

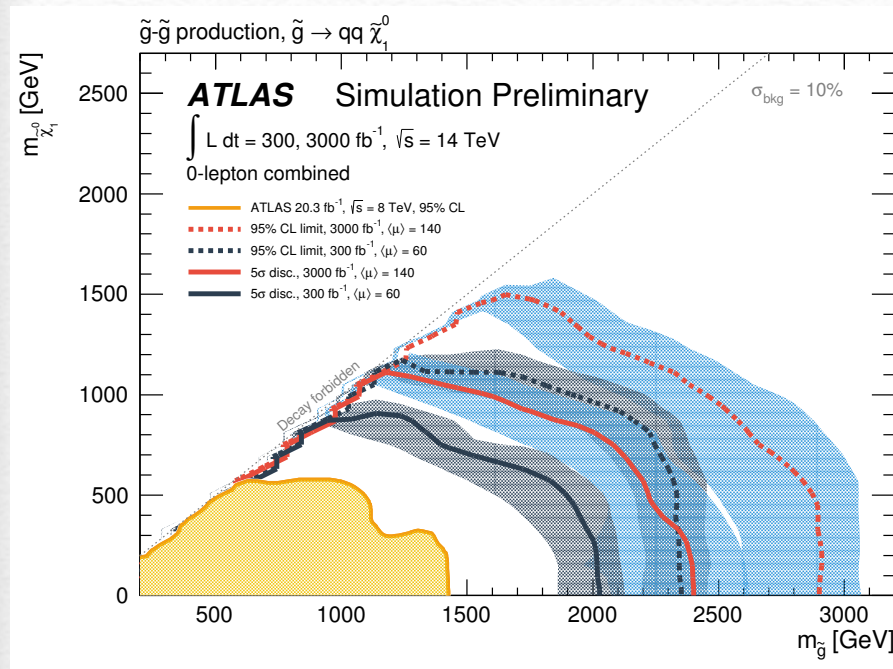
# Footprint of BSM Higgs sector

**Mihoko Nojiri (KEK &IPMU)**  
based on work with  
**Motoi Endo, Takeo Moroi**  
(Tokyo University )  
and work with  
**Hirohisa Kubota(KEK)**

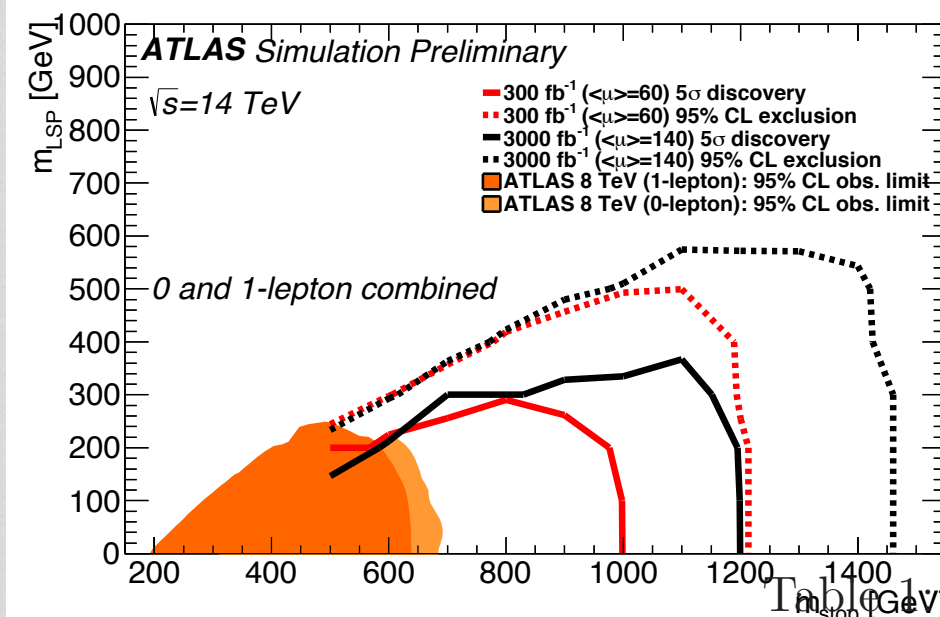


# starting soon

## LHC at 13 TeV toward HL-LHC



(a)  $\tilde{q}\tilde{q}$



Exclude gluino mass up to 3 TeV and  
degenerate case LSP mass up to 1.5 TeV  
scalar top up to 1.4 TeV

discovery potential of stop

—Future prospects 1309.1514

Collider	Energy	Luminosity	Cross Section	Mass
LHC8	8 TeV	20.5 $\text{fb}^{-1}$	10 fb	650 GeV
LHC	14 TeV	300 $\text{fb}^{-1}$	3.5 fb	1.0 GeV
HL LHC	14 TeV	3 $\text{ab}^{-1}$	1.1 fb	1.2 TeV
HE LHC	33 TeV	3 $\text{ab}^{-1}$	91 ab	3.0 TeV
VLHC	100 TeV	1 $\text{ab}^{-1}$	200 ab	5.7 TeV

The first line gives the current bound on stops from the LHC [7]. The remaining lines give the estimated 5 $\sigma$  discovery reach in stop pair production cross section and mass for hadron collider runs.

The 95% CL exclusion limits (dashed) and 5 $\sigma$  discovery reach (solid) for 300  $\text{fb}^{-1}$  (red) and 3000  $\text{fb}^{-1}$  (black) in the  $\tilde{t}, \tilde{\chi}_1^0$  mass plane assuming  $\tilde{t} \rightarrow t + \tilde{\chi}_1^0$  with a branching ratio of 100%. The



If we do not find “anything”  
at LHC, HL-LHC

- ❖ Should we build  $e^+ e^-$  collider?
- ❖ New channel: Higgs production and decay.
- ❖ How much we can learn by looking into Higgs sector in SUSY, MCHM,....
- ❖ New: CCB constraint and Higgs decays



# SUSY Higgs sector

- ❖ Type II model
- ❖ SUSY: 4point Higgs coupling ~ gauge coupling
- ❖ Radiative correction from top sector  
Higgs mass  $\Leftrightarrow$  SUSY scale and stop mixing

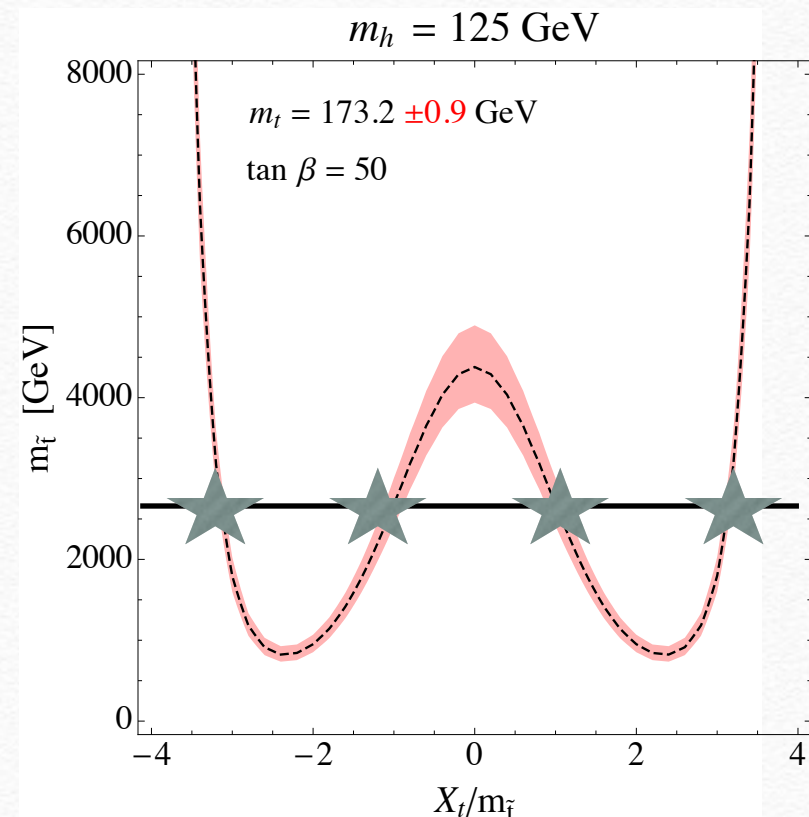
Okada Yamaguchi Yanagida  
Ellis Ridolfi Zwirner  
Haber Hempfling (1991)

$$\delta m_h^2 \simeq \frac{3m_t^4}{2\pi^2 v^2} \left[ \log \frac{m_{\tilde{t}}^2}{m_t^2} + \frac{X_t^2}{m_{\tilde{t}}^2} \left( 1 - \frac{X_t^2}{12m_{\tilde{t}}^2} \right) \right],$$

$$X_t = A_t - \mu \cot \beta$$

leading Higgs mass ~ one loop correction

$Y_t^4$ ,  $X_t^4$  dependent Large correction  
(NLO, yukawa and QCD correction)



from Gilly Elor et al 1206.5301

up to **4 solutions** for given  
stop mass



# Connection to Higgs Sector

## Bottom Yukawa coupling in MSSM( $A_t$ and $\mu$ )

- ❖ Non-holomorphic terms in the Yukawa coupling enhanced by  $\tan\beta$ , **non-decoupling**
- ❖ Large correction to the bottom Yukawa coupling if  $\mu < 0$  and  $A_t$  large, but suppressed by  $m_A^{-2}$  **decoupling**

effective Lagrangian Hall Rattazzi Sarid (93)  
Hempfling, Carena Olechowski Pokorski(94)

$$-\mathcal{L}_{\text{eff}} = y_b \epsilon_{ij} \bar{b}_R H_d^i Q_L^j + \Delta y_b \bar{b}_R Q_L^k H_u^{k*} + y_t \epsilon_{ij} \bar{t}_R Q_L^i H_u^j + \Delta y_t \bar{t}_R Q_L^k H_d^{k*} + \text{h.c.},$$

effective Yukawa

$$g_{h\bar{b}b} = - \left( \frac{\sin \alpha}{\cos \beta} \right) \frac{1 - \Delta_b \cot \alpha \cot \beta}{1 + \Delta_b} g_{h\bar{b}b}^{(\text{SM})}$$

$$= \left[ \sin(\beta - \alpha) - \frac{\tan \beta - \Delta_b \cot \beta}{1 + \Delta_b} \cos(\beta - \alpha) \right] g_{h\bar{b}b}^{(\text{SM})},$$

Carena Mrenna Wagner

sign of  $\Delta_b \sim$  sign of  $\mu$  makes difference

$y_b(\text{MSSM})$

$$y_b(M_{\text{SUSY}}) \simeq \frac{\sqrt{2} m_b(M_{\text{SUSY}})}{v \cos \beta (1 + \Delta_b)}.$$

$$\Delta_b \simeq \left[ \frac{2\alpha_s}{3\pi} M_3 \mu I(m_{\tilde{b}_1}^2, m_{\tilde{b}_2}^2, M_3^2) + \frac{y_t^2}{16\pi^2} \mu A_t I(m_{\tilde{t}_1}^2, m_{\tilde{t}_2}^2, \mu^2) \right] \tan \beta,$$

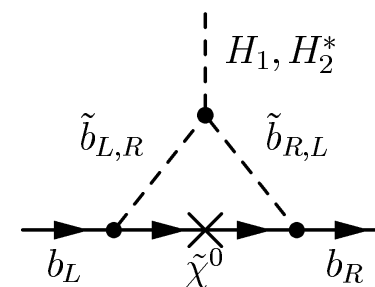
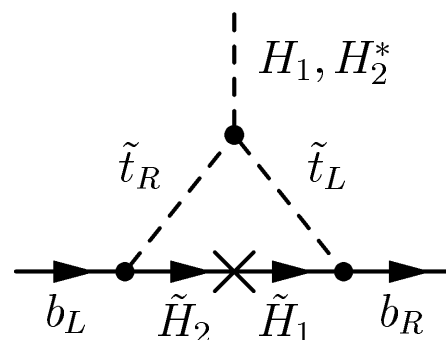
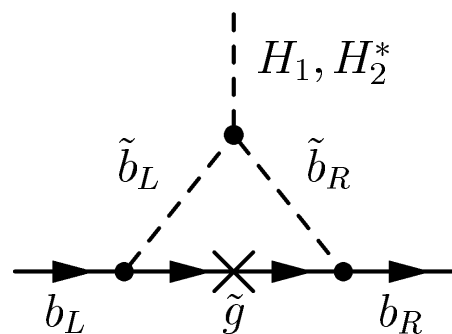


# Higgs branch and b-> s transition

H→bb

non decoupling for fixed mA

$$\mathcal{L}^{1\text{loop}} = (y_b + \Delta y_{b,1}) \bar{b}_R b_L H_1^0 + (\Delta y_{b,2}) \bar{b}_R b_L H_2^{0*} + \text{h.c.}$$



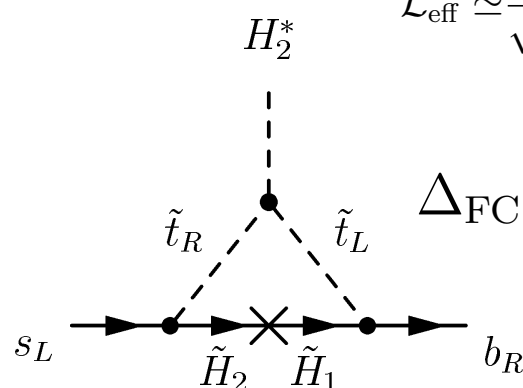
$$\mathcal{L} = \frac{\sqrt{2}m_i}{v_{SM}} \Phi_1^0 \bar{d}_R^i d_L^i + \lambda_2^{ij} \Phi_2^0 \bar{d}_R^i d_L^j + \text{h.c.}$$

