0.24 \oplus 0.10
$\sigma(Zh) \cdot BR(b\bar{b})$	0.25 \oplus 0.20
$\sigma(Zh) \cdot BR(\gamma\gamma)$	0.24 \oplus 0.10
$\sigma(t\bar{t}h) \cdot BR(b\bar{b})$	0.25 \oplus 0.20
$\sigma(t\bar{t}h) \cdot BR(\gamma\gamma)$	0.42 \oplus 0.10
$\sigma(WW) \cdot BR(\text{invisible})$	0.2 \oplus 0.24

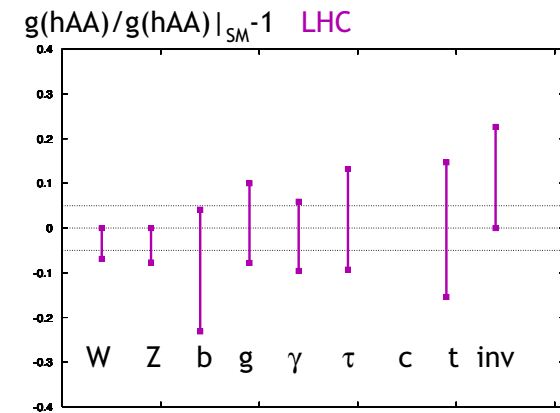


Table 1: Input data for the fits to Higgs couplings from LHC measurements.

Observable	Expected Error
ILC at 250 GeV with 250 fb ⁻¹	
$\sigma(Zh)$	0.025
$\sigma(Zh) \cdot BR(b\bar{b})$	0.010
$\sigma(Zh) \cdot BR(c\bar{c})$	0.069
$\sigma(Zh) \cdot BR(gg)$	0.085
$\sigma(Zh) \cdot BR(WW)$	0.08
$\sigma(Zh) \cdot BR(ZZ)$	0.28
$\sigma(Zh) \cdot BR(\tau^+\tau^-)$	0.05
$\sigma(Zh) \cdot BR(\gamma\gamma)$	0.27
$\sigma(Zh) \cdot BR(\text{invisible})$	0.005

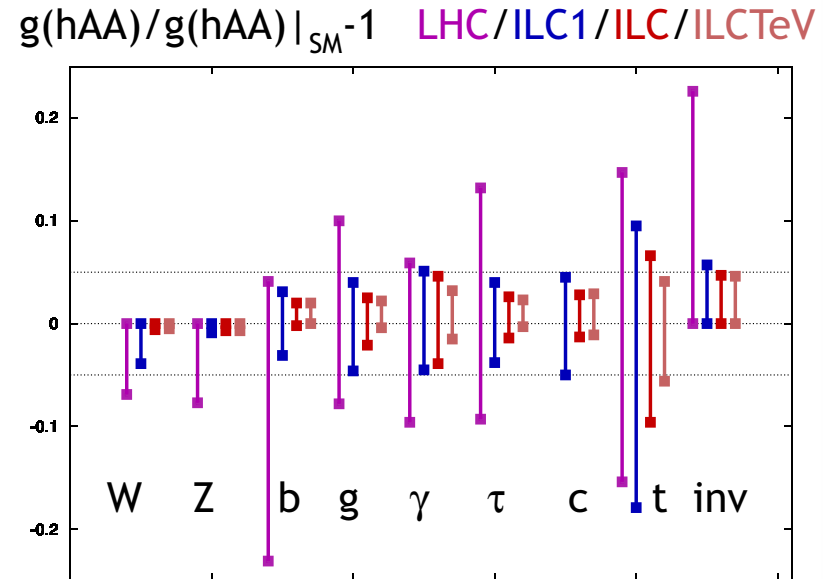


Table 2: Input data for the fits to Higgs couplings from ILC measurements.