Babu Kolda... using SuperISO 3.4 (Mahmoudi)

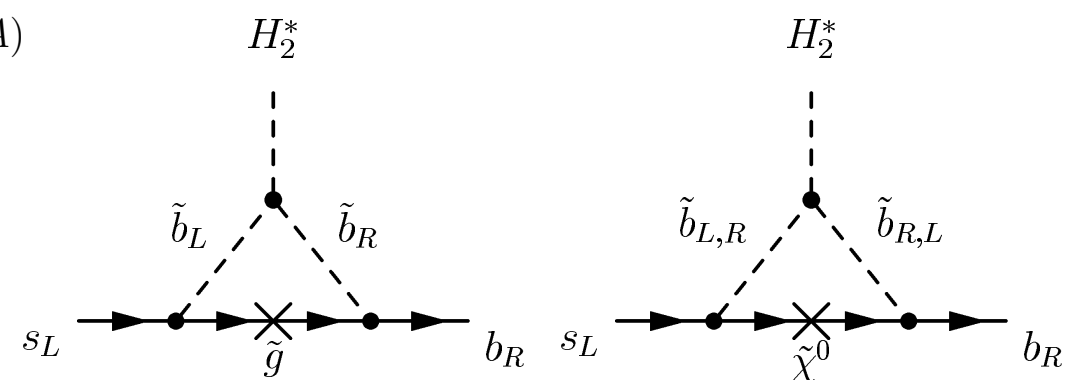
b→s transition

$$\mathcal{L}_{\text{eff}} \simeq \frac{gm_b}{\sqrt{2}m_W \cos \beta} \frac{\Delta_{\text{FC}}}{(1 + \Delta_b)(1 + \Delta_0)} V_{tb} V_{ts}^* (\bar{s}_L b_R) (H + iA)$$

$$\Delta_{\text{FC}} = \frac{y_t^2}{16\pi^2} \mu A_t \tan \beta I(m_{\tilde{t}_1}^2, m_{\tilde{t}_2}^2, \mu^2).$$



minimal



non minimal



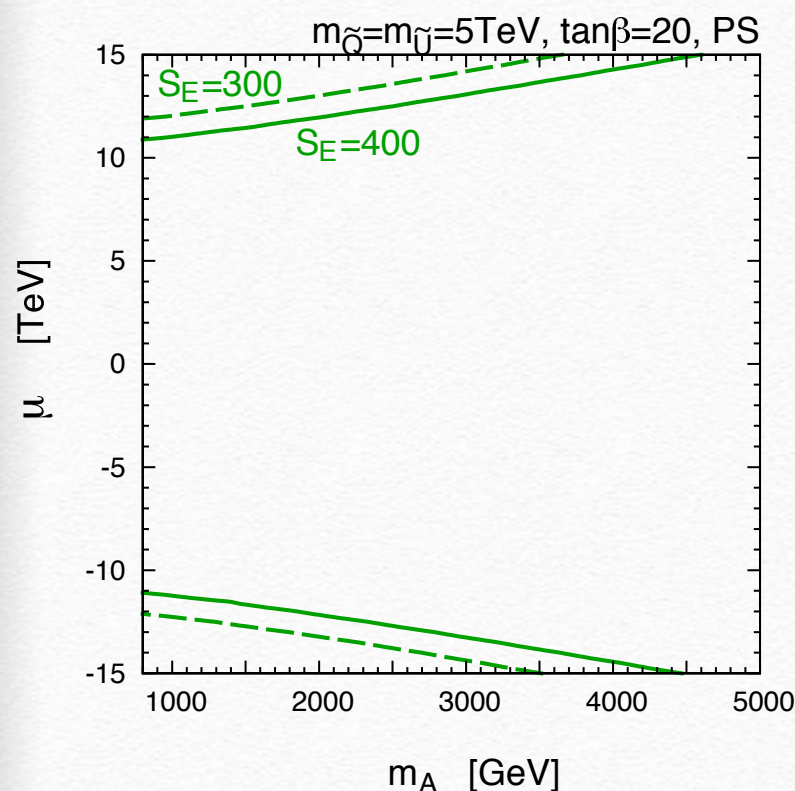
# CCB vacuum

- ❖ Higgs-stop-sbottom potential can have minimum deeper than EW vacuum. (... Casas, Lleyda and Munoz '96)
- ❖ Sufficiently small transition rate needed (Coleman, Callan Coleman '77)
- ❖ Previously  $A_t H_u t_L t_R$  term is considered but  $\mu H_d t_L t_R$  term can be same order  
 → upper bound to the  $\mu$  parameter for given squark mass and  $m_A$ .

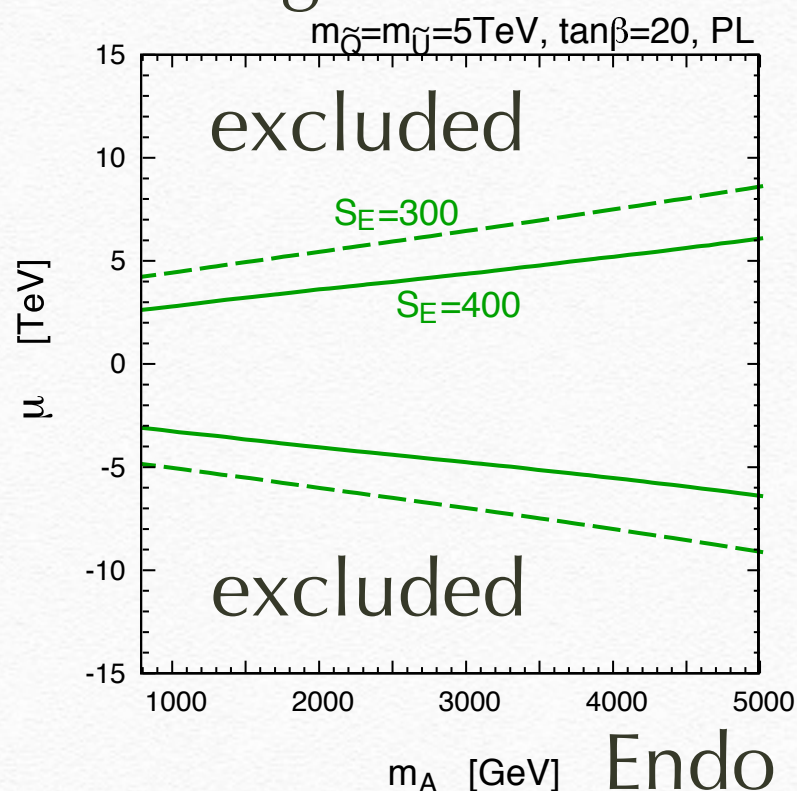
$$V = \frac{1}{2} m_{11}^2 h_d^2 + \frac{1}{2} m_{22}^2 h_u^2 - m_{12}^2 h_d h_u + \frac{1}{2} m_{\tilde{Q}}^2 \tilde{t}_L^2 + \frac{1}{2} m_{\tilde{U}}^2 \tilde{t}_R^2 + \frac{1}{\sqrt{2}} y_t (A_t h_u - \mu h_d) \tilde{t}_L \tilde{t}_R + \dots$$

soft  $\swarrow$   $\searrow$  susy  
 $\swarrow$   $\searrow$

small A solution



Large A solution



constraint on  $\mu$ !

numerical calculation  
cosmoTransition 2.0a1

The CCB vacuum is studied in  
Camargo-Molina et al 1309.7212  
Chowdhury et al 1310.1932  
Blinov et al 1310.4174  
in different constraint.

Endo Moroi Nojiri to appear



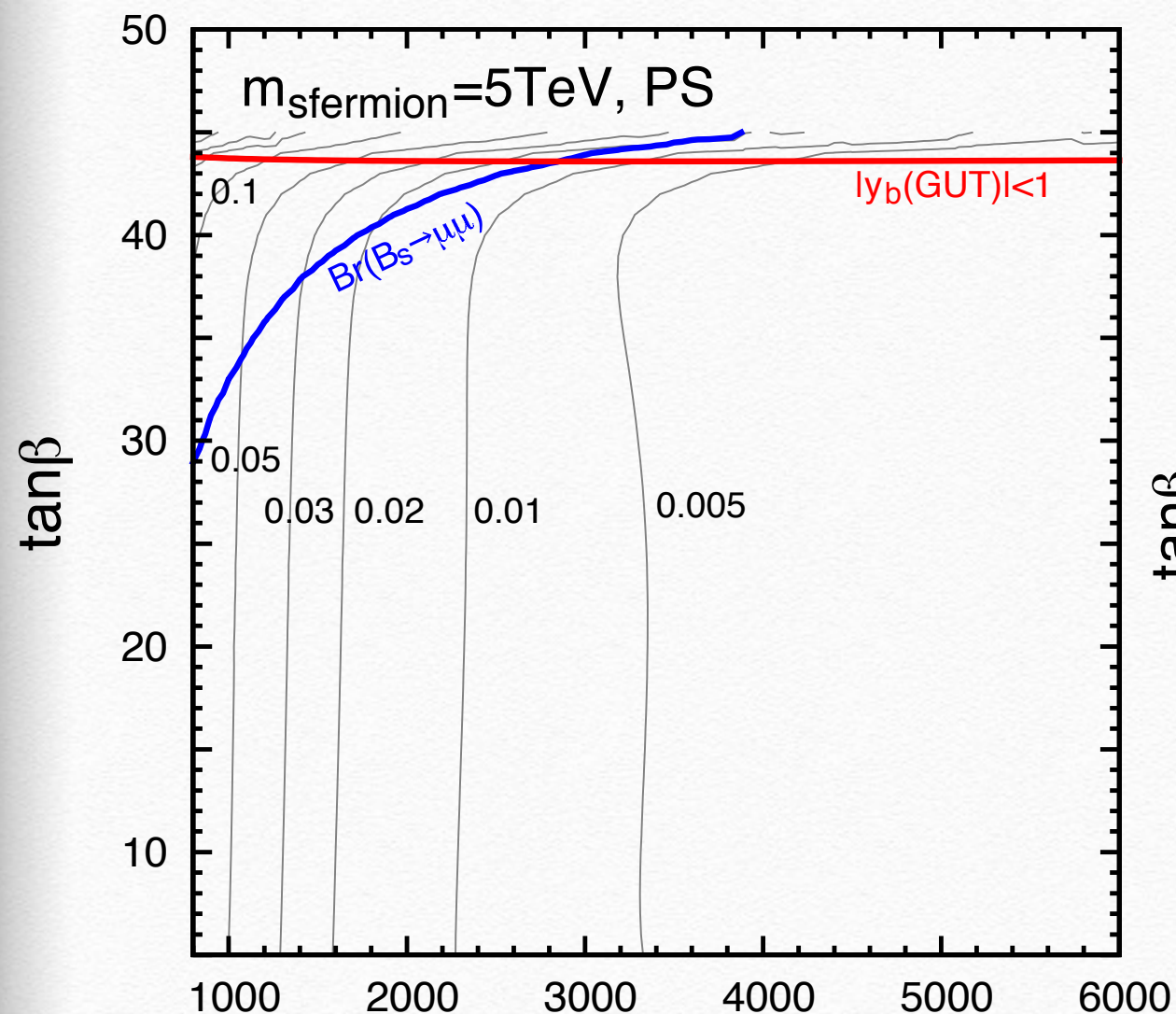
# a parameter scan

Endo Moroi MMN

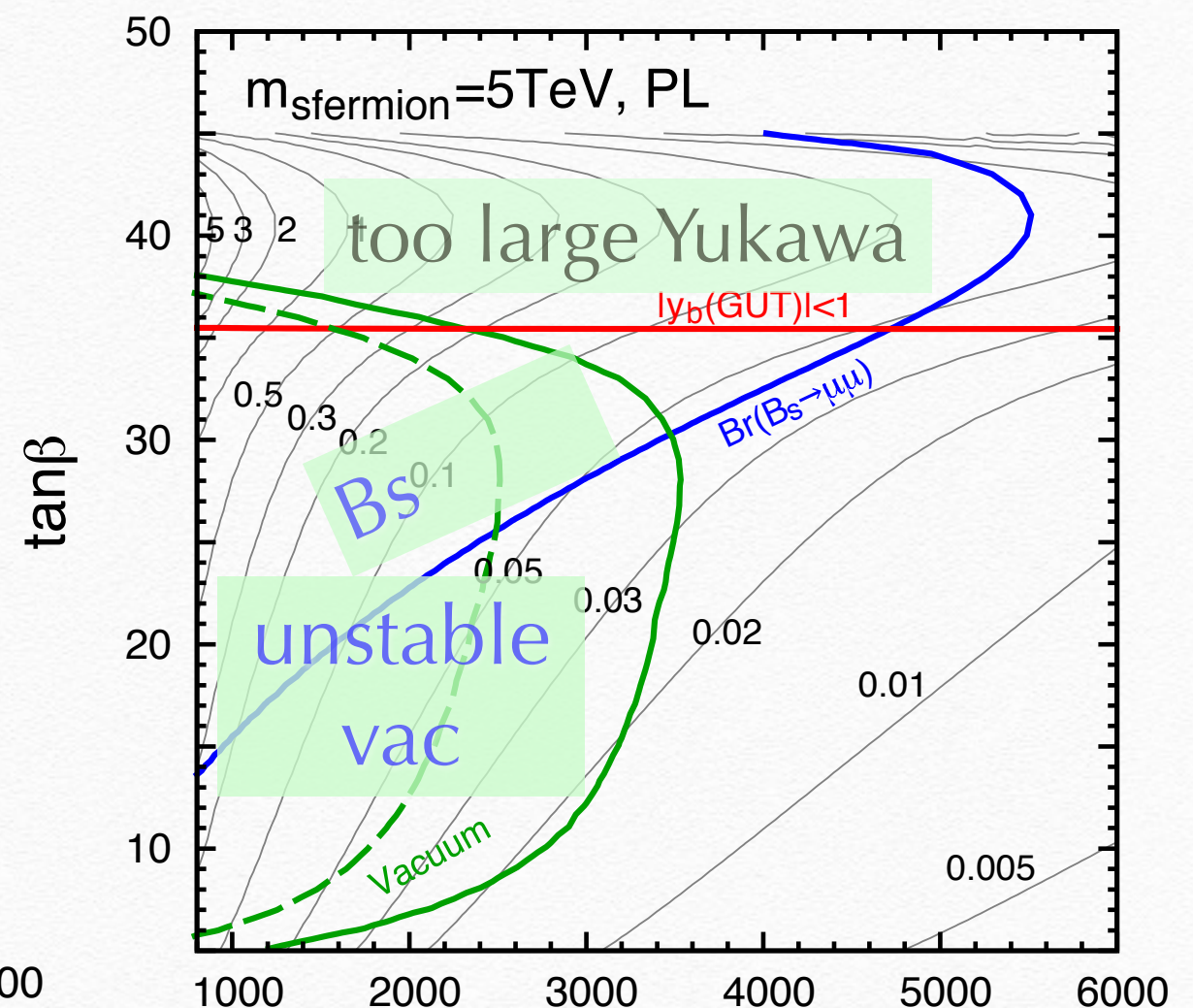
$$M_3 = -\mu = m(\text{sfermion}) \dots\dots = 5\text{TeV}$$

CCB vacuum constraint kill significant parameter space where  $\Delta\Gamma(h \rightarrow bb)$  is large

Small  $A_t > 0$



Large  $A_t > 0$





# full parameter scan

taken Universal because we are using SuperISO

- $m_{\tilde{Q}} = m_{\tilde{U}} = M_3 =$  3, 4, and 5 TeV, does not matter except  $h \rightarrow gg$
- $m_{\tilde{D}} = m_{\tilde{L}} = m_{\tilde{E}} = \max(m_{\tilde{U}}, |\mu|)$ ,
- $A_t = A_t^{(\text{NS})}, A_t^{(\text{NL})}, A_t^{(\text{PS})}, A_t^{(\text{PL})}$ , scan over all four  $A_t$  solution
- $0.8 \text{ TeV} < m_A < 6 \text{ TeV}$ ,
- $-2 < \mu/m_{\tilde{U}} < -0.5$ , or  $0.5 < \mu/m_{\tilde{U}} < 2$
- $5 < \tan \beta < 50$ .

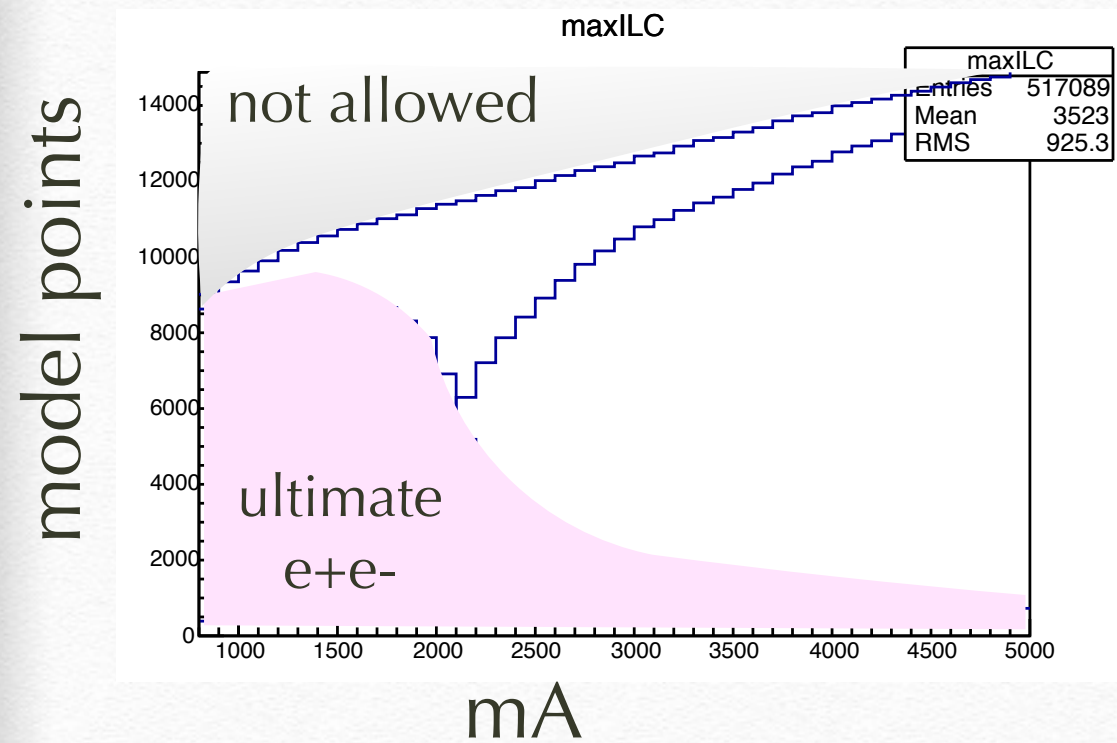
Extensive Modification of FeynHiggs to assure decoupling limit including **some bug** fix+choice of wave function renormalization (at  $p^2 = 0$ ) in higgs decay.

Our calculate include re-summation, higher order QCD  
(Hope this will be one of official options of FeynHiggs)



# accessibility to heavy higgs parameters

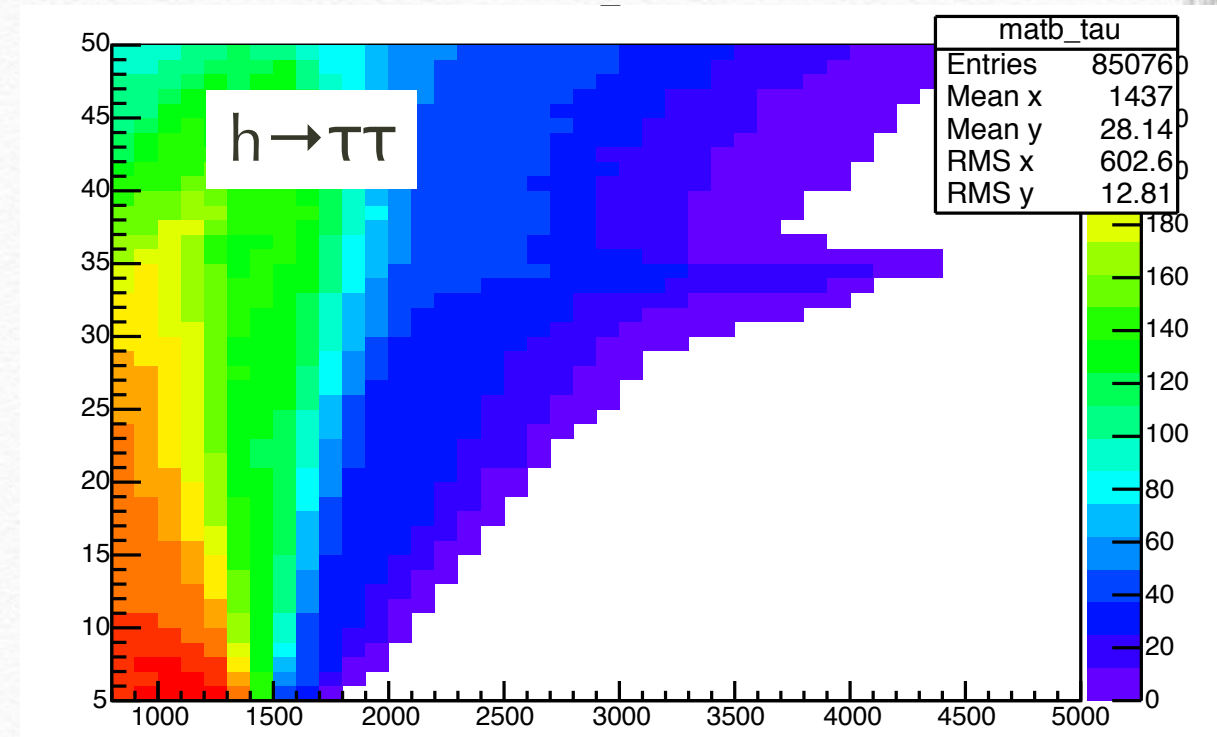
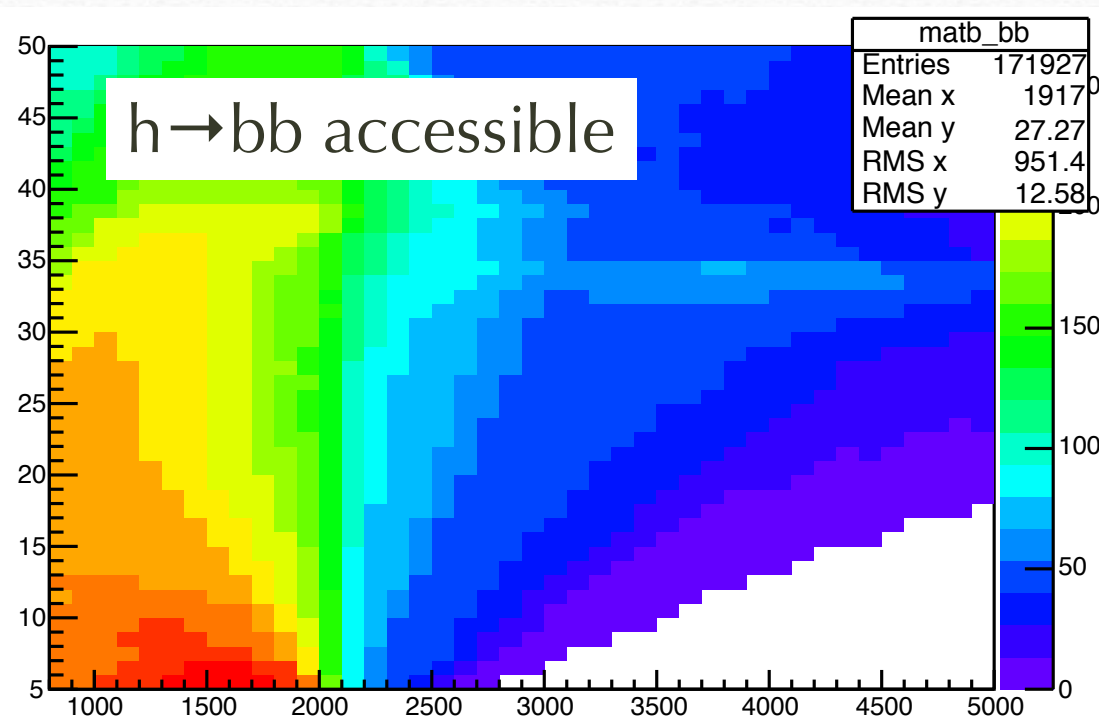
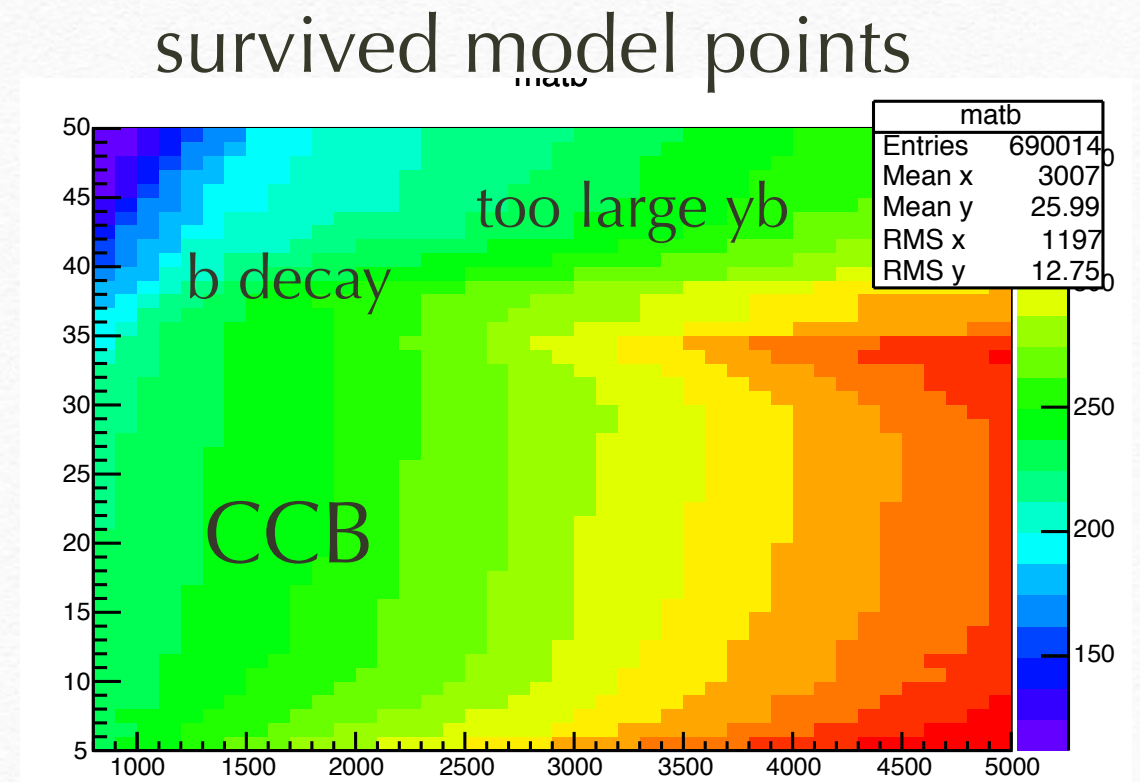
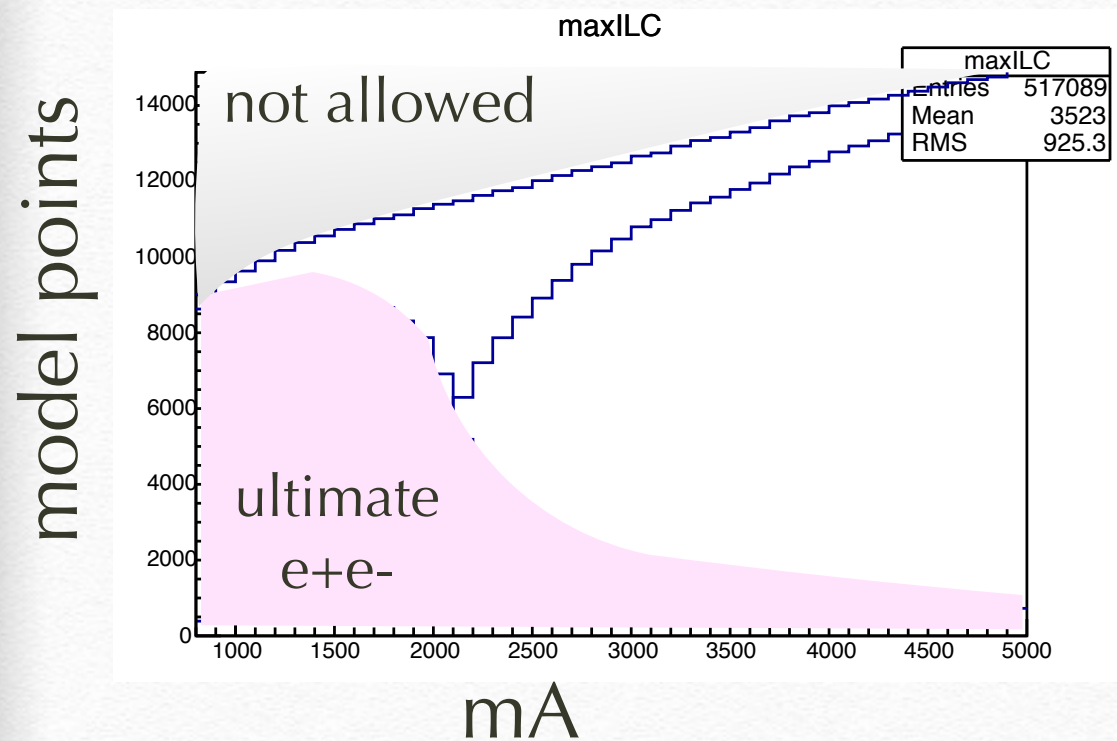
beyond  $m_A > 2000 \text{ GeV}$ , it is not easy to access deviation Endo Moroi, MMN