SUSY Higgs sector

CP even sector

$$\mathcal{M}^2 = \mathcal{M}_{\text{tree}}^2 + \begin{pmatrix} 0 & 0 \\ 0 & \epsilon \end{pmatrix}$$

Quantum corrections

$$\epsilon \simeq \frac{3 \bar{m}_t^4}{2\pi^2 v^2 \sin^2 \beta} \left[\ln \frac{M_S^2}{\bar{m}_t^2} + \frac{X_t^2}{2M_S^2} \left(1 - \frac{X_t^2}{6M_S^2} \right) \right]$$

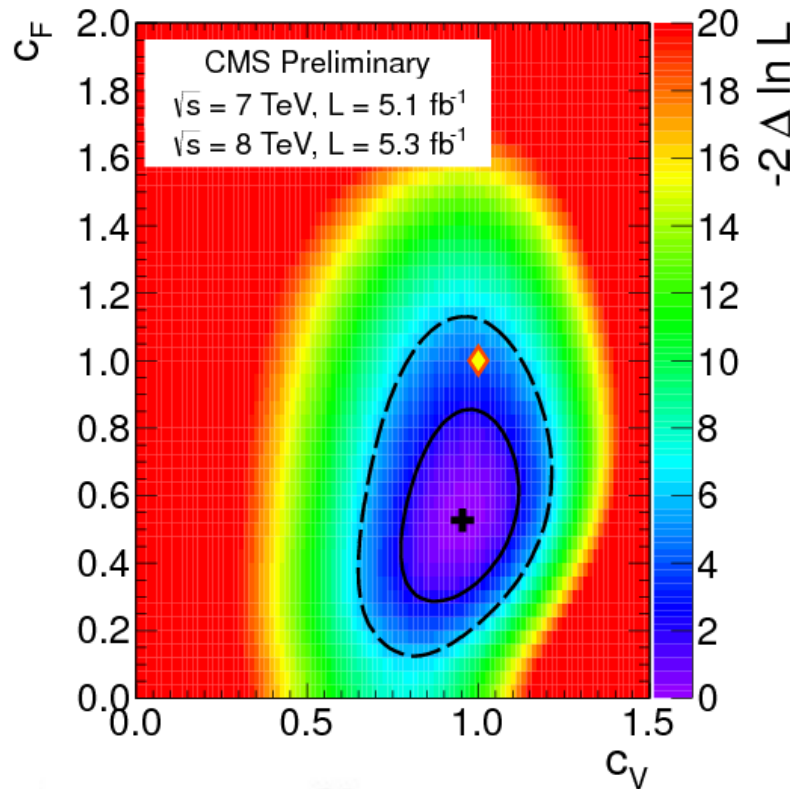
Mass eigenvalues & mixing angle

$$m_{h,H}^2 = \frac{1}{2}(m_A^2 + m_Z^2 + \epsilon) \left[1 \mp \sqrt{1 - 4 \frac{m_Z^2 m_A^2 \cos^2 2\beta + \epsilon(m_A^2 \sin^2 \beta + m_Z^2 \cos^2 \beta)}{(m_A^2 + m_Z^2 + \epsilon)^2}} \right]$$

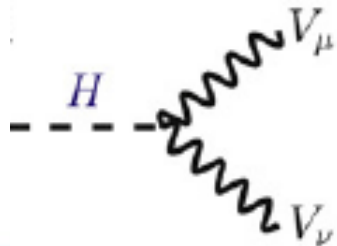
$$\tan 2\alpha = \tan 2\beta \frac{m_A^2 + m_Z^2}{m_A^2 - m_Z^2 + \epsilon / \cos 2\beta}$$

SM-like?