# accessibility to heavy higgs parameters

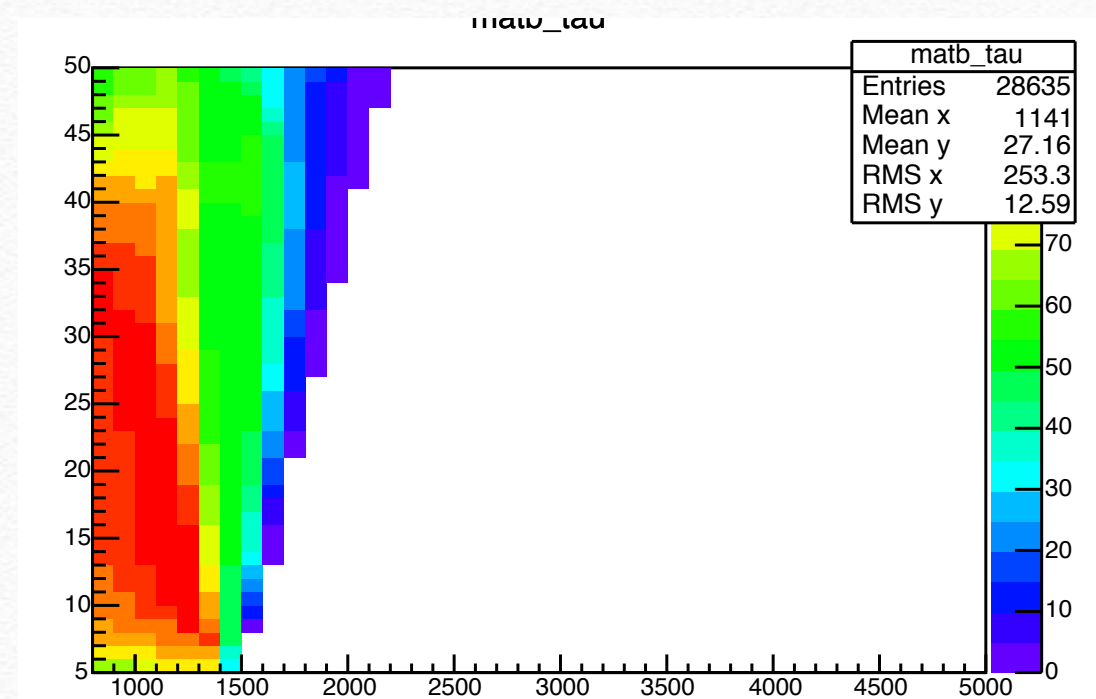
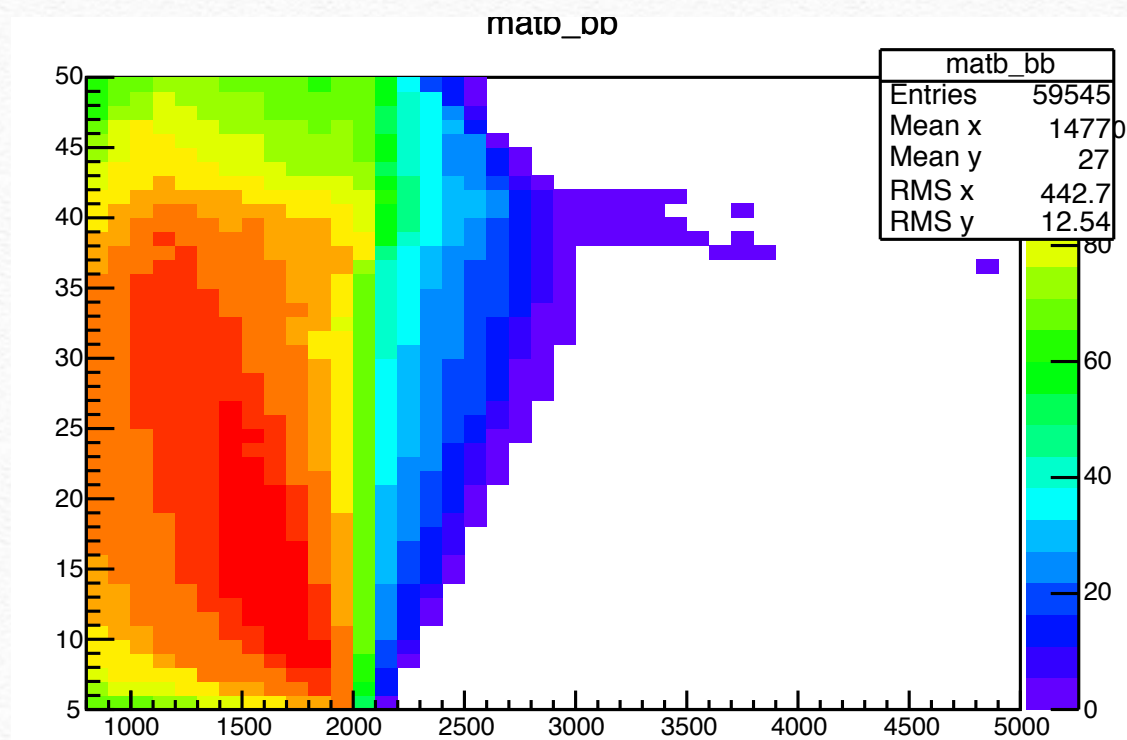
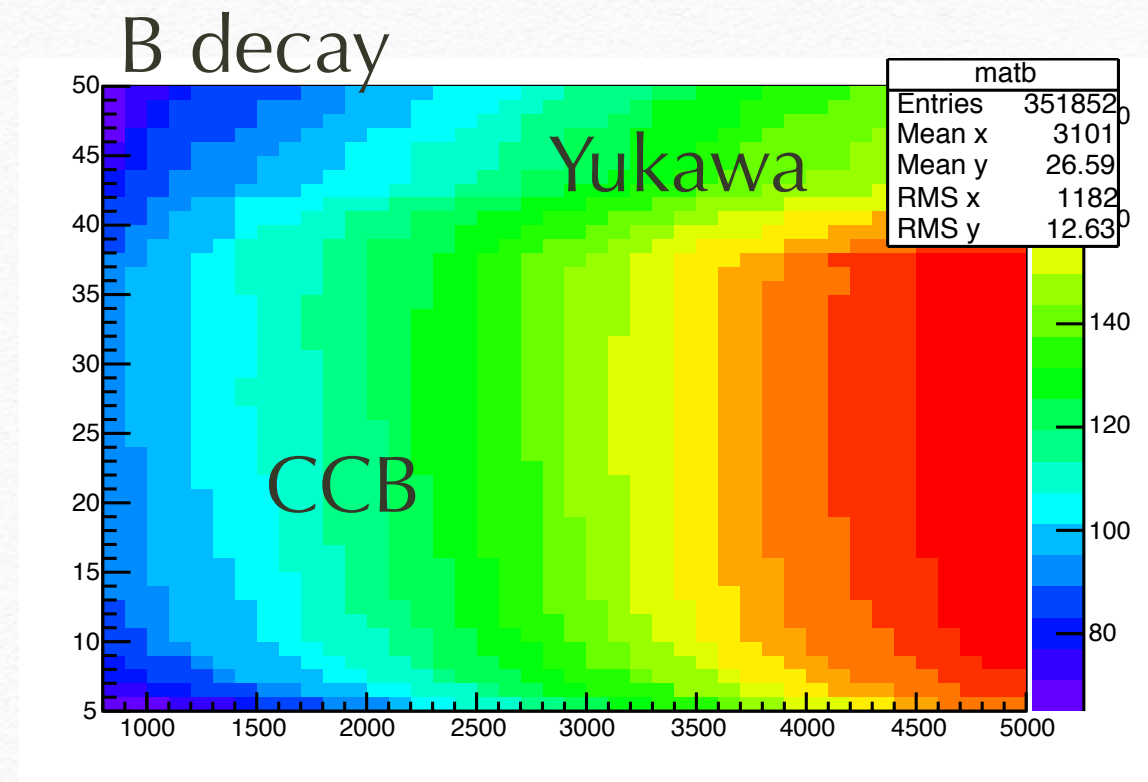
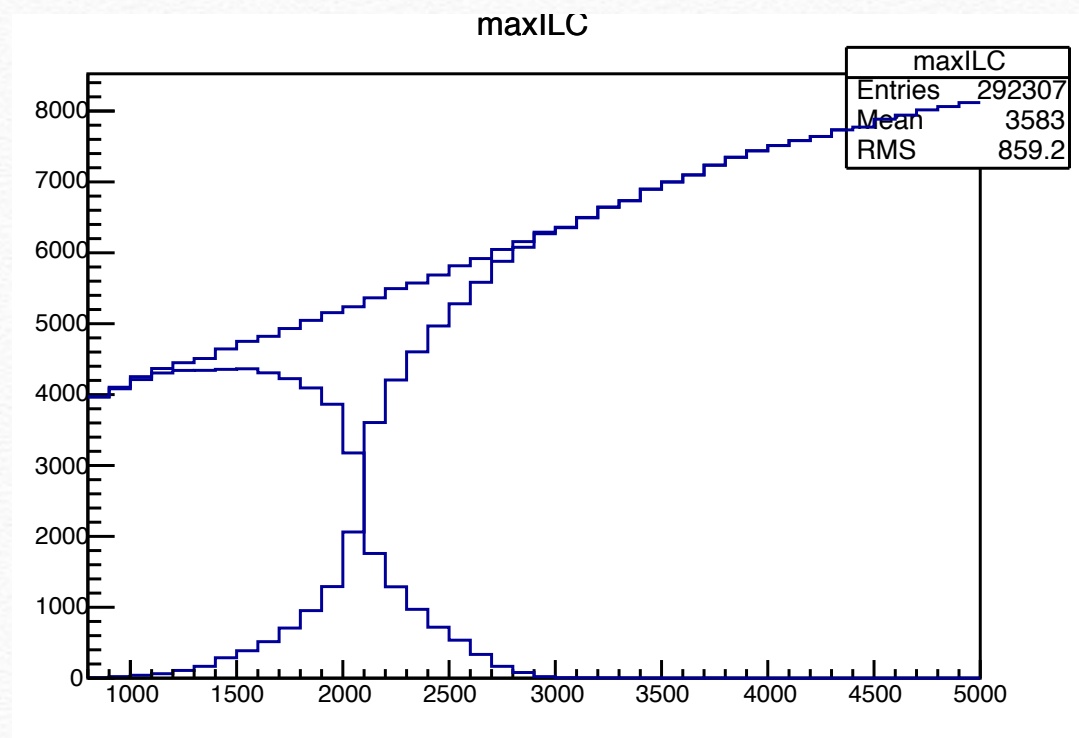
beyond  $m_A > 2000 \text{ GeV}$ , it is not easy to access deviation Endo Moroi, MMN