- SM-like gauge-gauge-Higgs coupling is favored



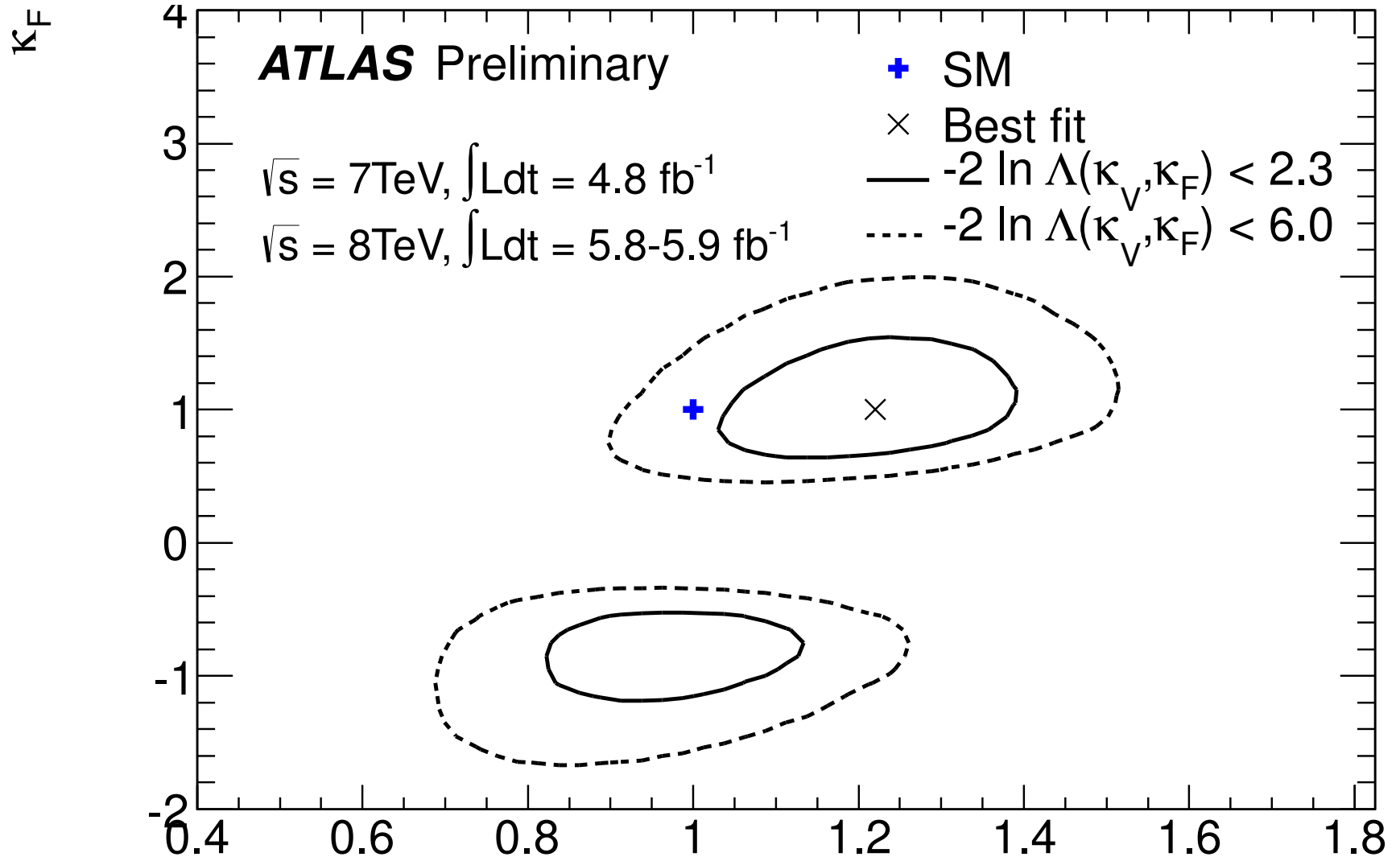
Production	Decay	LO SM	
VH	$H \rightarrow bb$	$\sim \frac{C_V^2 \times C_F^2}{C_F^2}$	$\sim C_V^2$
ttH	$H \rightarrow bb$	$\sim \frac{C_F^2 \times C_F^2}{C_F^2}$	$\sim C_F^2$
VBF/VH	$H \rightarrow \tau\tau$	$\sim \frac{C_V^2 \times C_F^2}{C_F^2}$	$\sim C_V^2$
ggH	$H \rightarrow \tau\tau$	$\sim \frac{C_F^2 \times C_F^2}{C_F^2}$	$\sim C_F^2$
ggH	$H \rightarrow ZZ$	$\sim \frac{C_F^2 \times C_V^2}{C_F^2}$	$\sim C_V^2$
ggH	$H \rightarrow WW$	$\sim \frac{C_F^2 \times C_V^2}{C_F^2}$	$\sim C_V^2$
VBF/VH	$H \rightarrow WW$	$\sim \frac{C_V^2 \times C_V^2}{C_F^2}$	$\sim C_V^4 / C_F^2$
ggH	$H \rightarrow \gamma\gamma$	$\sim \frac{C_F^2 \times (8.6C_V - 1.8C_F)^2}{C_F^2}$	$\sim C_V^2$
VBF	$H \rightarrow \gamma\gamma$	$\sim \frac{C_V^2 \times (8.6C_V - 1.8C_F)^2}{C_F^2}$	$\sim C_V^4 / C_F^2$