We found no deviation for  $h \rightarrow gg$  channel for  $M_{\text{susy}} > 3000 \text{ GeV}$



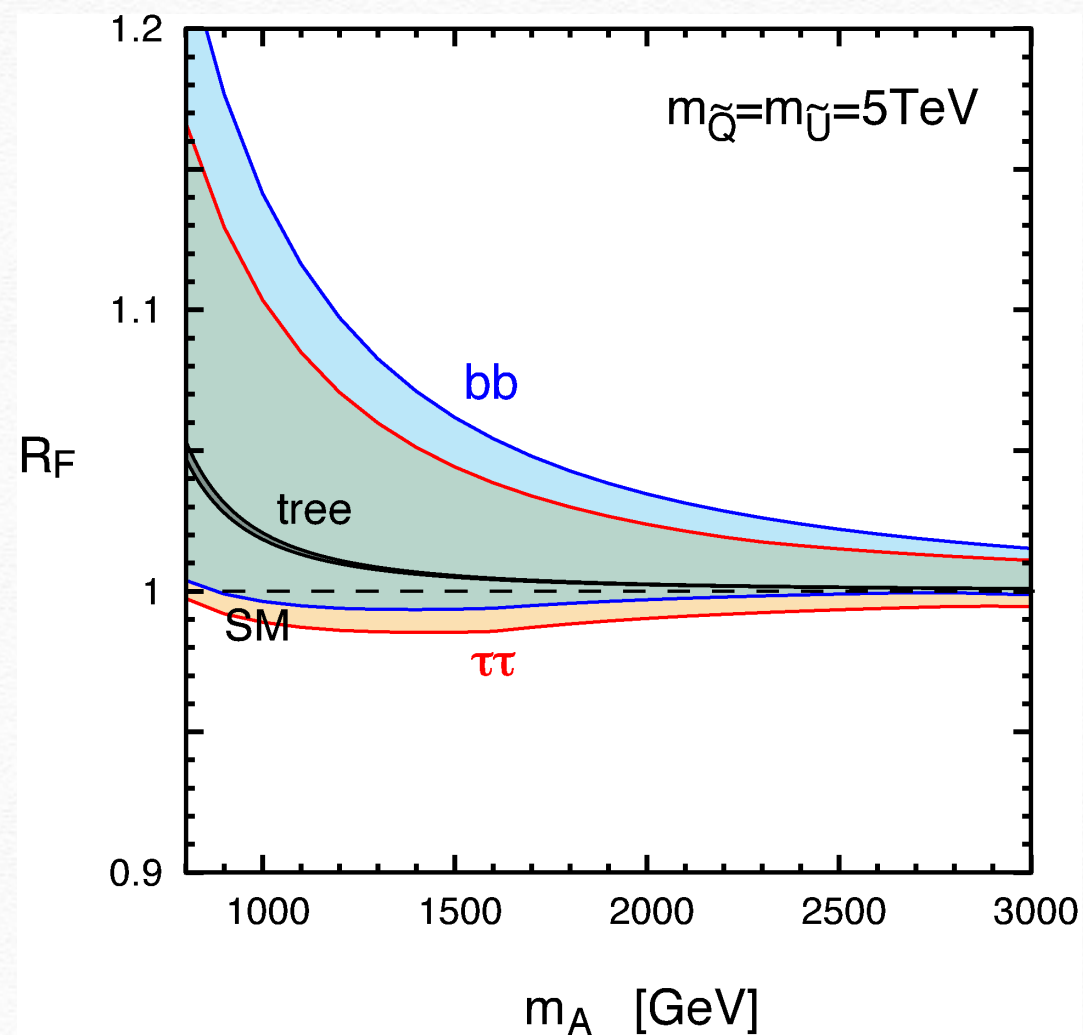
# If no deeper minimum required



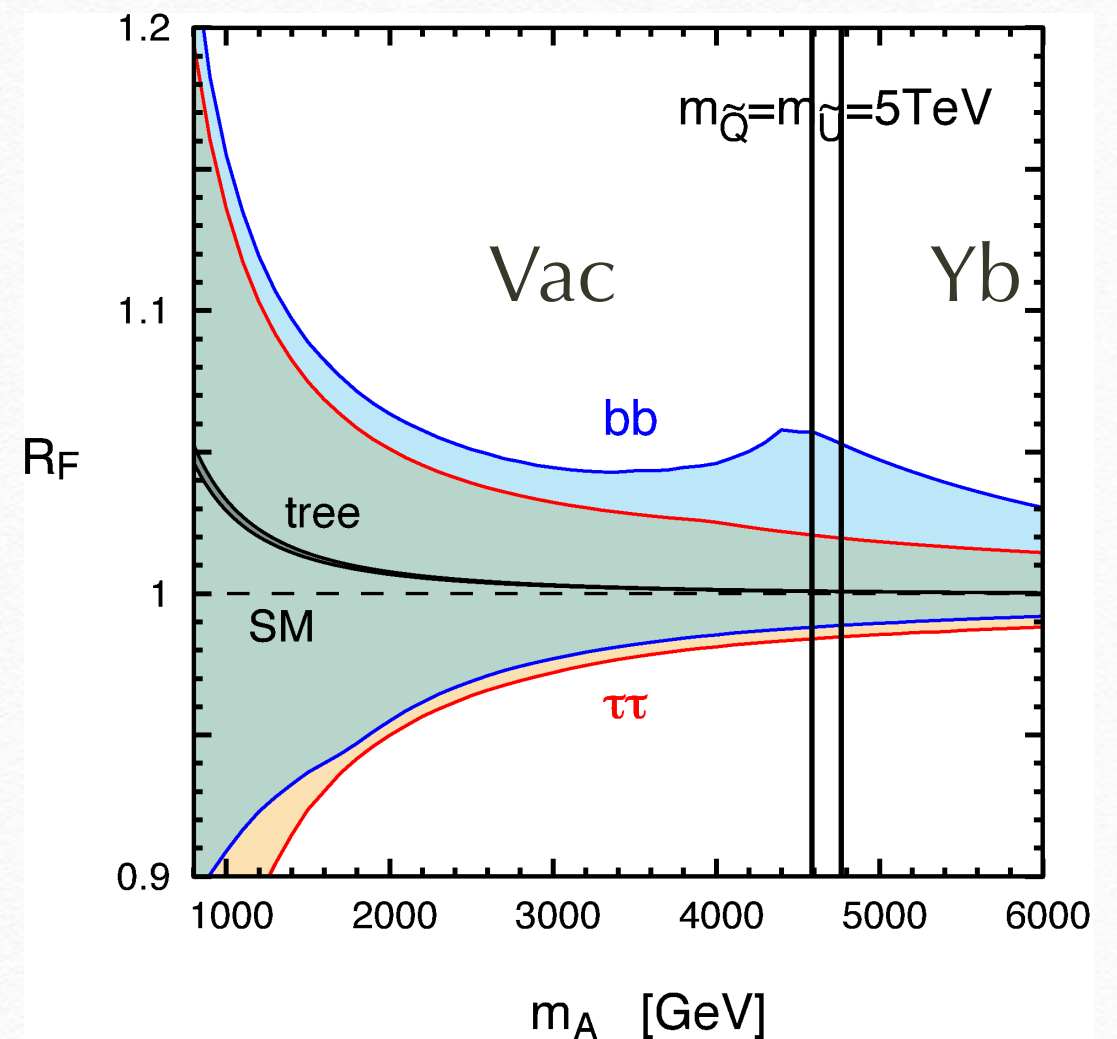


# Upper limit of deviations and large $A_t$ solutions

small  $A_t$  solutions



All solutions





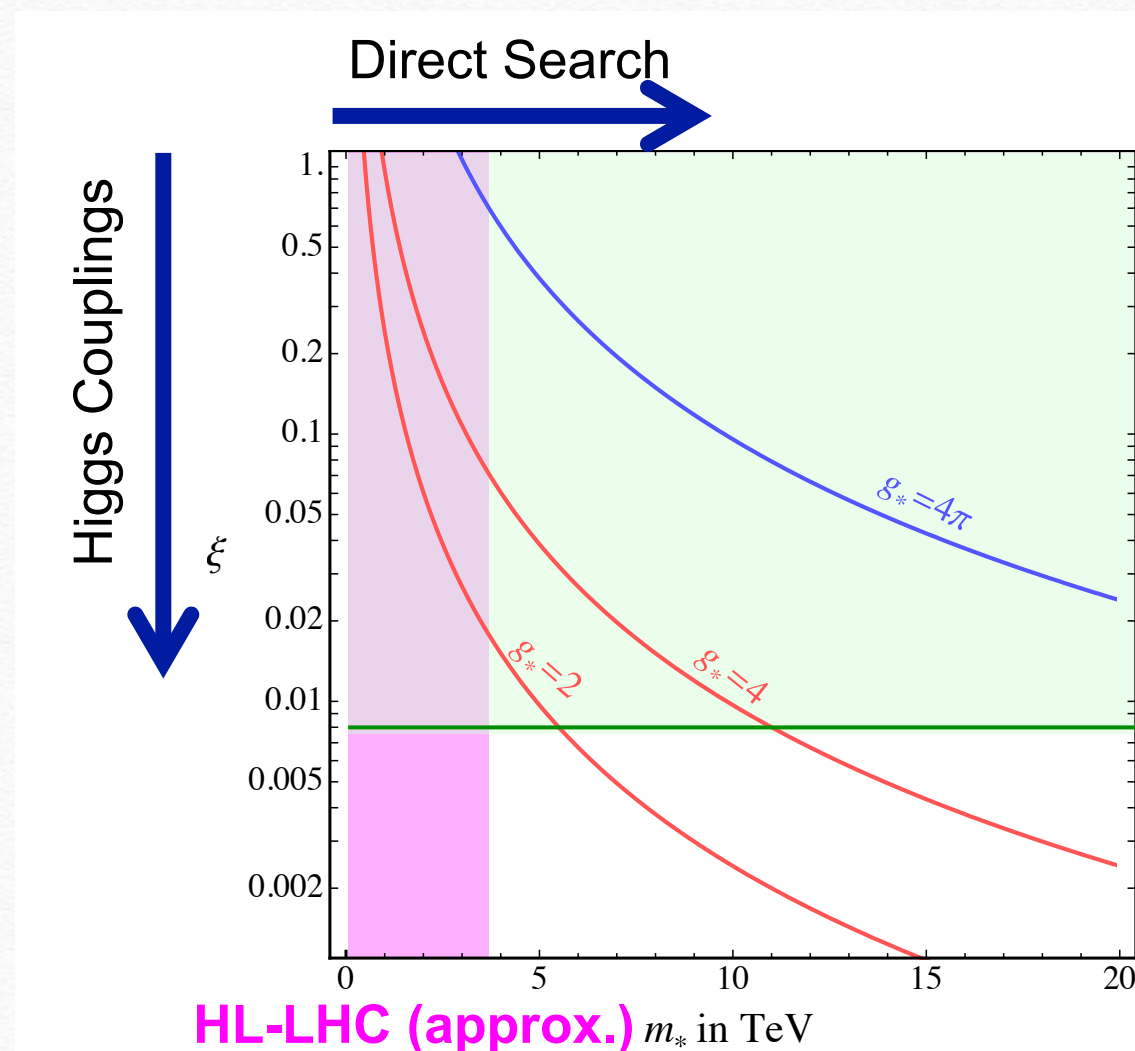
# Summary

- ❖ MSSM Higgs sector is more constrained after Higgs discovery.  
 $M_h = \text{fixed}$   $A$
- ❖ control parameter  $\Delta_b \rightarrow A_t, \mu,$
- ❖ **B decay and CCB constraint ( fragile)**
  - ❖  $B_s \rightarrow \mu\mu$  sensitive for non-universal squark mass
  - ❖ CCB vacua  $\rightarrow$  tree level calculation. Inclusion of leading SUSY QCD correction is important.
- ❖ Need to pay attention if public packages are doing right job in several TeV range, and  $O(1\%)$  deviation.



# Minimal Composite Higgs Model

- ❖ Higgs boson from  $SO(5) \rightarrow SO(4)$
- ❖ Higgs boson  $\sim$  PNC boson. Mass of the Higgs boson arise from correction of elementary sector.