$$W_\mu^+ W_\nu^+ h : ig_W M_W \sin(\beta - \alpha) g_{\mu\nu}$$

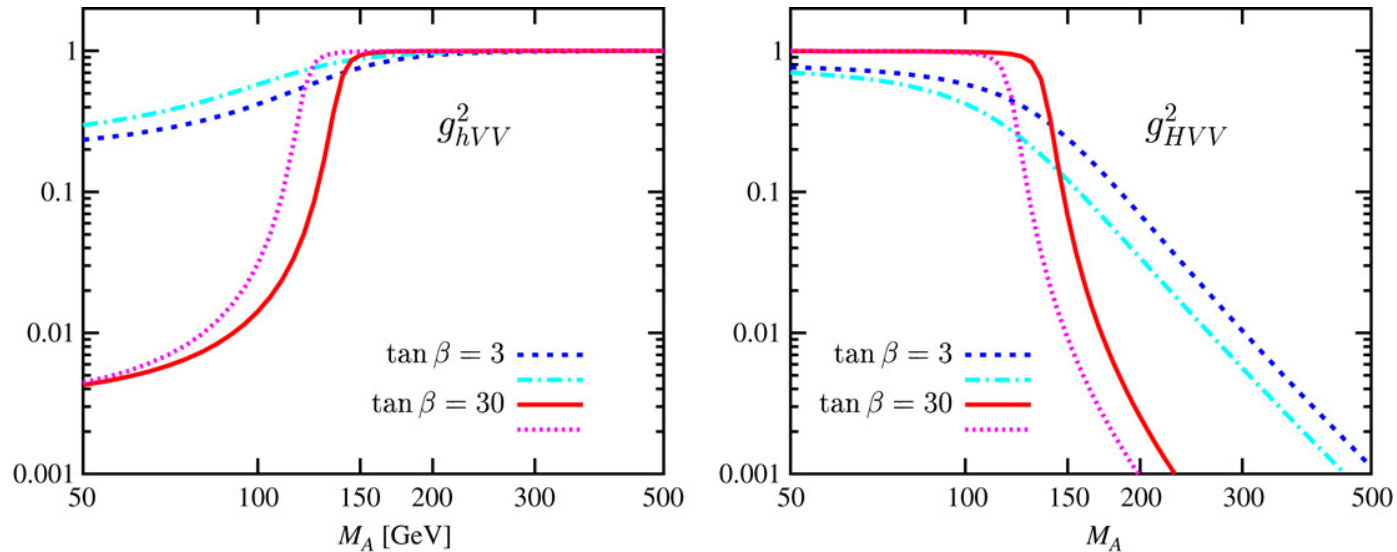
sin(β-α) can be different from unity