Robust Correction to  $H \rightarrow ZZ$

$$\xi = \frac{g_*^2}{m_*^2} v^2$$

$$\frac{g_{hVV}}{g_{h_{SM}VV}} = \sqrt{1 - \xi}$$

**ILC**

$$\frac{\Delta g_{hVV}}{g_{hVV}} = 0.4\%$$



# Origin of Yukawa coupling

Composite state

$$\psi_u^5 = \frac{1}{\sqrt{2}} \begin{pmatrix} B_u - X_u \\ -i(B_u + X_u) \\ T_u + U_u \\ i(T_u - U_u) \\ \sqrt{2}\tilde{T}_u \end{pmatrix}, \quad \psi_d^5 = \frac{1}{\sqrt{2}} \begin{pmatrix} B_d - X_d \\ -i(B_d + X_d) \\ T_d + U_d \\ i(T_d - U_d) \\ \sqrt{2}\tilde{T}_d \end{pmatrix},$$

Elementary-Composite mixing

$$\mathcal{L}_{mix}^5 = y_{uL}^5 f(\bar{Q}_{uL}^5)^I U_{IJ} \psi_{uR}^5{}^J + y_{uR}^5 f(\bar{T}_R^5)^I U_{IJ} \psi_{uL}^5{}^J \\ + y_{dL}^5 f(\bar{Q}_{dL}^5)^I U_{IJ} \psi_{dR}^5{}^J + y_{dR}^5 f(\bar{B}_R^5)^I U_{IJ} \psi_{dL}^5{}^J + h.c.,$$

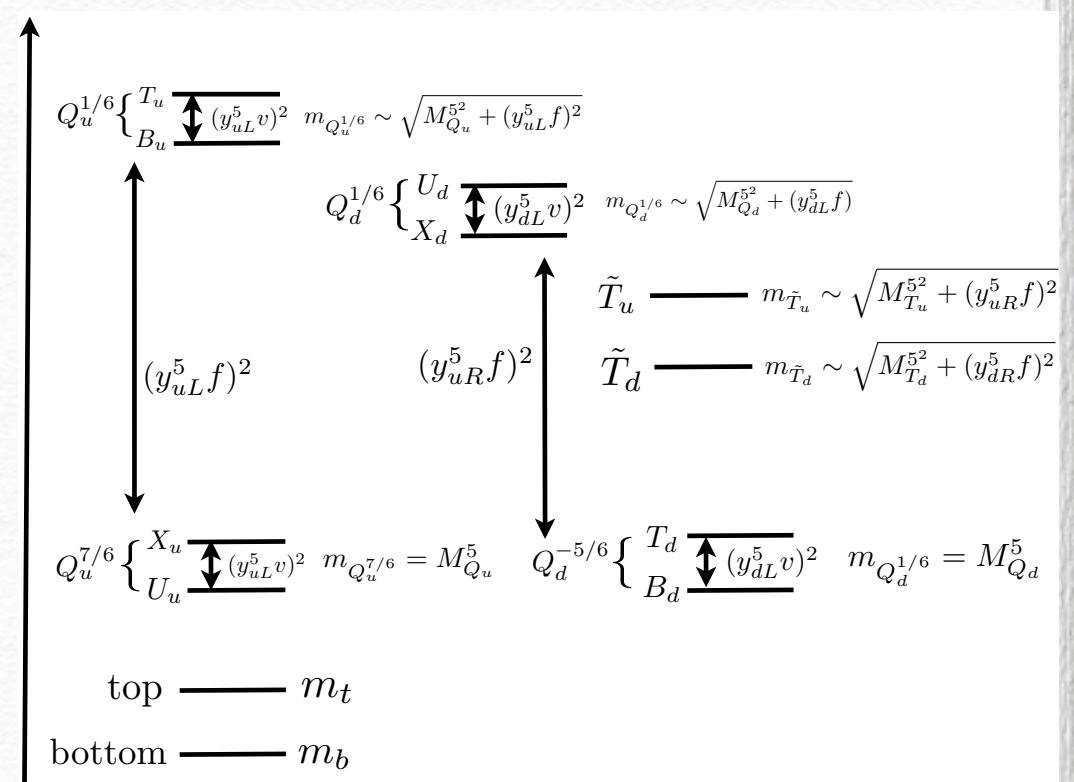
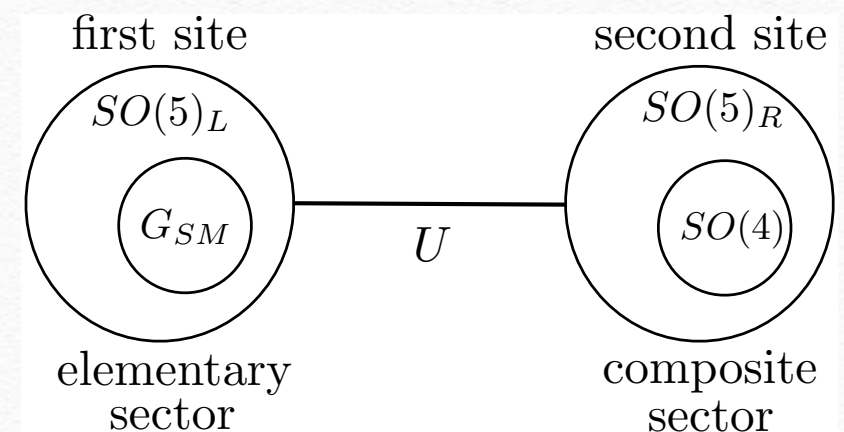
Composite mass

$$\mathcal{L}_{mass}^5 = -M_{Q_u}^5 \bar{Q}_u \tilde{Q}_u - M_{T_u}^5 \bar{T}_u \tilde{T}_u - M_{Q_d}^5 \bar{Q}_d \tilde{Q}_d - M_{T_d}^5 \bar{T}_d \tilde{T}_d + h.c$$

❖ Higgs boson does not have direct hff coupling

❖ Composite fermions mix to the elementary sector inducing Yukawa coupling. (top partner, bottom partners) → corrections

two site model





# Higgs to Fermion...

top and bottom Yukawa coupling correction

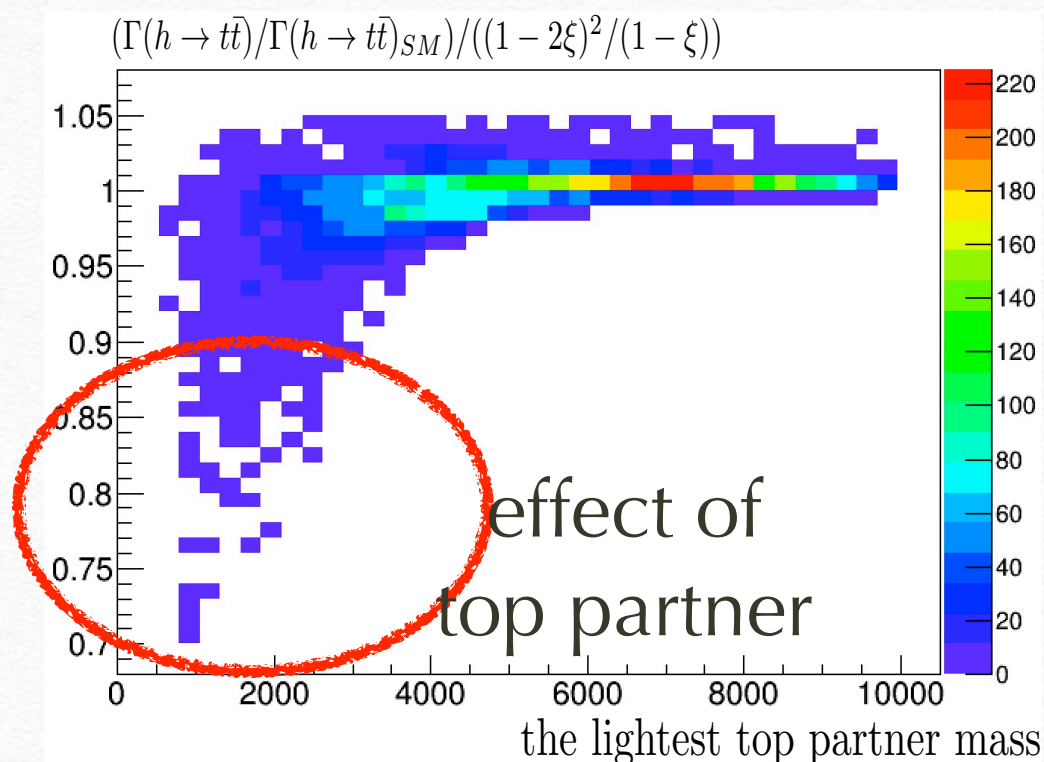
Kubota Nojiri to appear

$$\frac{y_u^5}{m_u^5} = \frac{1}{m_u^5} \frac{\partial m_u^5}{\partial v} = \frac{2}{f \tan(2v/f)} + \frac{f}{2Z_q^5 Z_{uR}^5} \sin(2v/f) \left[ \left( \frac{1}{|M_{u4}^5|^2} - \frac{1}{|M_{u1}^5|^2} \right) (|y_{uL}^5|^2/2 - |y_{uR}^5|^2) \right. \\ \left. + \left( \frac{1}{|M_{d4}^5|^2} - \frac{1}{|M_{d1}^5|^2} \right) |y_{dL}^5|^2/2 - \frac{f^2 |y_{uR}^5|^2}{2} \left( \frac{1}{|M_{u4}^5|^2} - \frac{1}{|M_{u1}^5|^2} \right) \left( \frac{|y_{uL}^5|^2}{|M_{u4}^5|^2} + \frac{|y_{dL}^5|^2}{|M_{d4}^5|^2} \right) \right],$$

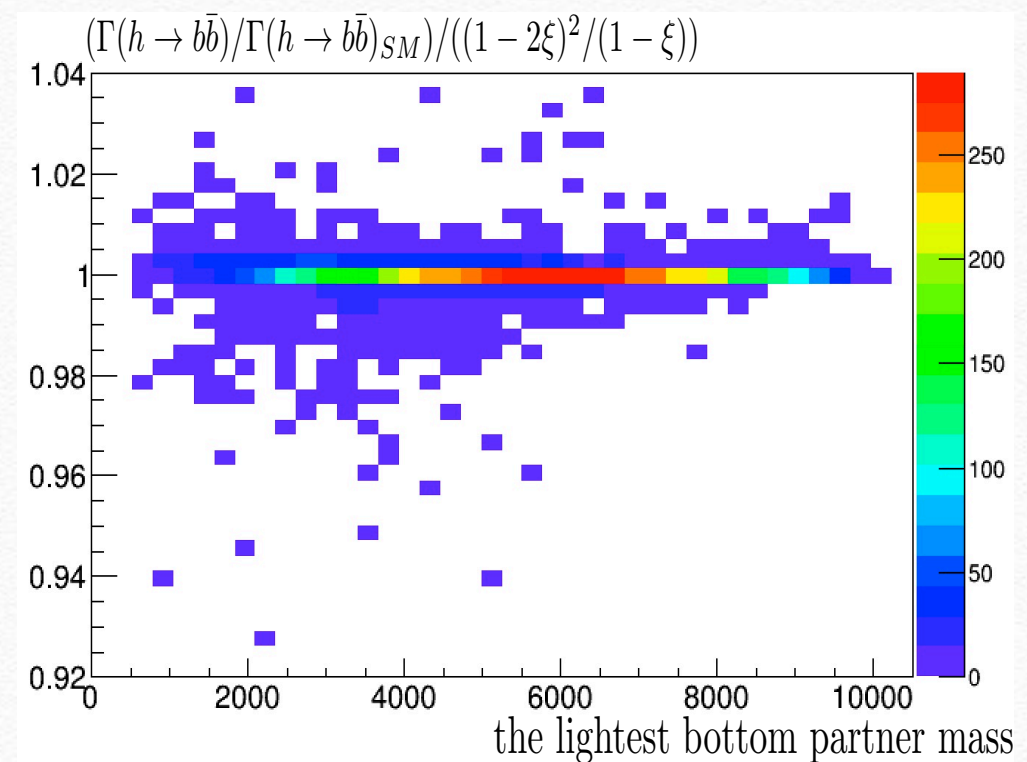
leading terms can be estimated by  $\xi$

5 representation model

$$g_{htt}^2 / [(1-2\xi)^2 / (1-\xi)]$$



$$g_{hbb}^2 / [(1-2\xi)^2 / (1-\xi)]$$





# Higgs to Fermion...

top and bottom Yukawa coupling correction

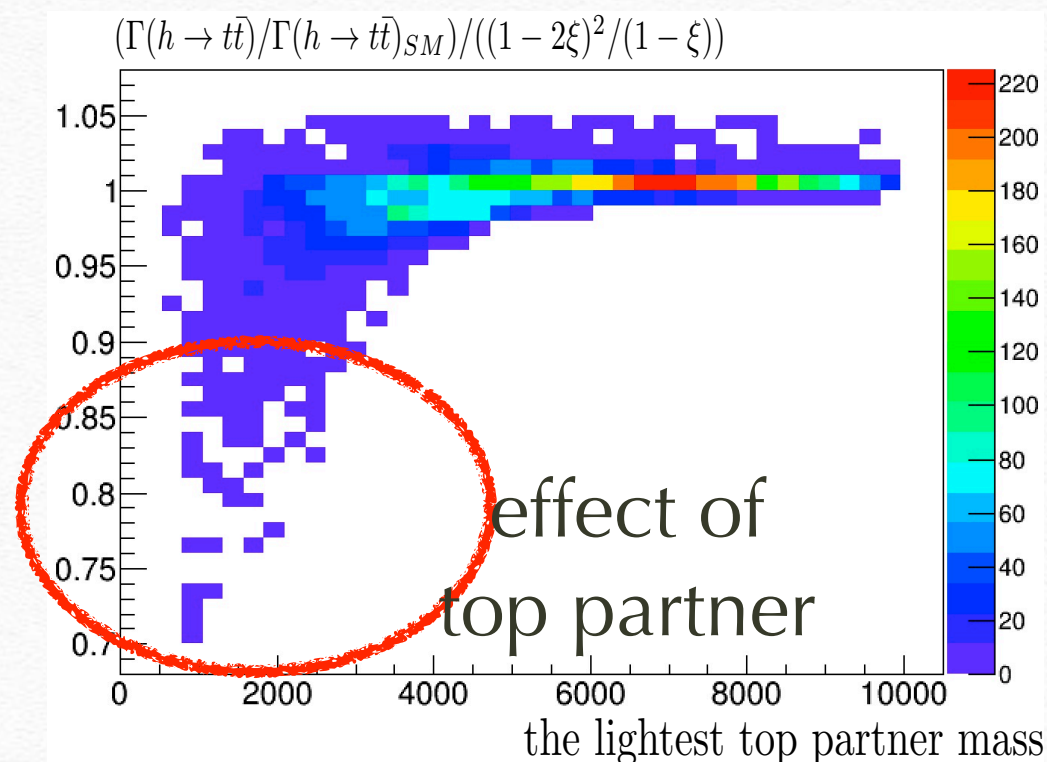
Kubota Nojiri to appear

$$\frac{y_u^5}{m_u^5} = \frac{1}{m_u^5} \frac{\partial m_u^5}{\partial v} = \frac{2}{f \tan(2v/f)} + \frac{f}{2Z_q^5 Z_{u_R}^5} \sin(2v/f) \left[ \left( \frac{1}{|M_{u_4}^5|^2} - \frac{1}{|M_{u_1}^5|^2} \right) (|y_{uL}^5|^2/2 - |y_{uR}^5|^2) \right. \\ \left. + \left( \frac{1}{|M_{d_4}^5|^2} - \frac{1}{|M_{d_1}^5|^2} \right) |y_{dL}^5|^2/2 - \frac{f^2 |y_{uR}^5|^2}{2} \left( \frac{1}{|M_{u_4}^5|^2} - \frac{1}{|M_{u_1}^5|^2} \right) \left( \frac{|y_{uL}^5|^2}{|M_{u_4}^5|^2} + \frac{|y_{dL}^5|^2}{|M_{d_4}^5|^2} \right) \right],$$