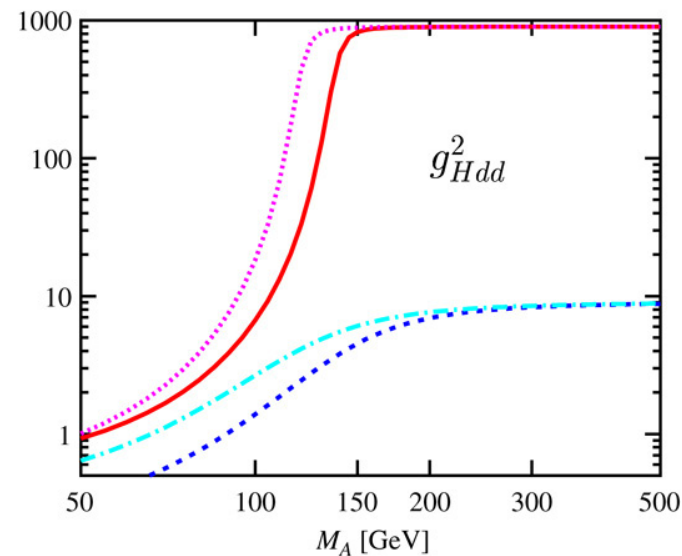
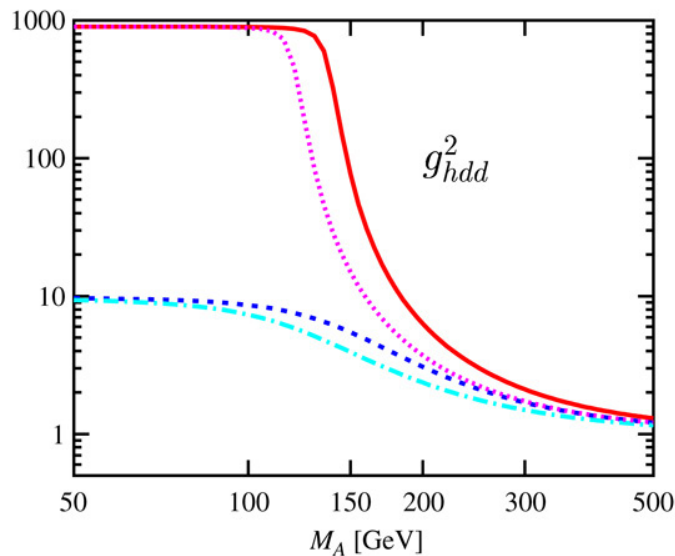
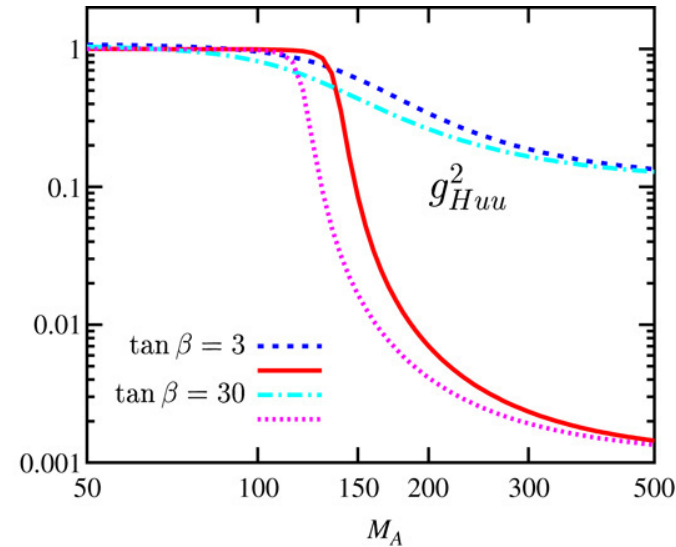
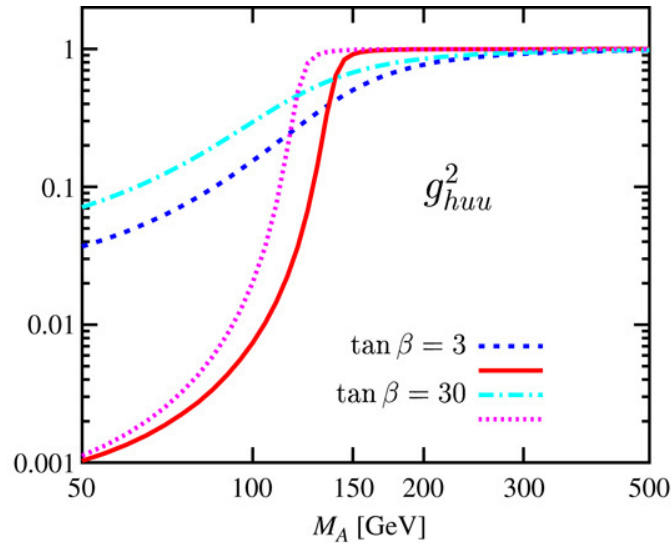
Gauge coupling in MSSM

Djouadi (2008)



Yukawa coupling in MSSM

Djouadi (2008)



Event analysis details

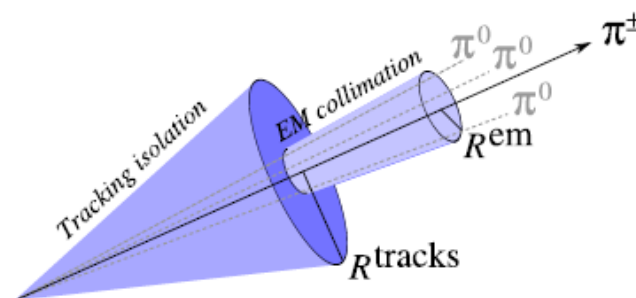
-MadGraph5: event generation, calculate (diff.) σ

-PYTHIA: hadronization (quark, $\tau \rightarrow$ hadron)

w/ TAUOLA (tau polarization)

-FastJet: (construct jets from hadrons)

jet is defined by anti-kT w/ $R < 0.4$



→ Detector simulation

(construct kinematical variables such as invariant mass, etc...)

□ $\tan\beta$ enhancement in λ couplings

$$\lambda_1 = \frac{1}{v^2 \cos^2 \beta} (-M^2 \sin^2 \beta + m_H^2 \cos^2 \alpha + m_h^2 \sin^2 \alpha)$$

$$\lambda_2 = \frac{1}{v^2 \sin^2 \beta} (-M^2 \cos^2 \beta + m_H^2 \sin^2 \alpha + m_h^2 \cos^2 \alpha)$$

$$\lambda_3 = \frac{1}{v^2} \left[-M^2 + (m_H^2 - m_h^2) \frac{\sin 2\alpha}{\sin 2\beta} + 2m_{H^\pm}^2 \right]$$

nearly SM-like ($\beta - \alpha = \pi/2 - \delta$), and $M = M_H = M_{H^\pm}$

$$\begin{aligned}\lambda_1 &\rightarrow +\frac{m_h^2}{v^2} - \frac{2(M^2 - m_h^2)t_\beta}{v^2} \delta - \frac{(M^2 - m_h^2)t_\beta^2}{v^2} \delta^2 \\ \lambda_2 &\rightarrow +\frac{m_h^2}{v^2} + \frac{2(M^2 - m_h^2)/t_\beta}{v^2} \delta + \frac{(M^2 - m_h^2)/t_\beta^2}{v^2} \delta^2 \\ \lambda_3 &\rightarrow +\frac{m_h^2}{v^2} + \frac{2(M^2 - m_h^2)}{v^2} \delta + \frac{(M^2 - m_h^2)}{v^2} \delta^2\end{aligned}$$

Only λ_1 diverges
@ large $\tan\beta$