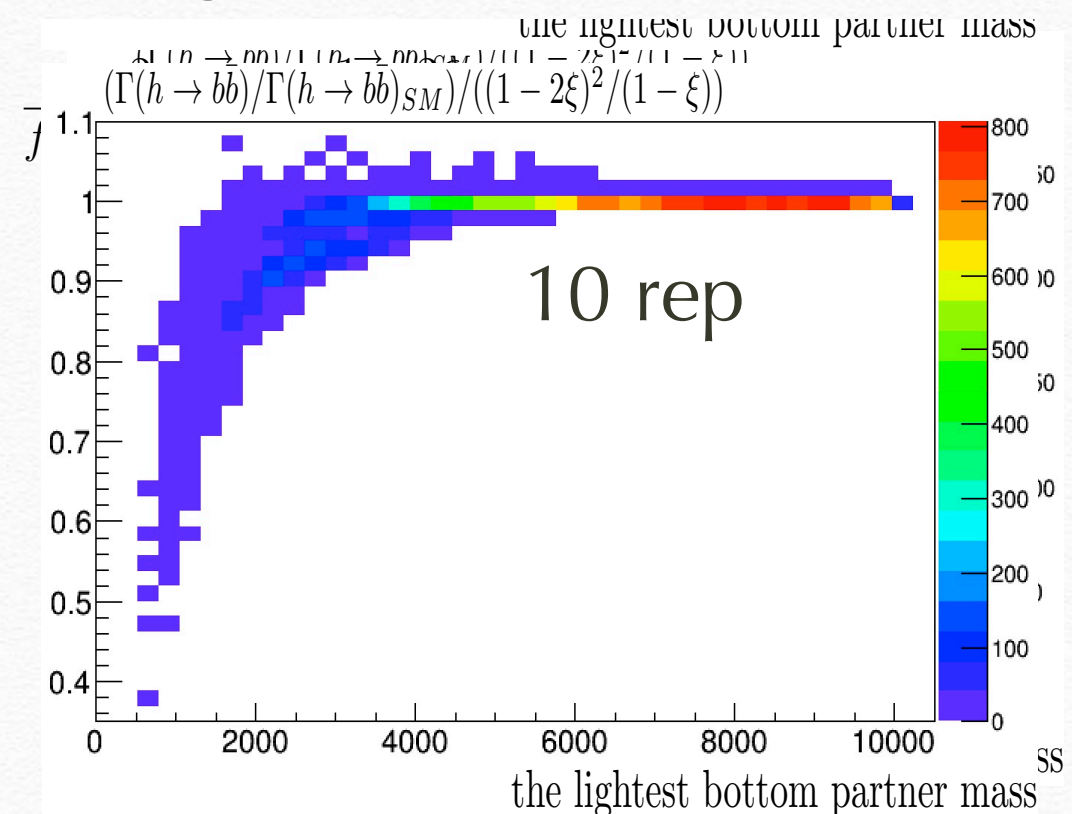
leading terms can be estimated by  $\xi$

5 representation model

$$g_{htt}^2 / [(1-2\xi)^2 / (1-\xi)]$$



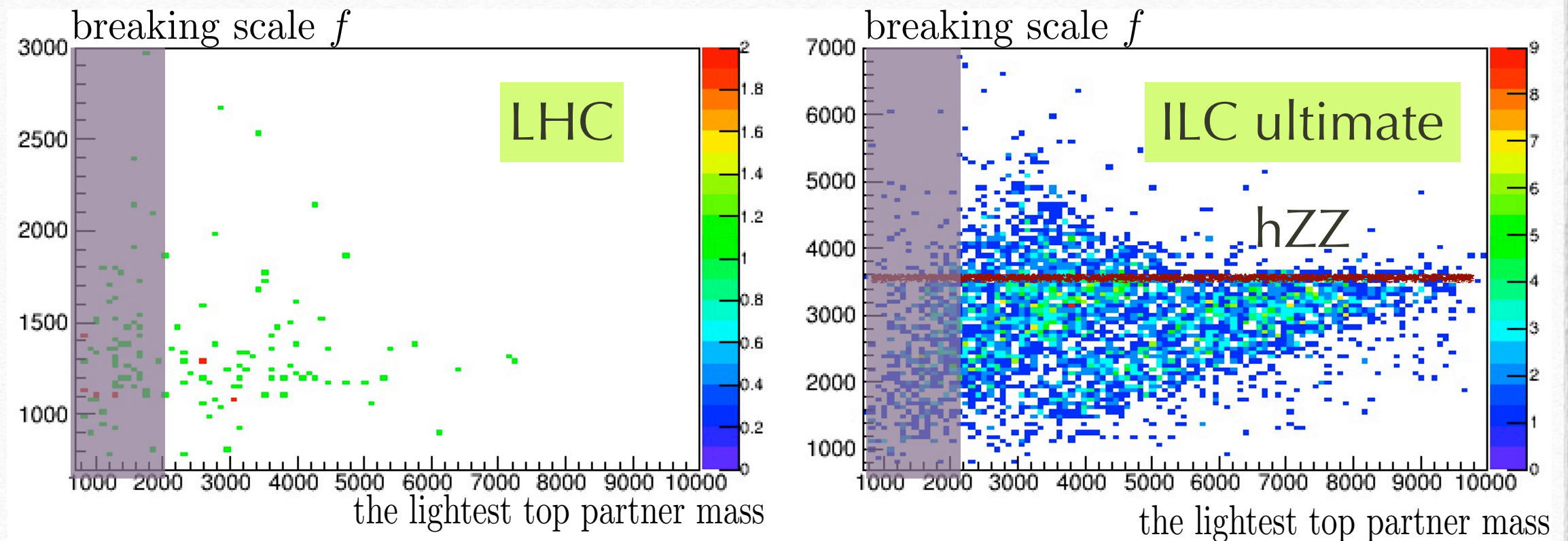
$$g_{hbb}^2 / [(1-2\xi)^2 / (1-\xi)]$$





# LHC vs ILC on accessibility Higgs coupling only

Kubota Nojiri to appear



Direct search at the Hadron Collider

Cross section based estimate

$m_X \sim 2\text{TeV}$  at 14TeV

$m_X \sim 7\text{TeV}$  at 100TeV

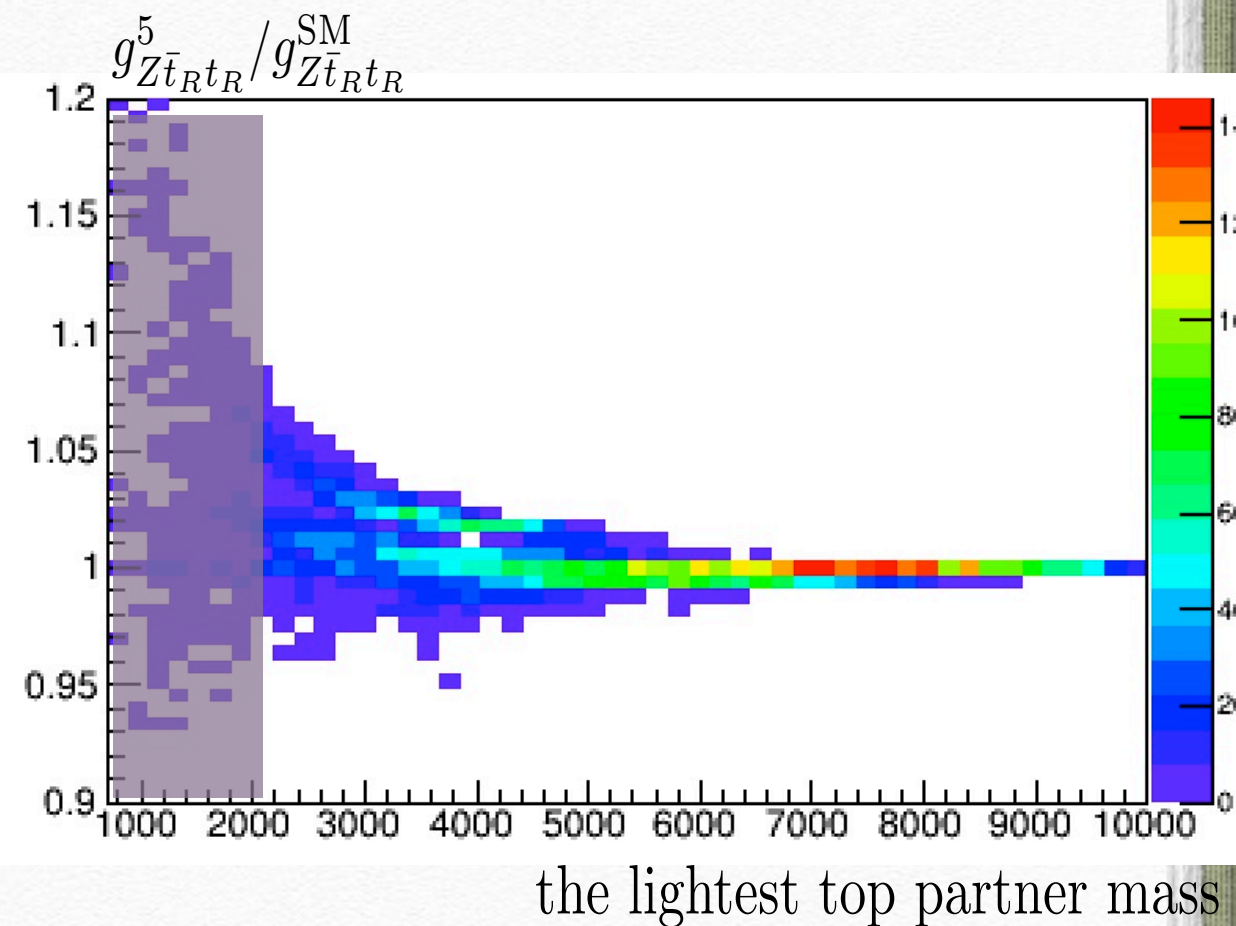
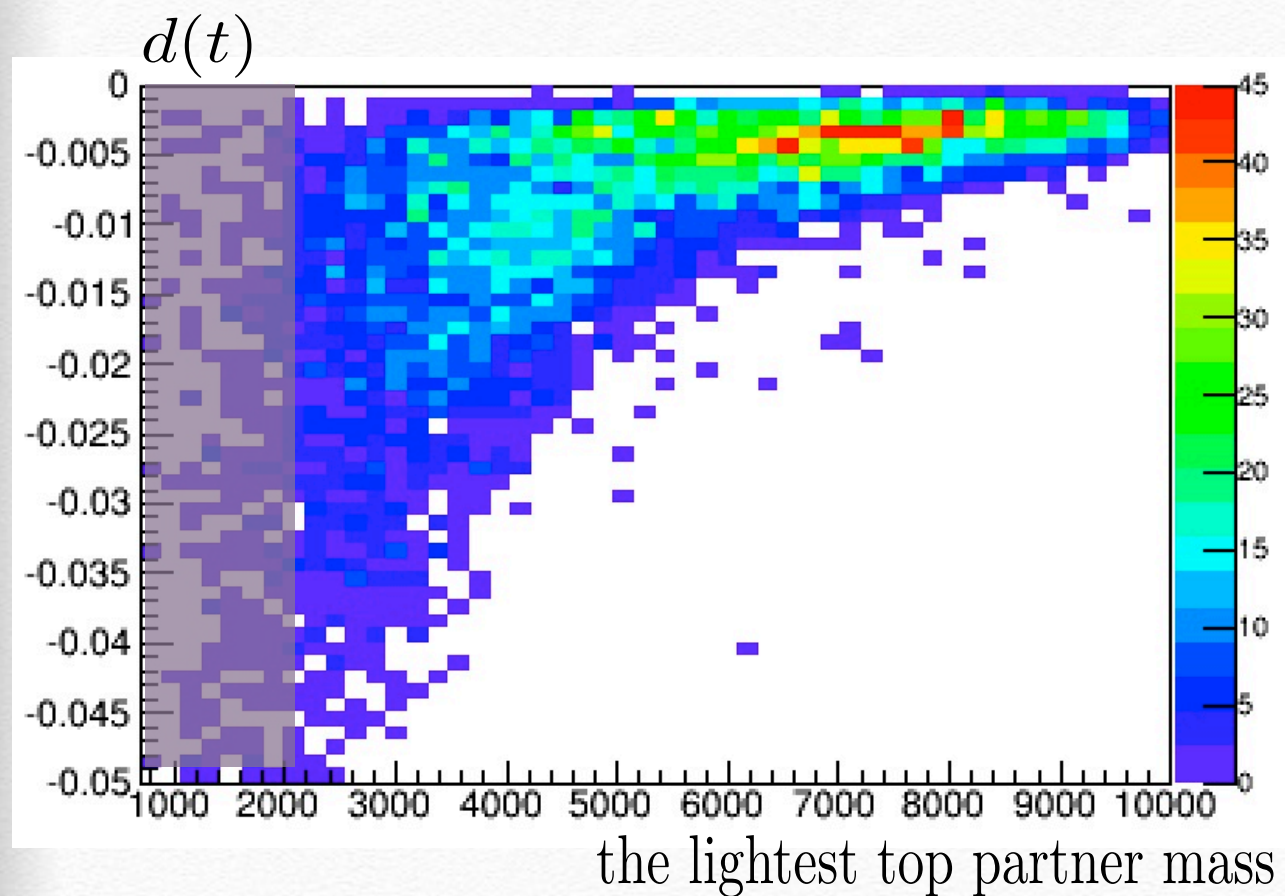
single production  $m_X \sim 12\text{TeV}$  at 100TeV



# $ttH$ vs $ttZ$

top Yukawa coupling

$ttZ(R)$  coupling



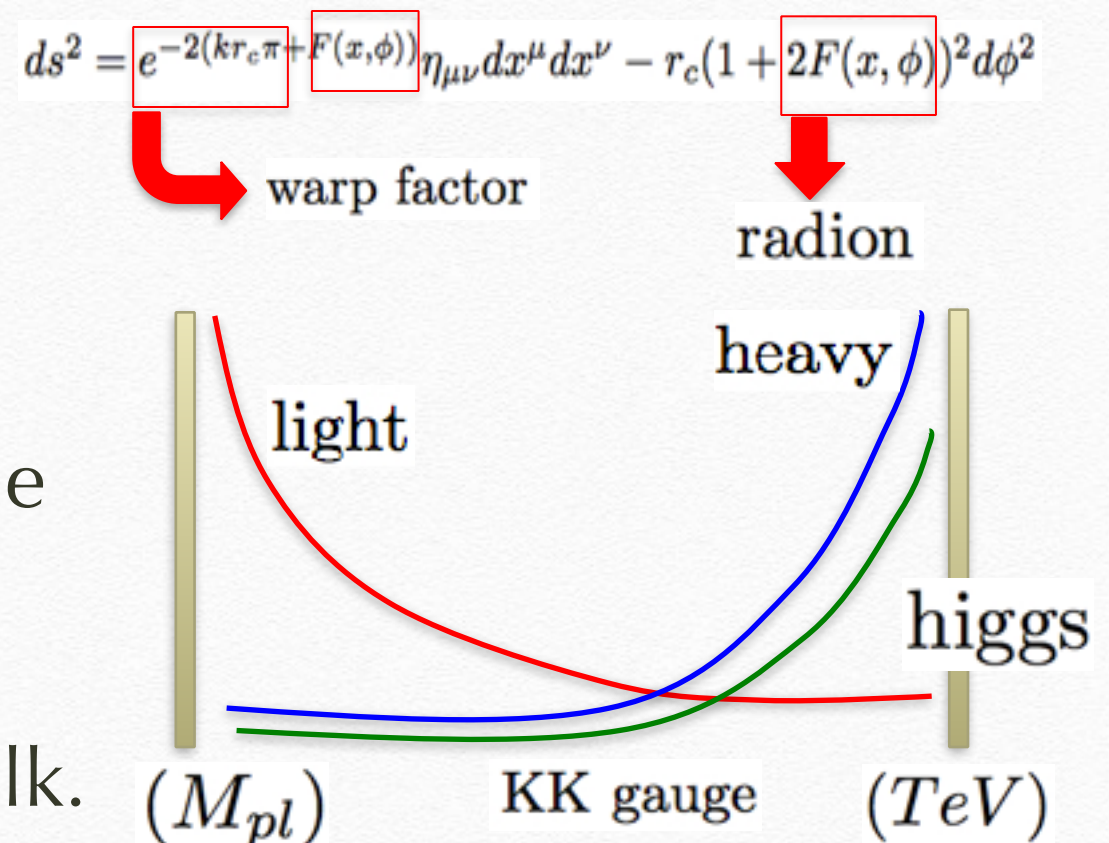
Relatively large correction to the top quark of order of 5% for both

$\sigma(ttZ)/\sigma(ttH)$  at VLHC?



# RS model

- ❖ 5 dim model but 5th dimension is not flat.
- ❖ All mass parameters are at Planck scale but Higgs boson on IR brane has light mass. warp factor
- ❖ matter and gauge boson in the bulk. bulk mass  $\rightarrow$  wave function profile
- ❖ Large KK corrections to loop process because KK modes live near IR brane. negative correction to  $gg \rightarrow h$
- ❖ Radion Higgs mixing : enhancement of  $\gamma\gamma$   $gg$  final state





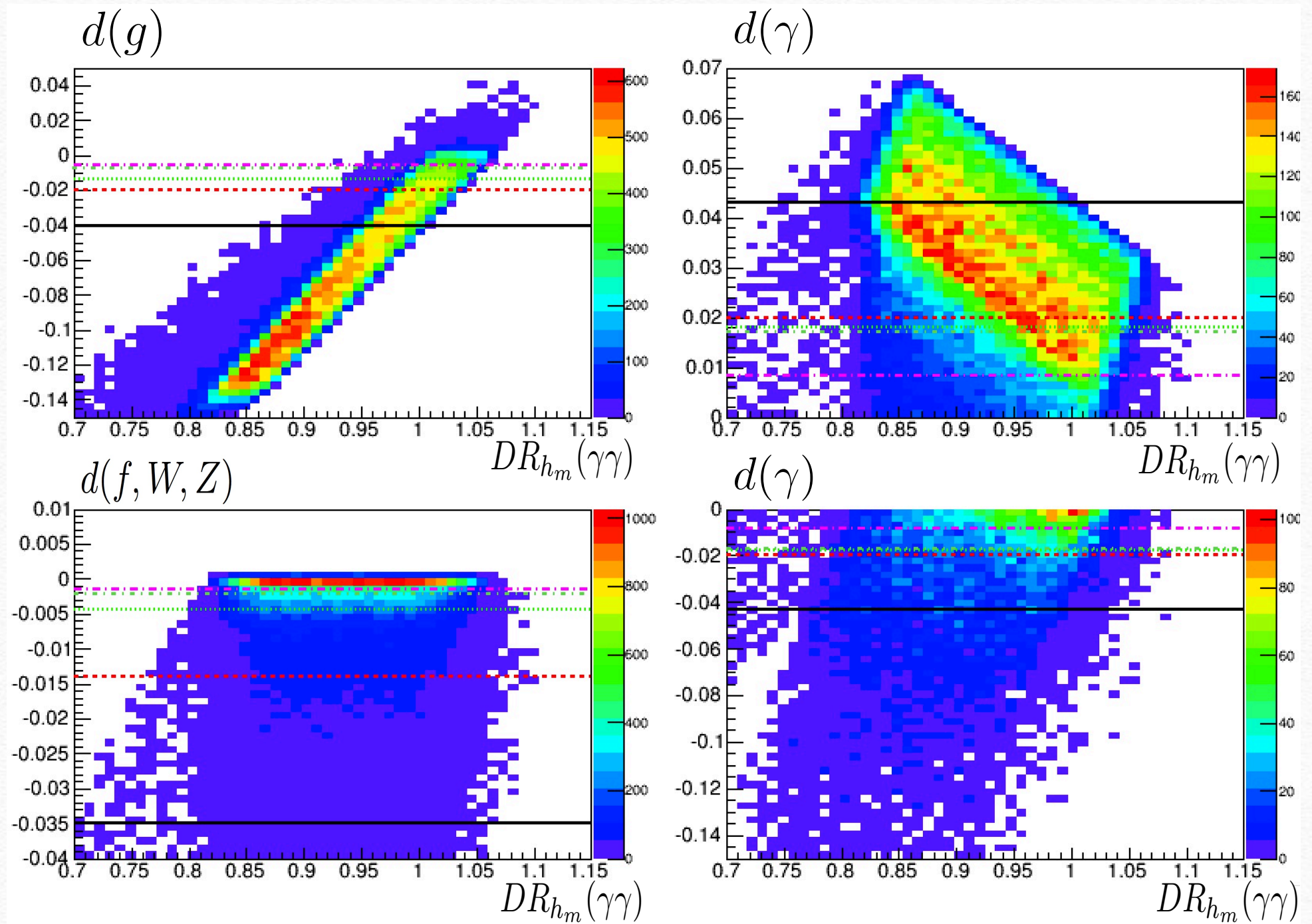


FIG. 7: Distributions of our model points in  $DR_{hm}(\gamma\gamma)$ - $d(A)$  plane, where  $d(A)$  is (a)  $d(g)$ , (b)  $d(f, W, Z)$ , (c)  $d(\gamma)$  with  $d(\gamma) > 0$  and (d)  $d(\gamma)$  with  $d(\gamma) < 0$ . Expected  $1\sigma$  sensitivity of the each coupling is also shown in the figure(see text).



# maximal deviation of the couplings

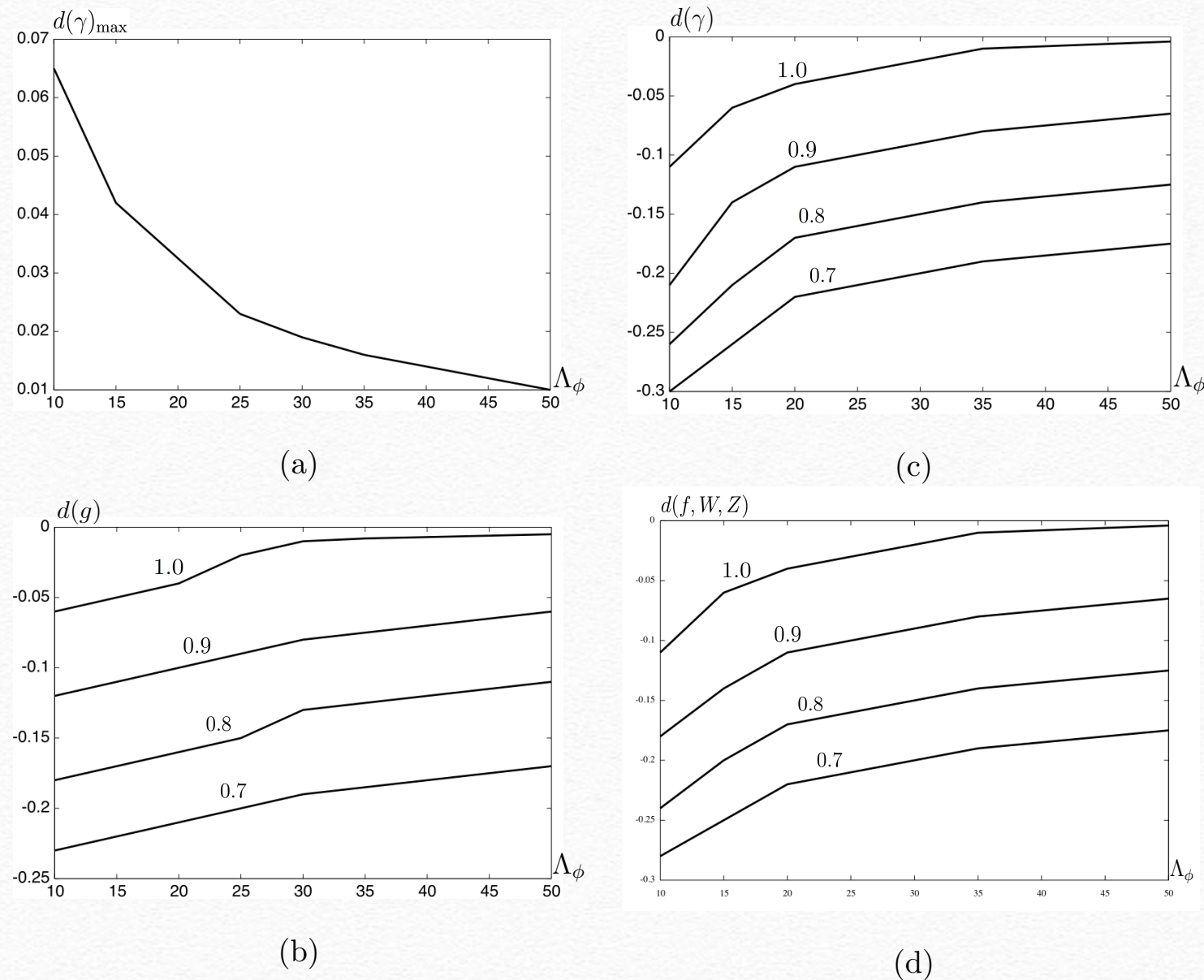


FIG. 4: The maximal deviations of  $d(A)$ , where  $d(A)$  is (a)  $d(\gamma) > 0$ , (b)  $d(g)$ , (c)  $d(\gamma)$  and (d)  $d(f, W, Z)$  vs  $\Lambda_\phi$  at  $DR_{h_m}(\gamma\gamma) = 0.7, 0.8, 0.9, 1.0$ .